



## Depletion Reactivity Benchmarks Derived from Measured Pressurized Water Reactor Flux Maps

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Washington, DC

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### Contributors

- Prof. Kord Smith, MIT
  - Prof. Benoit Forget
  - Nick Horelik
  - Bryan Herman
  - Geoffrey Gunow
- Dr. Dale Lancaster, NuclearConsultants.com
- Studsvik Team
  - Tamer Bahadir
  - Rodolfo Ferrer
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## Burnup Credit Standard, ANSI/ANS-8.27

$$k_p + \Delta k_p + \Delta k_d + \Delta k_b \leq k_c - \Delta k_c - \Delta k_m$$

$k_p$  is the calculated k from the rack model

$\Delta k_p$  is the bias and uncertainty in the rack model

$\Delta k_b$  is the uncertainty in the burnup

$k_c$  is the mean of the critical experiments

$\Delta k_c$  is the uncertainty about the mean given in  $k_c$

$\Delta k_d$  is the bias and uncertainty associated with depletion;  
it includes the uncertainties associated with isotopic content  
and worth (cross sections)

$\Delta k_m$  is an administrative margin, typically 5%

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## Problem Statement

Existing criticality benchmarks have been portrayed as insufficient by regulators in light of operational/licensing changes being sought by utilities

## Desired Outcome

Depletion uncertainty approaches that could increase licensee flexibility in addressing spent fuel criticality concerns

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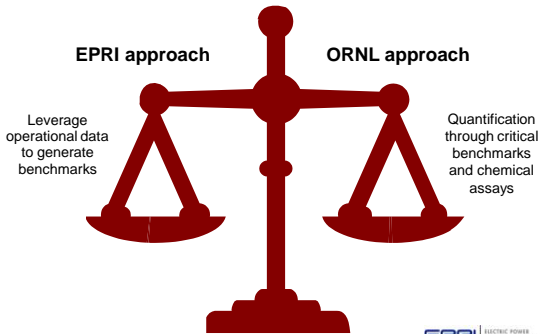
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## Depletion Uncertainty Quantification



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## Basis For The EPRI Uncertainty Methodology

1. Critical LWR cores provide a continuous source of measured reactivities for both fresh and depleted fuel assemblies at full-power conditions
2. Predictions of in-core reaction rate spatial distributions are very sensitive to the accuracy of computed assembly reactivities
3. By examining thousands of in-core measurements (flux maps), the burnup dependence of the error in computed assembly reactivities (and its uncertainty) can be deduced

Goal: **Experimental** benchmarks of burnup reactivity decrement, which are independent of analysis codes

## Reactor Data

Unit	Cycles	Cycle Length (EFPD)	Enrichment Range (%)	H2P Boron (ppm)	Maximum LWR # Pins	Maximum WRA # Pins	Maximum WRA+PRA # Pins
Microtur-1	10 to 21	363 - 514	3.40 - 4.55	1576 - 2060	24	128	24 + 128
Microtur-2	10 to 20	428 - 512	3.64 - 4.90	1680 - 2037	24	128	24 + 128
Catawba-1	9 to 19	407 - 522	3.45 - 4.75	1501 - 2104	24	128	16 + 128
Catawba-2	8 to 17	451 - 527	3.50 - 4.90	1819 - 2100	24	128	20 + 128

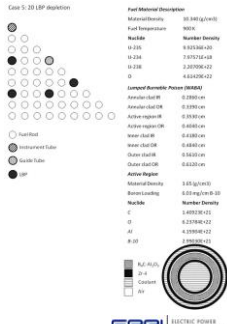
Cycle	Enrichment (%)	# of Assemblies	Cycle Length (EFPD)	Enrichment Range (%)	# of Assemblies
10	3.40	4	10	3.40-3.55	2
11	3.55	4	10	3.55-3.70	2
12	3.70	4	10	3.70-3.85	2
13	3.85	4	10	3.85-4.00	2
14	4.00	4	10	4.00-4.15	2
15	4.15	4	10	4.15-4.30	2
16	4.30	4	10	4.30-4.45	2
17	4.45	4	10	4.45-4.60	2
18	4.60	4	10	4.60-4.75	2
19	4.75	4	10	4.75-4.90	2
20	4.90	4	10	4.90-5.05	2
21	5.05	4	10	5.05-5.20	2

Involved processing  
~1 million measured signals  
from 680 flux maps  
covering 44 cycles  
from 4 reactors

## Product : 11 Reactivity Decrement Benchmarks for PWR 17 x 17 Design

1	3.25% Enrichment
2	3.50% Enrichment
3	4.25% Enrichment
4	off nominal pin diameter depletion
5	20 LWR depletion
6	104 WRA depletion
7	104 WRA plus 20 LWR depletion
8	high boron depletion/1500 ppm
9	branch to hot rack (1500 coolant/fuel)/1338.7%
10	branch to high rack boron = 1500 ppm
11	high power depletion/typical, coolant/fuel temp)

Case	Burnup (GWd/7)				
	10	20	30	40	50
1	-0.1329	-0.2139	-0.3211	-0.3954	-0.4554
2	-0.1146	-0.2021	-0.2806	-0.3545	-0.4238
3	-0.1223	-0.2157	-0.2990	-0.3758	-0.4445
4	-0.1207	-0.2176	-0.3075	-0.3931	-0.4715
5	-0.2045	-0.2335	-0.2998	-0.3717	-0.4372
6	-0.1726	-0.2215	-0.2968	-0.3726	-0.4418
7	-0.2524	-0.3169	-0.3961	-0.3626	-0.4363
8	-0.1216	-0.2129	-0.2932	-0.3662	-0.4310
9	-0.1237	-0.2171	-0.2998	-0.3756	-0.4432
10	-0.0967	-0.1784	-0.2530	-0.3217	-0.3826
11	-0.1235	-0.2149	-0.2945	-0.3664	-0.4259



## Utilization – Comparison with SCALE (ENDF/B-VII) Burnup Dependence (Benchmarks 1 thru 3)

- The uncertainty in the benchmarks is 0.00643 in k. The bias depends on the codes and cross sections used in the criticality analysis.
- For SCALE 6.1 and ENDF/B-VII the following is a table of the biases. Negative biases are ignored.

Burnup	Bias (SCALE $\Delta k$ - Benchmark $\Delta k$ )		
	3.25 wt% U-235	4.25 wt% U-235	5 wt% U-235
10	-0.0004	0.0005	0.0004
20	-0.0008	0.0002	0.0005
30	-0.0010	0.0001	0.0003
40	-0.0015	-0.0004	0.0006
50	-0.0014	0.0000	0.0005
60	-0.0022	-0.0005	0.0008

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## Comparison of the Reactivity Decrement Approach to the Kopp Guidance

- Assume the highest bias of all 11 benchmarks and all burnups
  - For ENDF/B-VII (SCALE) and 100-hour cooling, this is 0.0015 in k
  - To this, add the uncertainty of 0.00643

Burnup	EPRI	Kopp [Case #3]
10	0.0079	0.0061
20	0.0079	0.0108
30	0.0079	0.0150
40	0.0079	0.0188
50	0.0079	0.0222
60	0.0079	0.0251

← Small non-conservatism at low burnups

Large margin at discharge burnups

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## International Handbook of Evaluated Reactor Physics Benchmark Experiments (IRPhEP)

- Contains reactor physics benchmarks
  - Derived from experiments performed at nuclear experimental facilities
  - Intended for use by reactor physics personnel to validate calculational techniques
- 2012 Edition (May 2012)
  - Contains data from 56 different experimental series performed at 32 different reactor facilities
- EPRI-sponsored Benchmarks
  - Accepted as "Draft" by OECD/NEA Committee in October 2012 for publication in the 2013 edition of the Handbook
  - Submitted to OECD-NEA on January 21, 2013
  - Next logical step: Acceptance as "Final" in the 2014 Edition

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## IRPhEP Review

- Technically very sound reviews
  - Focus should be on Hot Full Power (HFP) conditions
    - Appendix for hot-to-cold conditions
    - **OK!**
  - Use of CASMO-SIMULATE as a reactivity meter
    - Would other tools give the same results?
    - **Only partially addressed!** → MIT's "BEAVERS" Project
  - Derivation of uncertainties
    - Completeness?
    - Provide data set?
    - **Best effort!** → MIT's "BEAVERS" Project
- Report formatting
  - Improvements required
    - **OK!**

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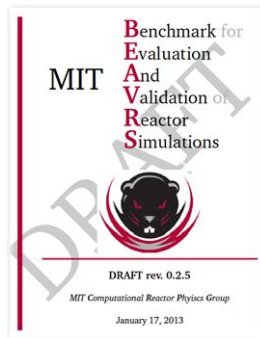
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## MIT's BEAVERS Project

- Opportunity: U. S. Utility made available two cycles of detailed, measured PWR operational data
- By performing core analysis with full-core CASMO models, one can eliminate dependences on nodal models/codes



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## Summary

- Experimental benchmarks of burnup reactivity decrement, which are independent of analysis codes, have been created
  - Benchmarks can be used to determine bias and uncertainty of applicant's specific analysis tools
- Ongoing work ongoing at MIT will provide opportunities for other analysts to independently verify the approach retained for creating the depletion reactivity benchmarks
- Regulatory review may be conducted as part of the review of NEI's *Guidance for Performing Criticality Analyses of Fuel Storage at Light-Water Reactor Power Plants* (to be formally submitted in March 2013 in support of a pilot-plant LAR)

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## EPRI Reports/Documents

1. "Benchmarks for Quantifying Fuel Reactivity Depletion Uncertainty" [Report 1022909 (August 2011)]
2. "Utilization of the EPRI Depletion Benchmarks for Burnup Credit Validation" [Report 1025203 (April 2012)]
3. "PWR Fuel Assembly Depletion Reactivity Determination Using PWR Fission Rate Measurements"
  - Benchmarks accepted as "Draft" for publication in the 2013 Edition of the OECD/NEA International Handbook of Evaluated Reactor Physics Benchmark Experiments [EPRI submittal finalized January 2013]
  - Pursuing OECD/NEA reviews for publication as "Final" in the 2104 Edition [To be finalized by January 2014]
4. "PWR Fuel Depletion Reactivity Verification and Uncertainty Using Flux Map Data" [EPRI Report (Planned Publication: Fall 2013)]

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