NOZ-FLAW: A FINITE ELEMENT PROGRAM FOR DIRECT EVALUATION OF STRESS INTENSITY FACTORS FOR PRESSURE VESSEL NOZZLE-CORNER FLAWS
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Sponsor: G. D. Whitman
Manuscript Completed - November 1980
Date Published - March 1981

Prepared for the
Office of Nuclear Regulatory Research
U. S. Nuclear Regulatory Commission

Washington, DC 20555
Under Interagency Agreements DOE 40-551-75 and 40-552-75
NRC FIN No. B0119

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Union Carbide Corporation, Nuclear Division operating the
Oak Ridge Gaseous Diffusion Plant . Oak Ridge National Laboratory Oak Ridge Y-12 Plant . Paducah Gaseous Diffusion Plant
under Contract No. W-7405-eng-26
for the
Department of Energy

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The work reported here was per:ormed at the Oak Ridge National I oratory and at the Georgia institute of Technology under UCC-ND Suncontract No, 7565. This work is sponsored by the U.S. Nuclear Regulatory Ccmmission's (NRC) Heavy-Section Steel Technology (HSST) Program which is directed at ORNL by G. D. Mitman. The manager for the NRC is M. Vagins.

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# NOZ-FLAW: A FINITE ELEMENT PROGRAM FOR VIRELT EVALUATION OF STRESS INTENSITY FACIORS FOR PRESSURE VESSEL NOZZLE-CORNER FLA* 

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ABSTRACT

This report describes a linear elastic finite element computer program (NOZ-FLAW) which is used for the direct evaluation of mixed-mode stress intensity factors ( $\mathrm{K}_{\mathrm{T}}, \mathrm{K}_{\mathrm{II}}, \mathrm{K}_{\mathrm{IIr}}$ ) along user-defined crack flaws at pressure-vessel nôzzle cornêrs. Special three-dimensional crack front elements are used to model the immediate vicinity of the flaw. These crack front elements have the proper square root and inverse square root variations for displacements and stresses, respectively. Regular isoparametric elements are used away fromi the flaw front. Inter-element displacement compatibility between singular and regular elements is satisified by assuming an independent boundary displacement field and using a Lagrange multiplier technique to enforce the compatibility constraint. The stress intensity factors at various points on the crack front are solved for directly along with the unknown nodal displacements. The program provides for automatic generation of a finite element model incorporating either a mathematical or user-defined crack flaw. Generation and analysis of the model are performed with program input consisting of 8 to 12 cards. Applications of the program to several crack flaws in an intermediate test vessel are described.

## 1. INTRODUCTION

A primary concern in the fracture safety analysis of a nuclear pressure vessel is the nozzle corner flaw located in the longitudinal plane, i.e., the plane containing both the nozzle and vessel axes (see Figure 1). Under cyclic pressure loading, the high hoop stresses at the inside nozzle corner may promote buth initiation and propagation of such flaws. Certain cyclic pressure experiments [1] have shown that fatigue cracks form first at this location. In addition, such cracks have occurred from thermal fatigue in boiling water reactor feedwater nozzles [2]. These flaws may lead to fast fracture at low temperatures if they grow by fatigue to a critical size. Thus, development of accurate fracture analysis methods zpplicable to such flaws is essential to assessing the structural integrity of reactor vessels.

In applications of linear elastic fracture mechanics (LEFM) to three-dimensional structures, the intensity of the elevated stress field near a crack flaw is characterized by mixed-mode stress intensity factors $\mathrm{K}_{\mathrm{I}}, \mathrm{K}_{\mathrm{II}}$ and $\mathrm{K}_{\text {III }}$ that depend upon geometry and applied loading (see, for example, (3才). These factors have been accepted as the appropriate parameters governing fatigue crack propagation and failure by brittle fracture. For nozzle corner flaws, the evaluation of these K-factors is complicated by the geanetry of the nozzle-vessel junction containing the flaw, as well as by the complex state of stress present for loadings of practical interest. A further complication arises from the stress intensity factors being undefined at the nozzle and vessel free surfaces. An early attempt to estimate K-factors for a nozzle corner crack was ade by Yukawa [4]. He combined the known solutions for a through crack emanating from a circular hole in a flat plate under uniaxial and equibiaxial tension [5] with a crack-shape reduction factor. This factor was based on the ratio of the stress intensity factor for a corner crack [6] to that for a through edge crack in a rectangular bar under uniform tension. More recently, various finite element methods have been employed [712]. Alternative numerical methods which generally require a solution for the hoop stresses in the crack area of the uncracked geometry have also been developed [13-16]. Stress intensity factors for nozzle corner flaws have been experimentally determined from burst tests on epoxy models [17] and from frozen-stress photoelastic techniques $[18,19]$.


Figure 1. Nozzle comer flaw in longitudinal plane

A critical evaluation of these results indicates that calculation of reliable stress intensity factors for nozzle corner flaws is still very much an open issue. For example, investigators have reported significantly different variations of the mode I factor, $K_{T}$, along the crack front for similar geometries and applied Joads. Môst of the numerical procedures compute a $K_{\text {a }}$ variation that has a relative maximum near the free surface and a relative minimum near the midpoint of the crack front (see, for example, [10-15]). In contrast, the photoelastic results of References 18, 19 demonstrate an opposite trend. Furthermore, most of the numerical techniques to date introduce simplifications or approximations necessary to make the nozzle corner flaw problem mathematically tractable. Modeling the crack. flaw as a quarter circle or quarter ellipse is a typical device, whereas certain experimental evidence $[18,19]$ indicates that this may be an oversimplification.

The need tor improved fracture analysis capability in reactor safety research has prompted the Nuclear Regulatory Cormission (NRC) to sponsor development of a linear elastic finite element program designed to calculate mixed-mode K-factors for nozzle corner flaws. Funding of this work is through the Heavy Section Steel Technology (HSST) program at the Oak Ridge National Laboratory (ORNL). The computer program NOZ-FLAW described herein is a product of this effort. nevelopment of program NOZ-FLAW was initiated under a subcontract to Professor S. N. Atluri at the Georgia Institute of Technology, with Dr . K. Kathiresan responsible for program design. The core of NOZ-FLAW was formed, prior to ORNL sponsorship, by installing a special hybrid-displacement crack-tip element proposed by Atluri and Kathiresan $[20,21]$ in the three-dimensional finite element program TEXGAP3D [22]. This program was then interfaced with the automatic mesh generator module AUTO, also developed under the subcontract, to complete the NOZ-FLAW package. Module AUTO was designed to produce a complete finite element model of a reinforced nozzle-cylinder connection containing a corner crack flaw using relatively few input cards. However, the subcontract with Professor Atluri expired before AUTO could be made operational according to the original ORNL specifications. Consequently, the NOZ-FLAW package was transmitted to ORNL with the mesh generation fature unfinished.

Technical staff in Computing Applications Engineering Department (CAD) and the HSST program at ORNL assumed responsibility for making NOZ-FLAW operational on the Oak Ridge computers. First, an IBMcompatible source program was developed from Dr. Kathiresan's CDC version, followed by extensive modifications and additions to the Auro mrdule to activate the automatic mesh generator option. Included in this effort were some 1 imited graphics developments for visual display of the generated finite element models. The completed Oak Ridge version of NOZ-FLAW was then used to analyze several nozzle corner flaws for comparison with other relevant experimental and numerical results, as described in Section 3 of this report.

Program NOZ-FLAW has the following unique features: (1) the capability to model user-defined flaw shapes as well as the mathematical shapes which have been analyzed and reported in the literature; (2) the use of special crack tip elements along the crack fronc (see Figure 2) which have the proper square root and inverse square root variations in Aisplacements and stresses, respectively; (3) the direct calculation o: K-factors, as opposed to previously reported finite element t H 'iques which employ displacement-stress extrapclation schemes or the calculation of strain energy release rates to determine K-values. Other features of the program include automatic mesh generation for a nozzle corner flaw located in the longitudinal plane and the use of regular twenty-node isoparametric elements away from the crack tip.


Figure 2. Special crack tip elements alony crack front

## 2. THE NOZ-FLAW COMPUTER PROGRAM

### 2.1 Capabilities and Limitations

NOZ-FLAW is a linear elastic finite element program which is used for the calculation of mixed-mode stress irtinsity factors along user-defined crack flaws at pressure-vessel nozzle corners. The crack flaw is assumed to lie in the longitudinal plane (see Figure 1). Special crack tip elements (hybrid-displacement) are used along the crack front and the K-factors are computed directly for each of these special elements.

NOZ-FLAW requires as few as eight cards of input to automatically generate a finite element mesh and perform an analysis. However, the convenience of having very limited user input introduces the following restrictions and limitations in the current version of the program:
(1) The material is linearly elastic, i.e., the plastic zone near the crack tip is ignored;
(2) The crack flaw is positioned in the longitudinal plane; al3o, certain restrictions on flaw dimensions are discussed in Section 2.3;
(3) A mesh for one-eighth of the configuration is automatically generated and boundary conditions are imposed to model the symmetric configuration shown in Figure 3. Thus, when one uses the present version of NOZ-FLAW to analyze a single nozzle with a single flaw, one assumes that the effects of a second nozzle underneath the vessel as well as the three additional flaws remote from the flaw of interest can be ignored. It is recommended that the present program be used only for relatively small nozzle-to-cylinder diameter ratios.
(4) The loading is due to internal pressure oniy, with or without crack face pressure;
(5) The nozzle-cylinder junction has ASME code 'standard' reinforcement only;
(6) The junction consists of a single material;
(7) The K-values are constant over an element; therefore, several crack tip elements must be used along tine crack front.


Figure 3. Nozzle comer flaw configuration with threefold symmetry

In addition, the strategy employed in the mesh generator requires that the user define an appropriate mesh in the longitudinal plane which is rotated and distorted to a compatible shape at various intervals around the nozzle. Hence, the mesh refinement at the transverse $(y-z)$ plane is much finer than usually required for an analysis. The mesh generator employs twenty-node brick elements for both regular and singular elements (except at the top of the reinforcement, where prisms are used), producing a model that typically consists of several thousand equations. Substantial computer resources are required by NOZ-FLAW to analyze such a problem, as described in Appendix B.

There are no inherent reasons why restrictions (2) through above could not be relaxed in future versions of the program, as they merely relate to geometry or boundary condition changes. For example, locating the flaw in the transverse plane or other planes would be relatively straightforward since the necessary mesh refinement already 3xists in these planes. Only the boundary conditions would need to be modified. With some additional effort, other mechanical ir even thermal loadings could be considered. Relaxing certain of the above resirictions, however, would certainly increase both the complexity and cost of the analysis.

Printed output from NOZ-FLAW consists of an echo of the input data, element connectivities, nodal global coordinates, imposed boundary conditions, displacements, stresses, and strains throughout the structure and K-values for each of the special crack $t: \sim$ elements along the crack flaw front.

### 2.2 The Hybrid-Displacement Finite Element Procedure

The special crack tip elements used in NOZ-FLAW were developed using a hybrid-displacement finite element procedure. This procedure has been developed and extensively applied to three-dimensional linear elactic fracture problems by Atluri, Kathiresan, et al. (References $20,21,23-25)$, and the details of the procedure will not be repeated here. Briefly, the hybrid-displacement finite element method is based on the stationary conditior of a modified total potential energy principle. The arbitrary element interior displacements, interelement boundary displacements, and element boundary tractions (Lagrange multipliers) are the three field variables. Threedimensional asymptotic silutions for displacements and stresses are embedded in. the special crack tip elements. Compatibility between the special crack tip elements and the regular isoparametric elements is enforced through the variational principle, assuring the convergence of the finite element procedure.

Application of the stationary condition yields a set of algebraic equations governiny the global nodal displacements $\underline{u}$, and the mode $r$, II, and III stress intensity factors $\underline{k}$ at various points along the crack front:

$$
\begin{aligned}
& S_{1} \underline{u}+S_{2} \underline{K}=\underline{Q}_{1} \\
& S_{2} \underline{u}+S_{3} \underline{K}=\underline{Q}_{2}
\end{aligned}
$$

Here, $S_{1}, S_{2}, S_{3}$ are the corresponding global stiffness matrices, and $\underline{Q}_{1}, \underline{Q}_{0}$ are the corresponding global nodal forces. Thus, the stress intensity factors are calculated directly from the governing equations, along with the nodal displacements.

### 2.3 AUTOMatic Mesh Generation

The automatic mesh generation module AL"TO in NOZ-FLAW is designed to generate a three-dimensional finite element model of an isolated nozzle-cylinder connection containing a corner crack flaw, subject to the restrictions outlined below. Isoparametric twenty-node brick type and sixteen-node prism type elements are used throughout the model. As few as eight input cards are required by the program to completely define the finite element model, including the nodal point coordinates, element connectivities, and imposed boundary conditions. A complete description of the required card input is given in the user instructions, Appendix A.

The following assumptions are made in generating the threedimensional finite element model of the nozzle-cylinder junction with corner flaw.
(1) The nozzle-cylinder junction is fully reinforced as iilustrated in Figure 4 (also, Figure NB-3338.2-2 (a) of the ASME Boiler and Pressure Vessel Code).
(2) The nozzle is radially attached to the cylindrical vessel.
(3) The model has inner and outer surface transitions ( $r_{1}$ and $r_{2}$ of Figure 4) between the nozzle and vessel. These transitions are circular arcs arcs and connect tangentially with the cylindrical nozzle and cylindrical vessel.
(4) The part-through corner flaw is positioned in the $x-y$ plane (also identified as the longitudinal plane) of Figure 1.


Pigure 4. ASME code standard
reinforcement design
(5) The geometric paraneters of the nozzle corner flaw model, defined on cards D-F of the user instructions, satisfy the following inequality:

$$
(\mathrm{PNR}+\mathrm{CRA}+2 . * \text { SIZE })<0.95 * \text { PVR }
$$

(If the option EXPR is chosen, then CRA is replaced by $\mathrm{X}(1)$ of card F .)
(6) The nozzle-vessel configuration has three planes of symmetry as shown in Figure 3. This assumption: is discussed further in the next section.

In constructing the finite element model, AUTO divides the generation of the node p,snt coordinates into two distinct steps. The first step consists of defining the coordinates of nodes positioned in the $x-y$ or longitudinal plane of the model. This is accomplished in subroutine NCNSTR by positioning nodes for the special crack tip elements along arcs that parallel the mathematically defined or experimentally measured crack front (region $I$ of Figure 5). The location of the crack front and number of divisions in this region are controlled by input parameters on cards D-F. The definition of the longitudinal cross section is completed by a rectangular discretization of the cylindrical vessel (region II) and the nozzle reinforcement (region III).

In the second phase of the node point generation scheme, subroutine NCNSTl 'rotates' the nodes in the longitudinal plane about the nozzle and/or vessel axes, defining the nodal coordinates in appropriately positioned meridional planes. The details of this scheme, including the relevant equations, are analogous to those described in Chapter 2 of keference 26, and will not be given here. The number of meridional planes is controlled by the parameter $N Z$ on Card E. The node point generation process terminates with the specification of nodal coordinates on the transverse plane ( $y-z$ plane, Figure 1).

With generation of the node point coordinates thus completed, program AUTO calls s broutine ELEMNT to define element types and nodal connectivities. In ELEMNT, the element types (brick, prism, or crack tip) are identified and numbered in sequence from the longitudinal to the transverse plane. Figures 6 through 8 illustrate the element numbering system generated by NOZ-FLAW for an Intermediate Test Vessel (ITV) model with a quarter-circular nozzle corner flaw. The nodal connectivity and face numbering scheme for the twenty-node isoparametric element are shown in Figure 9. The orientation of the

[^0]

Figure 5. Three regions for Aulo mesh generation


Figure 6. Finite element discretization for longitudinal plane of IIV model with a quarter-circular flaw $(\mathrm{a} / \mathrm{b}=0.41, \mathrm{a}=9.5 \mathrm{~cm})$


Figure 7. Finite element discretization for transverse plane of IIV model with a quarter-circular flaw $(a / b=0.41, a=9.5 \mathrm{~cm})$
ORNL. WWG 80-16641


FACE 5

Figure 9. Node and face numbering key for twenty-node isoparameteric brick element
connectivity is dependent upon the location of the element within the model. As shown in Figure 10, the connectivity scheme within the region bounded by the crack tip zone and the nozzle-vessel inner surface is rotated about the $y$-axis from the longitudinal to the transverse plane. Elements outside this region experience an additional rotation in the nozzle meridional plane, shown in Figure $-1$.

Program AUTO automatically specifies the appropriate displacement and traction boundary conditions for the symmetric nozzle-vessel configuration shown in Figure 3. In subroutine DSPLBC, nodes in a plane $3^{\text {of }}$ symmetry are constrainec in the direction normal to that plane, except for those nodes in the $x-y$ plane that fall within the crackface. Subroutine TRCBC computes the statically-equivalent node point forces for element faces exposed to internal pressure or end-cap blow-off loads. End caps are simulated by applying equivalent nodal forces to the nozzle and vessel end sections, as shown in Figure 12. Optional fixed-end boundary conditions for the nozzle and vessel are also imposed in this routine.

The instructions generated by program $\mathrm{AUTO}_{4}$ defining the finite element model are written on a system disk unit ${ }^{4}$ to be read later by the solution modules of NOZ-FLAW. In addition, the AUTO-generated instructions are echoed as part of the standard program output to permit the user to verify the finite element model.

The crack tip zone is that region of the model generated by revolving the four element layers surrc: inding the crack front about the $y$ axis from the longitudinal to the transverse plane (see Figure 11).
${ }^{3}$ In the output of program AUTO, fixed-displacement boundary conditions are displayed to the user by listing the constrained element faces. The designation "SLOPE $=0$ " (see microfiche output for example problem, Appendix C) for an element face indicates that each node of the face is constrained in the direction normal to that face.
${ }^{4}$ The instructions are written on unit NTAPE $2=12$.


Figure 10. Connectivity orientation for elements in nozzle comer region bounded by the crack tip zone ar.d inner surface


Figure 11. Connectivity orientation for elements
in and beyond the crack tip zone


## 3. NUMERICAL APPLICATIONS

NOZ-FLAW was used to analyze the intarmediate test vessel (ITV) configuration shown in Figure 13. A quarter-circular flaw (MATH) of तepth $a=9.5 \mathrm{~cm}$ and a similar natural flaw (EXPR) obtained in a photoelastic test [18] were analyzed under internal pressure loading. A crackface pressure equal to the internal pressure ( 100 MPa ) was applied simultaneously. For comparison purposes, the quarter-circular fiaw was also analyzed under internal pressure loading without crackface pressure. Figures 6 and 7 show longitudinal and transverse cross sectional views of the finite element mesh generated by NOZ-FLAW for the quarter-circular flaw model. Top and side views of the outside surface of the mesh are also given in Figures 14 and 15. A total of 324 elements and 1791 nodes was generated for this model.

The results of the anclyses are shown in Figure 16 , where normalized $K_{T}$ values are given at various points along the flaw front measured from the vessel free surface. The NOZ-FLAW values were obtained by averaging K-values from corresponding crack tip elements on each side of the crack. in addition, results are presented for the quarter-circular flaw using the BIGIF [27] computer program. BIGIF uses an influence function approach for the calculation of K-values and requires a prior stress analysis of the uncracked structure. This stress analysis was obtained using the CORTES-EP [28] finite element program. Each of the three NOZ-FLAW analyses, as well as the BIGIF analysis, gave ${ }^{\prime}$ distributions with relative maximums near the free surfaces and a relative minimum near the 45 position. The photoelastic results, however, show an opposite trend. It should be pointed out that these tests were conducted on small scale epoxy models which actually had the back free surface configuration indicated by the dotted boundary in Figure 13. Also, the inner nozzle corner fillet radius of the photoelastic models was slightly smaller than that modeled by NOZFLAW. One can also observe from Figure 16 that the inclusion of crackface pressure significantly elevates the NOZ-FLAW calculated K-values.

Each of the NOZ-FLAW analyses required 1200 K of memory and approximately 28 minutes of CPU time on the UCC-ND IBM 360/19!. The input for each, of the analyses shown is listed in Appendix C. A complete output from NOZ-FLAW for the quarter-circular flaw with crackface pressure is given on microfiche and attached to the back cover (see Appendix C).


Figure 13. Geanetry and dimensions of an ITV configuration
ORNL-DWG 80-16649

Figure 14. Top view (normal to $x-z$ plane) of outside surface


Figure 15. Side view (normal to $x-y$ plane) of outside surface of finite elenent mesh generated by NOZ-FLAW for ITV configuration

```
~-NOZ-FLAW, CRACKFFACE PRESSURE, MATH ORNL-DWG 80-16657
— NOZ-FLAW, CRACKFACE PRESSURE, EXPR
——NOZ-FLAW, NO CRACKFACE PRESSURE, MATH
---- BIGIF (REF. 27)
--*-- PHOTOELASTIC DATA (REF. 18)
```



ANGLE OF ROTATION FROM POINT OF FLAW INTERSECTION WITH VESSEL WALL (deg)

Figure 16. Variation of $K$ along a quarter-circular flaw and experimentally measured flaw (Ref. 18) in an IIV configuration $(\mathrm{a} / \mathrm{b}=0.41, \mathrm{a}=9.5 \mathrm{~cm})$

## 4. CONCLUSIONS

NOZ-FLAW is a linear elastic finite element computer program which calculates nozzle corner flaw stress intensity factors. Unique features include the use of special crack tip elemnts (hybrid-displacement), direct calculation of K-values, and automatic mesh generation incorporating userdefined crack flaws. As few as eight cards of input are required to automatically generate a finite element model and to execute the rrogram. The convenience of limited input, however, introduces certain limitations or restristions. The flaw must be positioned in the longitudinal plane of a standard reinforced pressure vessel nozzle configuration. Only internal pressure loading, with or without crackface pressure, may be considered. A finite element mesh is generated and appropriate boundary conditions are imposed for one-eighth of a configuration that possesses threefold symmetry. Thus, use of the present version of NOZ-FLAW to analyze a single nozzle with a single flaw ignores the effects of a second nozzle underneath the vessel as well as the additional flaws remote from the flaw of interest. It is therefore recommended that NOZ-FLAW be used oniy for relatively small-diameter nozzles attached to relatively large-diameter vessels. Also, the size of the special crack tip elements should be no more than me-tenth of the flaw depth.

Minor modifications of the NOZ-FLAW mesh generator will permit the analysis of a nozzle corner flaw configuration with two planes of symmetry, i.e., the second nozzle underneath the vessel could be removed. Other loadings could be considered by modifying the boundary condition routines. Work is currently under way to develop a more general program for the analysis of user-defined crack flaws in flat plates, cylinders, and nozzle corners. Other future developments include the addition of thermal loading and graphics plotting routines to the expanded version of the program.

## ACKNOWLEDGMENTS

The NOZ-FLAW computer program was initiated under the direction of Professor S. N. Atluri, School of Engineering Science and Mechanics, Georgia Institute of Technology. The work was sponsored by the Heavy Section Steel Technology Program (HSST) under UCC-ND Subcontract 7565 between UCC-ND and Georgia Institute of Technology.

The authors gratefully acknowledge the assistance of W. G. Johnson and J. B. Drake, UCC-ND Computer Sciences Division, in setting up the program to operate on the UCC-ND computer facilities. Special thanks are due R. H. Bryan, ORNL, who provided much encouragement in addition to his many rechnical contributions in this work.

Finally, the authors wish to express their gratitude to L. W. Walker for typing the drafts and preparation of the manuscript.

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APPENDICES

## APPENDIX A

## NOZ-FLAW INSTRUCTIONS

NOZ-FLAW requires as few as eight input cards to generate a finite element mesh and to execute in analysis. The program permits free format input for all but the first card, where AUTO must be specified in columns 1-4. Variable values are separated by commas and blanks are ignored, i.e., NO ZZLE will be read as NOZZLE. Cards $C-H$ must end with a $\$$ and card is must begin with a $\$$. A / is used to continue data to the next line, for example:

$$
\begin{array}{ll}
5,5,3 / & \text { Line } 1 \\
2,5 & \text { Line } 2
\end{array}
$$

is the same as

$$
5,5,3,2,5 \quad \text { Line } 1 .
$$

If a variable is zero or if the user chooses not to specify a variable, two consecutive commas (, ) may be used. For example:

$$
5,5,2,5
$$

is the same as

$$
5,5,0,2,5
$$

A coma should not be used before a / unless the last variable value is zero. For example,

$$
\begin{aligned}
& 5,5,3,1 \\
& 2,5
\end{aligned}
$$

is not the same as

$$
5,5,3,2,5 .
$$

The program would interpret this as

$$
5,5,3,0,2,5 .
$$

Finally, integer variables should receive integer values. Real variables require decimal input. For example, input for Card E with parameters NX1, NX2, NX3, NX4, NY1, NY2, NZ, SIZE, GRADX might be $2,2,2,1,1,2,4$, $0.005,1.5 \$$.

INPUT DATA

CARD A. Mesh generation code - specify AUTO in columns 1-4.
CARD B. Title - A \$ must appear in column 1. Any symbol other than a / may appear in columns 2-80.

CARD C. Parameters PBTPE, E, PO, CRACK, PMODEL. End this card with a \$.

PBTPE - Specify NOZZLE
E - Young's modulus for material
PO - Poisson's ratio for material
CRACK - Specify NDCORNER*
PMODEL - Specify 0.125*
*These values instruct NOZ-FLAW to generate a finite element mesh for the threefold symmetric configuration shown in Figure 3. Other mesh generation options are planned.

CARD D. Parameters CRPRF, PVR, PVT, PNR, PNT, PVL, PNL, R1, R2, PNL1, PNL2, PNT2, NCRS. End this card with a \$. See Figure 17 for a definition of these variables.

CRPRF - Specify MATH or EXPR; MATH for quarter-circular or quarter-elliptical flaws, EXPR for user-defined crack flais.

PVR - Pressure vessel inner radius
PVT - Pressure vessel thickness
PNR - Nozzle inner radius
PNT - Nozzle thickness above reinforcement
PVL - Pressure vessel length
PNL - Nozzle length
R1 - Inner fillet radius
R2 - Outer fillet radius
PNL1 - Nozzle length above reinforcement
PNL2 - Nozzle length to reinforcement
PNT2 - Nozzle thickness at reinforcement
NCRS - Number of mesh divisions along crack front
NOTE: NCRS $\geq$ NY1 + NY2 +2 (see CARD E)


Figure 17. Dimensional parameters for nozzle corner flaw configuration

CARD E. Mesh division parameters NX1, NX2, NX3, NX4, N11, NY2, NZ, SIZE, GRADX. End the card with a $\$$. See Figure 18 for a definition of these variables.

$$
\text { NOTE: } \quad \text { NX3 } \geq \text { NCRS }- \text { NY1 }- \text { NY2 }-2
$$

CARD F. Crack definition. End this card with a \$.
For CRPRF $=$ MATH on CARD D, input CRA, CRB .
See Figure 19 for a definition of these variables.
For CRPRF $=$ EXPR, input $X(I), I=1,2{ }^{*}$ NCRS $+1,2$
Y(I), I-1, 2*NCRS+1, 2
See Figure 20 for a definition of these variables.
NOTE 1: $X_{i}$ and $Y_{i}$ should be input using the local coordinate system shown in Figure 20.

NOTE 2. (PNR + CRA + 2 * SIZE) < 0.95 * PVR (for MATH)
or
(PNR $+\mathrm{X}(1)+2 *$ SIZE) $<0.95$ * PVR (for EXPR)
CARD G. Pressure loading and boundary conditions. End this card with a $\$$.

Possible inputs re:
CYPRESS, P
CRPRESS, P
ENDCAP, P
ENDDSPL
CYPRESS, P - Application of uniform internal pressure of magnitude $P$ in both cylinder and nozzle.

CPPRESS, $P$ - Application of uniform pressure of magnitude $P$ on the crack surface.

ENDCAP,P - Simulates end caps by applying appropriate force loadings at nozzle and cylinder end nodes. P is the internal pressure loading. See Figure 12.

ENJDSPL - Surpresses axial displacements at nozzle and cylinder ends. May not be specified simultaneously with ENDCAP,P.


Figure 18. Mesh generatial parameters for nozzle comer flaw configuration


Figure 19. Crack definition parameters


Figure 20. Local coordinate definition of crack front for CRPRF $=$ EXPR

CARD H. Termination and printout option. End this card with a $\$$.
End of input is signaled by specifying ENDBC. Stress intensity factors as well as stresses, strains, and displacements for the entire structure are printed. If only the stress intensity factors are desired, then specify SIF following ENDBC.

Example:
ENDBC\$ prints stress intensity factors as well as stresses, strains, displacements for entire structure.

ENDBC, SIF\$ prints only the stress intensity factors.

## APPPENDIX B

## PROGRAM RESOURCE REQUIREMENT AND R.VAILABILITY

Program NOZ-FLAW consists of approximately 17,000 cards in 160 subroutines (FORTRAN IV) and is available in both IBM and CDC versions. When used with the job control language given in this section, the current IBM version requires approxinately 1200 K bytes of core memory for execution on the Oak Ridge IBM 360/195 computer. Currently, the program is dinensioned for a finite element model not exceeding 500 elements and/or 6000 nodal points. A larger model can be accommodated by modifying four statements in subroutine SETUP to reflect an increase in the maximum number of eiements and nodes. In SETUP, the dimension of each array listed below must be greater than or equal to the corresponding expression in parentheses:

```
IJK (22* [maximum number of elements])
    \(X\) (maximum number of nodes)
    \(Y\) (maximum number of nodes)
    \(z\) (maximum number of nodes)
```

Also, the integer values of MAX, NDIM must be set to the following values:

$$
\begin{aligned}
\text { MAX } & =\text { maximum number of elements } \\
\text { NDIM } & =\text { maximum number of nodes. }
\end{aligned}
$$

The job con rol language (JCL) necessary to xecute program NOZ-FLAW on the IBM 360/195 computer at Cot Ridge is listed at the end of this section.

Included in the listing is the program overlay structure and the required system I/O disk units. The JCL is organized to link in several double-precision bit manipulation routines written in assembler language. These routines are employed in subroutine FFLDSB to translate the free format input data into the appropriate alphanumeric data for the initialization of variables. Because NOZ-FLAW is written in double precision, the standaru single-precision IBM library versions of these routines are not applicable. In mid-FY 81, both the IBM (including assembler language routines) and CDC versions of the NOZ-FLAW source program will be available to the public through the National Energy Software Center at Argonne, Illinois.

[^1]```
//BXBCYLNF JOB (14486),'BR BASS BLK1007' K25 RM2240 X48718
//*CLASS CPU95=3M,L=75, TO=8,C=0,REGION=1200K
/*
//STEPL EXEC FORTHCLG,PARM.FORT='MAP,XREF',
// PARM.LKED='OVLY,MAP,LIST',CLSIZE=498K,
// PARM.GO='CK=-7, EU=-1,DUMP=I',GOSIZE=1200K,GOTIME =2
//FORT.SYSLIN DD SPACE=(TRK, (300,50),RLSE)
//FORT.SYSIN DD *
=NOZ-FLAW SOURCE PRUGRAM
/*
//LKED.ASMHEX DD DSN=A.H.TEA14938.ASMHEX,DISP=SHR,
// UNIT=3330-1,VOL=SER=CSDCAD
/*
//LKED.SYSIN DD *
    INCLUDE ASMHEX
    INSERT MAIN
    OVERLAY ONE
    INSERT SETUP,MATRED,DIRCOS,MATROT,MESH3D,ELDATA,ADJUST
    OVERLAY ONE
    INSERT
FORMK3,SHAPEB, SHAPEP,SHAPET,SSHAPE,BIGSTF,MFUNC, BNDARY, PRLOAD
    INSERT
BIGPR,SLOPES,VECNIC, CRACK3,ROTATE, CALKMS,STIFF,MATCH,VOLUME
    INSERT AREA, QUDFR,F,FO, INVERT, CALTMP
    UVERLAY ONE
    INSERT
PUZGP 3,NDF, PUZSET, PUZSOL,PREFKN,FRONT,FRONTI, TAPS,GAPS, EXPAND
    INSERT
NUM,FRONTS, ZERO,RO'WS,SEMBL1,SEMBL2,REDUCE,SETDIS,SETCOR
    INSERT
SCRMBL, SWITCH,FORMNO,BACKSU,BPASS,PRNTO,PRNT1,PRNT2,PRNTA
    INSERT PRNTC,PRNTX
    OVERLAY ONE
    INSERT
POST, INITLP,STPTS,NUMFA,STRSPR,BIGSTR,CROSS,XFORM,PSTRES,K123
    INSERT SUMARY,BOX,FACEP,OUTLIN, ELMP,CONTR, DRAWBL,ROT3D,SIF
    OVERLAY ONE
    INSERT
RZONE 3,REZONE,REFINS,FINBC,STRSFG,BSHPF,NORMAL,BSHPL,NMESHF
    INSERT MOVEP,MESH3E
    OVERLAY ONE
    INSERT
AUTO,SETZER,ERROR,CHECK,DEFLT,SETUP2,AMXMN,POINT,CSEGCO,CONST
R
    INSERT
JILOC,TANGEN, CTHETA, DATAIN,BASE, ELEMNT, AXELMS,DSPLBC,TRCBC
    INSERT NCNSTR,NCNST1, IAVER,JAVER,KAVER, COMGAM
/*
//GO.FT06F001 DD SYSOUT=A
//FT11F001 DD UNIT=SYSDA,SPACE=(TRK, (300,100)),
// DCB=(RECFM=VBS,BLKSIZE=13030, BUFNO=1,OPTCD=C),
// DSN=UN1T11,DISP=(,PASS)
//FT12F\overline{001}}\textrm{DD}\mathrm{ UNIT=SYSDA,SPACE=(TRK, (300,100)),
// DCB=(RECFM=VBS,BLKSIZE=13030, BUFNO=1,OPTCD=C),
```

```
// DSN=UNIT12,DISP= (,PASS)
//FT13F\overline{001 DD UNIT=SYSDA,SPACE=(TRK, (300,100)),}
// DCB=(RECFM=VBS,BLKSIZE=13030, BUFNO=1,OPTCD=C),
// DSN=UNIT13,DISP=(,PASS)
//FT14F\overline{001} DD UNIT=SYSDA,SPACE=(TRK, (300,100)),
// DCB=(RECFM=VBS,BLKSI2E=13030, BUFNO=1,OPTCD=C),
// DSN=UNIT14,DISP=(,PASS)
//FT15F\overline{001} DD UNIT=SYSDA,SPACE=(TRK, (300,100)),
// DCB=(RECFM=FB, LRECL=80, BLKSIZE=3200,OPTCD=C),
// DSN=UNIT15,DISP=(,PASS)
//F. 16F\overline{001 DD UNIT=SYSDA,SPACE=(TRK, (1500,100)),}
// DCB=(RECFM=VBS,BLKSIZE=13030, BUFNO=1,OPTCD=C),
// DSN=UNIT16,DISP=(,PASS)
//FT17F\overline{001 DD UNIT=SYSDA,SPACE=(TRK, (300,100)),}
// DCB=(RECFM=VBS,BLKSIZE=13030, BUFNO=1,OPTCD=C),
// DSN=UNIT17
//FT18F\overline{001} DD UNIT=SYSDA,SPACE=(TRK, (300,100)),
// DCB=(RECFM=VBS,BLKSIZE=13030, BUFNO=1,OPTCD=C).
// DSN=UNIT18,DISP=(,PASS)
//FT19F\overline{001}}\mathrm{ DD UNIT=SYSDA,SPACE=(TRK, (300,100)),
// DCB=(RECFM=VBS,}\textrm{BLKSIZE=13030, BUFNO=1,OPTCD=C),
// DSN=UNIT19,DISP=(,PASS)
//FT20F\overline{001} DD UNIT=SYSDA,SPACE=(TRK, (300,100)),
// DCB = (RECFM=VBS,BLKSIZE=13030, BUFNO=1,OPTCD=C),
// DSN=UNIT20,DISP=(,PASS)
//FT21F001 DD UNIT=SYSDA,SPACE=(TRK, (300,100)),
// DCB=(RECFM=VBS,BLKSIZE=13030, BUFNO=1,OPTCD=C),
// DSN=UNIT21,DISP= (,PASS)
//FT22F\overline{001}DD UNIT=SYSDA,SPACE=(TRK, (300,100)),
// DCB=(RECFM=VBS,BLKSIZE=13030, BUFNO=1,OPTCD=C),
// DSN=UNIT22,DISP=(,PASS)
//FT23F\overline{001 DD UNIT=SYSDA,SPACE=(TRK, (300,10C)),}
// DC3=(RECFM=VBS,BLKSIZ.E=13030, BUFNO=1,OPTCD=C),
// DSN=UNIT23,DISP= (,PASS)
//FT05F\overline{001 DD *}
=INPUT DATA DECK
/*
//
ENDINPUT
```


## APPENDIX C

Input data that were provided for the three different NOZ-FLAW analyses of an ITV model reported in Chapter 3 (see Figures 13, 16) are given below. A suarter-circular flaw (MATH, $a / b=0.41, a=9.5 \mathrm{~cm}$ ) was analyzed under internal pressure loading ( 100 MP a) both with and without crackface pressure ( 100 MPa ). A similar experimi htally measured flaw (EXPR) from Reference 18 was also analyzed under internal pressure loading ( 100 MPa ) with applied crackface pressure ( 100 MPa ).

A complete printout for the quarter-circular flaw model with applied crackface pressure is provided on microfiche and actached to the back cover. NOZ-FLAW prints an echo of the input data, nodal global coordinates and element connectives, imposed boundary conditions, stresses, strains, and displacements throughout the structure, and the mode I, II, and III siress intensity factors for each of the special crack tip elements along the flaw front.

## IMAGE EVALUATION TEST TARGET (MT-3)



IMAGE EVALUATION TEST TARGET (Mĩ-3)

-nput data for ITV model with a quarter-circular flaw (MATH) under internal pressure loading and crackface pressure.

```
AUTO
$ITV NOZZLE CORNER FLAW
NOZZLE, 3.E7, . 3, NDCORNER, .125$
MATH, .343,.152,.114,.102,1.,1.,.038,.076,.670,.721,.152,6$
2,2,2,1,2,1,4,0.005,1.5$
0.11,0.11$
CRPRESS, 100.$
CYPRESS, 100.$
ENDCAP, 100.$
ENDBC$
```

Input data for ITV model with a quarter-circular flaw (MATH) under internal pressure loading without crackface pressure.

```
AUTO
$ITV NOZZLE CORNER FLAW
NOZZLE, 3.E7, .3, NDCORNER, .125$
MATH,.343,.152,.114,.102,1.,1.,.038,.076,.670,.721,.152,6$
2,2,2,1,2,1,4,0.005,1.5$
0.11,0.11$
CYPRESS,100.$
ENDCAP,100.$
ENDBC$
```

Input data for TTV model with an experimentally measured flaw (EXPR) under internal pressure loading and crackface pressure.

AUTO
\$ITV NOZZLE CORNER FLAW
NOZZLE, 3.E7, .3,NDCORNER, . $125 \$$
EXPR,.343,.152,.114,.102,1.,1.,.038,.076,.670,.721,.152,6\$
$2,2,2,1,2,1,4,0.0,1.5 \$$
$.118, .119, .108, .076, .045, .012,0, .0 ., .012, .045, .076, .108, .117, .118 \$$
CRPRESS, $100 . \$$
CYPRESS, $100 . \$$
ENDCAP, $100 . \$$
ENDBC $\$$

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[^0]:    ${ }^{1}$ Th is inequality is required by the algorithm used in the node point coordinate generating routine NCNSTI in the AUTO inodule.

[^1]:    1 The CDC source utilizes standard system library routines.

