# SOUTHERN CALIFORNIA EDISON COMPANY PWR REACTOR PHYSICS METHODOLOGY USING <br> CASMO-3/SIMULATE-3 

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## SOUTHERN CALIFORNIA EDISON COMPANY

PHR REACTOR PHYSICS METHODOLOGY
USING
CASMO-3/SIMULATE-3

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## ABSTRACT

This report documents the validation and level of accuracy of the reactor core physics methodology used by Southern California Edison Company to perform steady-state analyses for Pressurized Water Reactors (PWR). The methodology is based on the CASMO-3/SIMULATE-3 computer program package. This methodology has been validated by an in-house benchmarking effort of CASMO-3/SIMULATE-3 predictions with measured data from power reactors and critical experiments. Based on the results from this benchmarking effort, a set of 95/95 tolerance limits has been calculated. Southern California Edison Company intends to use this methodology to perform PWR calculations including reload design, input to safety analyses, startup predictions, core physics databooks, and, reactor protection system and monitoring system setpoint updates.
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### 1.0 INTRODUCTION

This report describes Southern California Edison (SCE) Company's reactor core physics methodology for Pressurized Water Reactor (PWR) analyses using the CASMO-3/SIMULATE-3 computer program package (References 1 through 6). Studsvik AB and Studsvik of America developed the CASMO-3/SIMULATE-3 computer program package. This package is widely accepted within the nuclear industry.

Yankee Atomic Electric Company (YAEC) provided the theoretical basis and validation of this computer program package to the NRC (References 7 and 8). In these reports YAEC provided detailed descriptions of the computer programs and a general methodology for performing reactor physics analyses.

The objective of this report is to demonstrate SCE's ability to use the CASMO-3/SIMULATE-3 computer program package. The report also documents the uncertainty factors determined through the benchmarking of key PWR physics parameters, presented in Table 1.1, with plant measurements.

### 1.1 OVERVIEW

The data demonstrating the applicability of SCE's methodology for PWR core physics analyses are documented in Sections 2 through 7 of this report.

Section 2, Description of Methodology, presents a brief description of the CASMO-3/SIMULATE-3 computer program package.

Section 3, Description of Reactors Used in the Benchmarking, describes the PWRs used in the benchmarks.

Section 4, Benchmark Comparisons, details the benchmarking of the key PWR core physics parameters listed in Table 1.1. For each parameter, the calculated data were compared with plant measurements, the sample mean and standard deviation were quantified, and a 95/95 tolerance limit (bias $\pm$ reliability factor) determined.

Section 5, Pin Peaking Factor Uncertainties, presents the derivation of the pin peaking factor 95/95 tolerance limits.

Section 6, Conclusions, presents the conclusions of this report and the range of applications for which SCE will use this
methodology.
Section 7, References, presents documents referenced in this report.

### 1.2 SUMMARY

Table 1.2 summarizes the $95 / 95$ tolerance limits calculated in Sections 4 and 5. The tolerance limits are such that, when applied to the CASMO-3/SIMULATE-3 results, there is a 95 percent probability, with a 95 percent confidence that the calculated values will conservatively bound the "true" values.

SCE concludes that this methodology is acceptable for the performance of all steady-state PWR core physics analyses including:

- Reload design,
- Safety analyses input,
- Startup predictions,
- Core physics databooks, and
- Reactor protection and monitoring system updates.


## List of Key PWR Physics Parameters

- Core Reactivity
- Zero Power
- Full Power
- Inverse Boron Worth
- Power Coefficient
- Isothermal Temperature Coefficient
- Control Rod Worth
- Axial Offset
- Assembly Power Peaking
$-\quad F_{Q}^{s}$
$-\quad \mathrm{F}_{\mathrm{XY}}^{\mathrm{s}}$
$-\quad F_{R}^{S}, F_{\Delta B}^{S}$
- Pin Peaking

$$
\begin{array}{ll}
- & F_{Q} \\
- & F_{X Y} \\
- & F_{R}, F_{\Delta B}
\end{array}
$$

## List of $95 / 95$ Tolerance Limits (Bias $\pm$ Reliability Factors)

| Parameter | Bias | Reliability Factor | Units* |
| :---: | :---: | :---: | :---: |
| Core Reactivity ( $\% \Delta k / k$ ) |  |  |  |
| Zero Power | -0.08 | 0.26 | Absolute |
| Full Power | 0.01 | 0.35 | Absolute |
| Critical Boron (PPM) |  |  |  |
| Zero Power | -7 | 26 | Absolute |
| Full Power | 2 | 34 | Absolute |
| Inverse Boron Worth (PPM/\% $\Delta K / K$ ) | 0.0 | 10\% | Relative |
| Power Coefficient $\left(10^{-4} \Delta K / K / \% P\right)$ | 0.0 | 0.20 | Absolute |
| Isothermal Temperature |  |  |  |
| Control Rod Worth ( $\% \Delta k / k$ ) | 1.2\% | 8. $2 \%$ | Relative |
| Local Pin Power | 0.0 | 2\% | Relative |
| Axial Offset | -0.003 | 0.0 .14 | Absolute |
| Assembly Peaking $\mathrm{F}_{8}^{\text {s }}$ | 0.0 | 4.17\% | Relative |
| $\mathrm{F}_{\mathrm{x}}^{\mathbf{s}} \mathrm{Y}$ | 0.0 | 4.80\% | Relative |
| $F_{R}^{\hat{S}}$ | 0.0 | 3.34\% | Relative |
| Pin Peaking $\quad F_{Q}$ | 0.0 | 4.62\% | Relative |
| $\mathrm{F}_{\mathrm{XY}}$ | 0.0 | 5.20\% | Relative |
| $\mathrm{F}_{\mathrm{R}}, \mathrm{F}_{\Delta \mathrm{B}}$ | 0.0 | 3.89\% | Relative |

*For those parameters with differences expressed in relative units:

$$
\text { Predicted }=\text { Calculated } *(1-\text { Bias } \pm \text { Reliability Factor })
$$

For parameters with differences in absolute units, the following equation applies:

$$
\text { Predicted }=\text { Calculated }- \text { Bias } \pm \text { Reliability Factor }
$$

## DESCRIPTION OF METHODOLOGY

### 2.0 INTRODUCTION

This section provides a brief description of the CASMO-3/SIMULATE-3 methodology. Yankee Atomic Electric Company (YAEC) has already presented the theoretical bases and validation of CASMO-3 and SIMULATE-3 before the Nuclear Regulatory Commission (NRC). The computer program package has received NRC approval for use in core physics calculations (References 21 and 22).

### 2.1 COMPUTER PROGRAM DESCRIPTIONS

The CASMO-3/SIMULATE-3 computer program package (References 1 through 6) was developed by STUDSVIK AB, Nykoping, sweden and their American subsidiary STUDSVIK OF AMERICA, Newton, Massachusetts. The computer program package consists of five computer programs:

| • | CASMO-3, |
| :--- | :--- |
| • | MASLIB, |
| - | MICBURN-3, |
| •. |  |
| - SIMUEROD-3, and, |  |
|  |  |

In addition, the Electric Power Research Institute's (EPRI) ESCORE computer program (Reference 9) was incorporated into the program sequence. The computer program sequence flow chart is shown in Figure 2.1 .

These computer programs are briefly described below. Detailed information--theory, user manual, etc.--can be found in the referenced documents.

## ESCORE

ESCORE (Reference 9) is a computer program for predicting bestestimate, steady-state fuel performance data for light water reactor fuel rods. This computer program has received NRC approval for use in calculating fuel rod temperatures for input to design and safety analyses (Reference 23). SCE uses this computer program to calculate the fuel temperature of the average rod as a function of burnup. Output from this computer program provides the burnup independent fuel pin temperature for use in

CASMO-3, and a burnup dependent fuel pin temperature for the SIMULATE-3 model.

## CASMO-3

CASMO-3 is a multigroup, two-dimensional transport theory computer program (Reference 1). This computer program models cylindrical fuel rods of varying composition in a square pitch array. CASMO-3 can model fuel rods, fuel rods with integral burnable absorber, burnable absorber rods, control rods, guide tubes, in-core instruments, and water gaps.

CASMO-3 generates all cross-section data for SIMULATE-3. SCE uses CASMO-3 in a single assembly format with reflective boundary conditions. A 40-energy group cross-section library is used.

## CASLIB

CASLIB (Reference 2) produces a binary neutron cross-section library for input to CASMO-3 from a card-image, formatted library. The card-image, formatted library, supplied with CASMO-3 from STUDSVIK, is based mainly on data from ENDF/B-IV with an update from ENDF/B-V and other sources. Both forty- and seventy-group cross-section data are available for nearly 100 materials.

## MICBURN-3

MICBURN-3. (Reference 3) calculates the microscopic burnup in a fuel rod containing an initially homogeneously distributed strong burnable absorber such as gadolinia. It generates effective cro'ss-sections as a function of the absorber number density to be used in CASMO-3.

## MOVEROD-3

MOVEROD-3 (Reference 4) is a file editing program that creates a new CASMO-3 restart file from existing files by selecting and rearranging data for specified fuel pins. The new restart file can then be used for continued CASMO-3 calculations on a reconstituted fuel assembly.

TABLES-3
TABLES-3 (Reference 5) is a data processing program that links CASMO-3 to SIMULATE-3. The program processes the following types of data from CASMO-3:
fission product data,

- in-core instrument response data,
- pin power reconstruction data, and
- kinetics data.

TABLES-3 reads the CASMO-3 card image files and produces a master binary cross-section library for SIMULATE-3.

## SIMULATE-3

SIMULATE-3 is a two- or three-dimensional (2-D or 3-D), two-group coarse mesh diffusion theory reactor simulator program (Reference 6). The program explicitly models the baffle/reflector region, eliminating the need to normalize to higher-order fine mesh calculations such as PDQ. Homogenized cross-sections and discontinuity factors are applied to the coarse mesh nodal model to solve the two-group diffusion equation using the QPANDA neutronics model. QPANDA employs fourth order polynomial representations of the intra-nodal flux distributions in both the fast and thermal groups.

The nodal thermal hydraulic properties are calculated based on the inlet temperature, RCS pressure, coolant mass flow rate, and the heat addition along the channels.

The pin-by-pin power distributions, on a $2-\mathrm{D}$ or 3-D basis, are constructed from the inter- and intra-assembly information from the coarse mesh solution and the pin-wise assembly power distribution from CASMO-3.

The SIMULATE-3 program performs a macroscopic depletion. Individual Uranium, Plutonium, and lumped fission product isotope concentrations are not computed. However, microscopic depletion of Iodine, Xenon, Promethium, and Samarium is included to model typical reactor transients.

### 2.2 MODEL DESCRIPTIONS

## CASMO-3 FUEL ASSEMBLY AND REFLECTOR MODELS

Each unique PWR fuel assembly type (defined by geometry, enrichment, and burnable poison pins) is separately modeled in CASMO-3 using octant symmetry. Enrichment zoning among fuel pins, burnable poison pins, and guide tubes are explicitly modeled. The water gap between assemblies in the reactor core is included in the CASMO-3 model. The spacer grids are also included. Design bases documents such as the updated Final Safety Analysis Report (FSAR), reload reports, and as-built
drawings provide the necessary data to develop the CASMO-3 assembly models.

Three depletion cases are needed to generate each fuel assembly type's average cross-section data. First, the fuel assembly is depleted at hot full power, reactor average conditions. Moderator temperature, fuel temperature, and soluble boron concentration are set to constant average values for the complete depletion. The average fuel temperature at hot full power conditions is calculated with EPRI's ESCORE computer program (Reference 9). Next, the fuel assembly is depleted at a low moderator temperature, a few degrees below hot zero power conditions. However, the fuel temperature and the soluble boron concentration are kept at the constant hot full power, reactor average values. Last, the fuel assembly is again depleted at constant hot full power, reactor average conditions, but with a constant soluble boron concentration higher than is usually seen in normal operation. Restart files are saved from all three depletions. Each fuel assembly type is depleted to greater than 50 GWD/T assembly average burnup using the CASMO-3 default depletion steps.

Branch cases are performed to calculate instantaneous effects. Instantaneous effects are individually calculated and added together later to recreate the proper fuel assembly cross sections. The branch cases are executed from the hot full power, reactor average conditions restart file at typically $0,5,10$, 20, 30, 40, and 50 GWD/T. Branch cases are run for off-normal moderator temperatures, fuel temperatures, soluble boron concentrations, and control rod insertions.

CASMO-3 also generates top, bottom, and radial reflector cross sections. The radial reflector consists of the stainless steel core baffle followed by about 15 centimeters (cm) of water. The top reflector extends from the top of the active fuel to the lower surface of the fuel assembly upper end fitting. The bottom reflector extends from the bottom of the active fuel to the lower surface of the core support plate. Reflector cross-sections are modeled as a function of soluble boron concentration and moderator temperature.

## TABLES-3 MODEL

The TABLES-3 program generates two-dimensional reactor and cycle specific cross-section tables for SIMULATE-3. Data from the following CASMO-3 card image files are combined into binary cross-section libraries for input to SIMULATE-3:

- HFP Reactor Average Depletion + Branches,
- Fuel Temperature Branches


## - Moderator Temperature Branches

- Soluble Boron Concentration Branches
- Control Rod Insertion Branches
- Low Moderator Temperature Depletion, - HFP High Soluble Boron Concentration Depletion,
- Bottom Reflector Data,
- Radial Reflector Data, and

Top Reflector Data.

## SIMULATE-3 MODEL

The SIMULATE-3 model divides the active fuel region into 20 axial and four radial nodes per assembly. A pseudo-assembly, consisting of reflector material, surrounds the core and is divided into one radial and 20 axial nodes. Axially, the fuel is divided into a single bottom reflector node, 20 nodes for the active fuel region, and a single top reflector node.

Additional model input data are the:

- Full core assembly serial number map,
- Quarter core fuel assembly type map,
- Fuel assembly axial zone definition, including reflectors,
- Asymmetric (radially) fuel assembly node definition,
- Control rod locations,
- Grouping of control rods into banks,
- Axial zone definitions for control rods, especially part length rods,

In-core instrumentation locations,

- Fuel temperature versus power level and burnup correlation (ESCORE program),
- Core MW-thermal output at $100 \%$ power,
- Core pressure, power density, and coolant mass flow rate at $100 \%$ power conditions,
- Coolant inlet temperature versus power level,
- Input Restart files, and
- Output Restart file.

After the cycle base model is set up, the user can specify the percent power level, rod bank positions (percent withdrawn), output and edit options, and the type of calculation: depletion, xenon transient, coefficient calculation (e.g., ITC, IBW, FTC; etc).

Figure 2.1
Program Sequence Flow Chart


Pin/Assembly Power Distributions Reactivity Coefficients Control Rod Worths
Boron Concentration, Cycle Length, Etc.

### 3.0 INTRODUCTION

This report compares the CASMO-3/SIMULATE-3 predictions of key physics parameters against measured plant data. Data from four different reactor plants were used. The measurements were obtained during plant startup and normal operation. The reactor plants are:

- San Onofre Nuclear Generating Station Unit 1,
- San Onofre Nuclear Generating Station Unit 2,
- San Onofre Nuclear Generating Station Unit 3, and
- Arkansas Nuclear One - Unit 2.

The following sections provide brief descriptions of these reactor cores. Detailed information can be found in References 10, 11, and 12.

### 3.1 SAN ONOFRE NUCLEAR GENERATING STATION UNIT 1 (SONGS 1)

SONGS 1 is a commercial nuclear power plant. The unit began commercial operation in 1968 and has completed 10 cycles of operation: The plant is a Westinghouse three-loop PWR. The reactor core produces 1347 megawatts-thermal at $100 \%$ rated power.

The reactor core consists of 157 fuel assemblies arranged as shown in Figure 3.1. Both conventional and low leakage fuel management patterns have been used. Each fuel assembly consists of a $14 \times 14$ array of 180 fuel rods and 16 control rod guide thimbles. The fuel assembly cross-section is shown in Figure 3.2. Core, fuel assembly, and control rod data are summarized in Table 3.1.

The fuel rods consist of slightly enriched (3.15 to 4.0 weight percent U-235) uranium dioxide $\left(\mathrm{UO}_{2}\right)$ pellets with stainless steel cladding. The control rod guide thimbles are also stainless steel. Seven Inconel-718 grids are located along the length of the assembly.

The in-core instrumentation system for power distribution measurement consists of two moveable fission chambers. These instruments can be inserted into 30 core locations. The detector's neutron flux signal is processed off-line with the Westinghouse INCORE3 program (Reference 13). The 30 instrumented
core locations are shown in Figure 3.3.
There are 45 full-length control rods, called rod cluster control assemblies (RCCA's). Each RCCA consists of 16 individual absorber rods fastened to a common hub. The RCCA's are not zoned. The single absorber material is Silver-Indium-Cadmium in stainless steel tubes. The RCCA's are moved in four symmetrically located banks. Banks \#2 and \#1 are called the Control Banks, and they are moved to control the reactor over the power range. The remaining RCCA's are called Shutdown Banks \#1 and \#2. Figure 3.1 shows the RCCA's locations.

The SONGS 1 reactor has two unique features which were modeled with CASMO-3/SIMULATE-3. The first unique feature modeled was the stainless steel fuel rod cladding. Most PWR cores use zircaloy cladding. The second unique feature was the use of mixed oxide $\left(\mathrm{PuO}_{2}-\mathrm{UO}_{2}\right)$ assemblies. In Cycles 2 and 3, four Edison Electric Institute (EEI) mixed oxide ( $\mathrm{PuO}_{2}-\mathrm{UO}_{2}$ ) demonstration assemblies were irradiated.

### 3.2 SAN ONOFRE NUCLEAR GENERATING STATION UNITS $2 \& 3$ (SONGS 2\&3)

SONGS $2 \& 3$ are commercial nuclear power plants. SONGS 2 began commercial operation in 1983. SONGS 3 began commercial operation
in 1984. Both units are in their fifth cycle of operation. SONGS 2\&3 are Combustion Engineering two-loop PWRs. Each unit produces 3390 megawatts-thermal at $100 \%$ rated power.

Each reactor core consists of 217 fuel assemblies arranged as shown in Figure 3.4. Both conventional and low leakage fuel management patterns have been used. Each fuel assembly consists of a $16 \times 16$ array of 236 fuel/burnable absorber rods and 5 control rod guide tubes. A typical fuel assembly cross-section is shown in Figure 3.5. Core, fuel assembly, control rod, and burnable absorber data are summarized in Table 3.2.

The fuel rods consist of slightly enriched (1.87 to 4.05 weight percent U-235) $\mathrm{UO}_{2}$ pellets clad in Zircaloy-4. The control rod guide tubes are also Zircaloy-4. Ten Zircaloy-4 grids and one Inconel-718 grid are located along the length of the assembly.

The in-core instrumentation system for power distribution measurement consists of 56 strings of fixed Rhodium detectors. Each detector string consists of five individual, 40 cm long, Rhodium detectors placed at about $10,30,50,70$, and 90 percent of active core height. The detector signals are processed offline with the Combustion Engineering CECOR program (Reference 14) to determine the power distribution in the core. The 56 instrumented core locations are shown in Figure 3.6.

There are 83 full-length and eight part-length (PL) control rods,
called control element assemblies (CEA's). Seventy-nine fulllength CEA's have five identical individual absorber rods consisting of 1-1/8" Inconel nose cap, 12-1/2" Ag/In/Cd, and 136" of $B_{4} C$ pellets. Four full-length CEA's located on the periphery of the core have four identical individual absorber rods consisting of 8-5/8" Inconel nose cap, $5^{\prime \prime} \mathrm{Ag} / \mathrm{In} / \mathrm{Cd}$, and 135-1/2" of $B_{4} C$ pellets. . The eight PLCEA's each have five identical absorber rods consisting of $75^{\prime \prime}$ of Inconel; 58" of water filled Inconel tube, and $16^{\prime \prime}$ of $\mathrm{B}_{4} \mathrm{C}$ pellets. The cladding material is Inconel-625. The CEA's are moved in nine symmetrical groups: Regulating Groups 1 through 6, PLCEA, and Shutdown Groups A and B. Figure 3.4 shows the CEA locations.

Burnable absorber rods, consisting of $\mathrm{B}_{4} \mathrm{C}-\mathrm{Al}_{2} \mathrm{O}_{3}$ pellets in Zircaloy-4 cladding, were used in all cycles for both units. The burnable absorber rods have the same outer dimension as fuel rods and replace fuel rods when used.

The SONGS $2 \& 3$ reactors have several unique features. The outermost row of four assemblies does not line up with the next interior row of assemblies. The four-finger CEA inserted in the middle pair of these "off-set" assemblies has two fingers in one assembly and two fingers in the adjacent assembly. The burnable absorber rods in SONGS $2 \& 3$ do not extend the full length of the active fuel region and result in axially zoned fuel assemblies. Both units have been transitioned to 24 -month fuel cycles with Cycle 5 being the second such cycle for each unit. Finally, the five control rod guide tubes per fuel assembly are large compared to Westinghouse and Babcock \& Wilcox designs and displace four fuel rods each.

### 3.3 ARKANSAS NUCLEAR ONE - UNIT 2 (ANO-2)

ANO-2 is a commercial nuclear power plant operated by the Arkansas Power And Light Company. ANO-2 began commercial operation in 1980, and only data from the first cycle of operation are used in this report. The plant is a Combustion Engineering two-loop PWR. The reactor core produces 2815 megawatts - thermal at $100 \%$ rated power.

The reactor core consists of 177 fuel assemblies arranged as shown in Figure 3.7. Each fuel assembly consists of a 16 x 16 array of 236 fuel/burnable poison rods and five control rod guide tubes. A typical fuel assembly cross-section is shown in Figure 3.8. Core, fuel assembly, control rod, and burnable absorber data are summarized in Table 3.3.

The fuel rods consist of slightly enriched (1.93 to 2.94 weight percent U-235 in Cycle 1) $\mathrm{UO}_{2}$ pellets with Zircaloy-4 cladding. The control rod guide tubes are also Zircaloy-4. Eleven Zircaloy-4 grids and one Inconel-625 grid are located along the
length of the assembly.
The in-core instrumentation system for power distribution measurement consists of 44 strings of fixed Rhodium detectors. Each detector string consists of five individual, 40 cm long, Rhodium detectors placed at about $10,30,50,70$, and 90 percent of active core height. The detector signals are processed offline with the CECOR program (Reference 14). The 44 instrumented core locations are shown in Figure 3.9.

There are 73 full-length and eight part-length (PL) control rods, called control element assemblies (CEA's). The full-length CEA's have dissimilar absorber rods. The four corner rods consist of an Inconel nose cap, 12-1/2" of $\mathrm{Ag} / \mathrm{In} / \mathrm{Cd}$, and 135-1/2" of $\mathrm{B}_{4} \mathrm{C}$ pellets. The center absorber rod uses solid Inconel plugs instead of Ag/In/Cd. The eight PLCEA's each have five identical absorber rods consisting of $75^{\prime \prime}$ of Inconel, $58^{\prime \prime}$ of water filled Inconel tube, and $16^{\prime \prime}$ of $\mathrm{B}_{4} \mathrm{C}$ pellets. The cladding material is Inconel-625. The CEAs are moved in nine symmetrical groups: Regulating Groups 1 through 6, PLCEA, and Shutdown Groups A and B. Figure 3.7 shows the CEA locations.

Burnable absorber rods, consisting of $\mathrm{B}_{4} \mathrm{C}-\mathrm{Al}_{2} \mathrm{O}_{3}$ pellets in Zircaloy-4 cladding, are used. The burnable absorber rods have the same outer dimension as fuel rods and replace fuel rods when used.

Cycle 1 of ANO-2 has some unique features. The burnable absorber rods within some fuel assembly types are asymmetrically distributed (See Figure 3.9). Also the burnable absorber rods do not extend the full length of the active fuel region and result in axially zoned fuel assemblies. Finally, the five control rod guide tubes per fuel assembly are large compared to Westinghouse and Babcock \& Wilcox designs and displace four fuel rods each.

Table 3.1

## MECHANICAL DESIGN PARAMETERS

SONGS 1'

## Core description

Power Level
Number of Assemblies
Number of Control Rods
Fuel Assembly Pitch
Core area
Core Equivalent Diameter

## Fuel Assembly Description

Fuel Rod Array
Fuel Rod Pitch
Outside Dimension
Number of Guide Tubes
Guide Tube I.D.
Guide Tube O.D.
Guide Tube Material
Fuel Rod Description
Material
Pellet \% t.d. of $10.96 \mathrm{~g} / \mathrm{cm}^{3}$
Pellet Diameter
Clad Material
Clad I.D.
Clad O.D.
Clad Thickness
Active Fuel Length
Full Length Control Rod
Number
Clad Material
Clad Thickness
Clad O.D.
Absorber
Material
Diameter
Length

1347 Megawatts-Thermal
157
45
7.803 inches
67.1 Square Feet
110.9 inches
$14 \times 14$
0.556 inches
7.76 inches

16
0.535 inches
0.511 inches

Stainless Steel
$\mathrm{UO}_{2}$
95 nominal
0.3835 inches

Stainless Steel
0.389 inches
0.422 inches
0.0165 inches

120 inches

45 (16-Finger)
Stainless Steel
0.0185 inches
0.4315 inches

Ag-In-Cd
0.3905 inches

133 inches

## EEI* Mixed Oxide Assemblies

Number of Assemblies
Fuel Rod Array
Outside Dimension
Rod pitch
Number of Guide Tubes
Guide Tube Material

## EEI Mixed oxide Fuel Rods

Clad Material
Outside Diameter
Diametral Gap
Clad Thickness
Fuel Length
EEI Mixed Oxide Fuel Pellets
Diameter
Length
Material
Density, \% T. D.
Enrichment (w/o fissile Pu)
Pu Isotopics
a/o Pu-239
a/o Pu-240
0.3659 inches
0.600 inches
$\mathrm{PuO}_{2}-\mathrm{UO}_{2}$
91
$2.84 / 3.10 / 3.31$
80.6
a/o Pu-241
13.4
a/o Pu-242
5.2
0.8
*EEI: Edison Electric Institute.

## MECHANICAL DESIGN PARAMETERS

SONGS 2\&3

## Core description

Power Level
Number of Assemblies Number of Control Rods Fuel Assembly Pitch Core area
Core Equivalent Diameter
Fuel Assembly Description

Fuel Rod Array
Fuel Rod Pitch
Outside Dimension
Number of Guide Tubes
Guide Tube I.D.
Guide Tube O.D.
Guide Tube Material

## Fuel Rod Description

Material
Stack Height Density
Pellet Diameter
Clad Material
Clad I.D.
Clad O.D.
Clad Thickness
Active Fuel Length
Full-Length Control Rod
Number
5-Finger
4-Finger
Clad Material
Clad Thickness
Clad O.D.
Poison
Material
Length
5-Finger
4-Finger

83
3390 Megawatts-Thermal
217
91
8.180 inches
101.1 Square Feet

136 inches
$16 \times 16$
0.506 inches
7.972 inches

5
0.90 inches
0.98 inches

Zircaloy-4
$\mathrm{UO}_{2}$
$10.061 \mathrm{~g} / \mathrm{cm}^{3}$
0.325 inches

Zircaloy-4
0.332 inches
0.382 inches
0.025 inches

150 inches

79
4
Inconel-625
0.035 inches
0.816 inches
$\mathrm{B}_{4} \mathrm{C} / \mathrm{Ag}-\mathrm{In}-\mathrm{Cd} /$ Inconel
136" 12.5" 0.6"
135.5" 5.0" 8.6"
$B_{4} C$ pellet
Diameter
$\%$ T. D. of $2.52 \mathrm{~g} / \mathrm{cm}^{3}$
Weight \% Boron, Min
Part Length Control Rod
Number
Clad Material
Clad Thickness
Clad O.D.
Poison
Material
Length
$B_{4} C$ pellet
Diameter
$\%$ T. D. of $2.52 \mathrm{~g} / \mathrm{cm}^{3}$.
Weight \% Boron, Min

Burnable Poison Rod
Absorber Material
Pellet Diameter
Pellet Length
Pellet Density, Min \% T. D.
Theoretical Density, $\mathrm{Al}_{2} \mathrm{O}_{3}$
Theoretical Density, $\mathrm{B}_{4} \mathrm{C}$
Clad Material
Clad I.D.
Clad O.D.
Clad Thickness
Diametral Gap (Cold)
Active Length
0.737 inches

73
77.5

8 ( 5-Fingers )
Inconel-625
0.035 inches
0.816 inches

Inconel / WATER / $\mathrm{B}_{4} \mathrm{C}$
75 " 58 " 16"
0.737 inches

73
77.5
$\mathrm{Al}_{2} \mathrm{O}_{3}-\mathrm{B}_{4} \mathrm{C}$
0.307 inches
1.0 inches

93
$3.94 \mathrm{~g} / \mathrm{cm}^{3}$
$2.52 \mathrm{~g} / \mathrm{cm}^{3}$
Zircaloy-4
0.332 inches
0.382 inches
0.025 inches
0.025 inches
136.0 inches

Table 3.3

## MECHANICAL DESIGN PARAMETERS

## ANO-2

## Core description

Power Level
Number of Assemblies
Number of Control Rods
Fuel Assembly Pitch
Core area
Core Equivalent Diameter
Fuel Assembly Description
Fuel Rod Array
Fuel Rod Pitch
Outside Dimension
Number of Guide Tubes
Guide Tube I.D.
Guide Tube O.D.
Guide Tube Material
Fuel Rod Description
Material
Stack Height Density
Pellet Diameter
Clad Material
Clad I.D.
Clad O.D.
Clad Thickness
Active Fuel Length

## Full Length Control Rod

Number
Clad Material
Clad Thickness
Clad O.D.
Center Finger
Poison Material
Length
Outside Fingers
Poison Material Length

2815 Megawatts - Thermal 177
81
8.177 inches
82.25 Square Feet

123 inches
$16 \times 16$
0.506 inches
7.977 inches

5
0.90 inches
0.98 inches

Zircaloy-4
$\mathrm{UO}_{2}$
$10.061 \mathrm{~g} / \mathrm{cm}^{3}$
0.325 inches

Zircaloy-4
0.332 inches
0.382 inches
0.025 inches

150 inches

73 (5-Finger)
Inconel-625
0.035 inches
0.816 inches
$\mathrm{B}_{4} \mathrm{C}$ / Inconel
135.5" 12.5"
$\mathrm{B}_{4} \mathrm{C}$ / Ag-In-Cd
135.5"
12.5"

Full Length control Rod (continued)
$\mathrm{B}_{4} \mathrm{C}$ pellet
Diameter
$\%$ T. D. of $2.52 \mathrm{~g} / \mathrm{cm}^{3}$
Weight \% Boron, Min
0.737 inches

73
77.5

## Part Lenath Control Rod

| Number | 8 ( 5-Fingers |
| :---: | :---: |
| Clad Material | Inconel-625 |
| Clad Thickness | 0.035 inches |
| Clad O.D. | 0.816 inches |
| Poison |  |
| Material | Inconel / Water / $\mathrm{B}_{4} \mathrm{C}$ |
| Length | 75 " 58' 16" |
| $\mathrm{B}_{4} \mathrm{C}$ pellet |  |
| Diameter | 0.737 inches |
| \% T. D. of $2.52 \mathrm{~g} / \mathrm{cm}^{3}$ |  |
| Weight \% Boron, Min | 77.5 |

## Burnable Poison Rod

Absorber Material
Pellet Diameter
Pellet Length
Pellet Density, Min \% T. D.
Theoretical Density, $\mathrm{Al}_{2} \mathrm{O}_{3}$
Theoretical Density, $\mathrm{B}_{4} \mathrm{C}$
Clad Material
Clad I.D.
Clad O.D.
Clad Thickness
Diametral Gap (Cold) Active Length
$\mathrm{Al}_{2} \mathrm{O}_{3}-\mathrm{B}_{4} \mathrm{C}$
0.310 inches
0.50 inches min

85 min
$3.90 \mathrm{~g} / \mathrm{cm}^{3}$
$2.52 \mathrm{~g} / \mathrm{cm}^{3}$
Zircaloy-4
0.332 inches
0.382 inches
0.025 inches
0.022 inches
136.0 inches

Figure 3.1

## REACTOR CORE CONTROL ROD PATTERN SONGS 1



## SONGS 1



x GUIDE TUBE LOCATION

Figure 3.3

## REACTOR CORE INSTRUMENTATION LOCATIONS

 SONGS 1

1-30 indicate incore instrumentation location

Figure 3.4

## REACTOR CORE CONTROL ROD PATTERN

SONGS 2\&3


## TYPICAL FUEL ASSEMBLY

SONGS 2\&3

Figure 3.6
REACTOR CORE INSTRUMENTATION LOCATIONS SOM

1-56 indicates incore instrumentation location

Figure 3.7
REACTOR CORE CONTROL ROD PATTERN - ANO-2


* indicates the location of the worst stuck rod, A-52.

| BANK | NUMBER OF RODS |
| :---: | :---: |
| 1 | 8 |
| 2 | 8 |
| 3 | 8 |
| 4 | 4 |
| 5 | 4 |
| 6 | 5 |
| P | 8 |
| A | 16 |
| B | 20 |
| - --1 | 81 |
| TOTAL | 28 |

Figure 3.8

## TYPICAL FUEL ASSEMBLY

ANO-2

Pitch $=0.5063^{\prime \prime}$



- FUEL ROD LOCATION
$x \times$
$x x$ GUIDE TUBE LOCATION
- TYPICAL ASYMMETRIC BURNABLE ABSORBER LOCATION

REACTOR CORE INSTRUMENTATION LOCATIONS

$$
\text { ANO- } 2
$$



1-44 indicate incore instrumentation locations

## SECTION 4

## BENCHMARK COMPARISONS

### 4.0 INTRODUCTION

This section compares the calculated parameters and the measured plant data. The measured data are from zero power startup testing and normal operations at San Onofre Nuclear Generating Station (SONGS) Units 1, 2, 3, and Arkansas Nuclear One - Unit 2 (ANO-2). Six cycles at SONGS 1, five cycles from SONGS 2, four cycles from SONGS 3, and one cycle from ANO-2 were analyzed for a total of sixteen cycles including initial and reload cores. For each parameter compared, the sample mean and standard deviation of the observed differences were calculated. Based on the mean, standard deviation, and the sample size, a conservative 95/95 tolerance limit (bias $\pm$ reliability factor) was calculated.

Section 4.1 provides the Critical Boron Concentration (CBC) comparisons for Zero Power and Full Power conditions. Differences between calculated and measured data are represented in absolute terms, (Calculated - Measured). The SIMULATE-3 reactivity (1 - 1/Keff) is also calculated for each case:

Section 4.2 presents the Isothermal Temperature Coefficient (ITC) comparison. As in the CBC comparisons, the differences are in absolute terms.

Section 4.3 describes the Power Coefficient (PC) comparison with the differences represented in absolute terms.

Section 4.4 presents the control rod worth comparison. The difference between calculated and measured data is given in relative terms:

$$
\text { Difference }=(\text { Calculated }- \text { Measured }) / \text { Calculated } * 100 \% .
$$

Section 4.5 verifies the ability of SIMULATE-3 to predict the net ( $\mathrm{N}-1$ ) rod worth.

Section 4.6 presents the Inverse Boron Worth (IBW) comparison. The differences are calculated in relative terms.

Section 4.7 compares the SIMULATE-3 assembly (radial and axial) power distributions, axial offset, and incore detector signals with plant measurements. The axial offset differences are quantified in absolute terms, and the assembly peaking factor differences are quantified in relative terms.

### 4.1 CRITICAL BORON CONCENTRATION

SIMULATE-3 Critical Boron Concentration (CBC) and reactivity predictions were compared to zero-power startup test measurements as well as to full-power operating data. The most reliable measurements are the zero-power startup tests. These measurements are made under well controlled conditions without significant thermal and xenon feedbacks.

The zero-power comparison statistics quantify SIMULATE-3's accuracy in predicting CBC and reactivity for Beginning-of-Cycle (BOC), zero-power conditions without xenon in the core. The full-power operating boron concentration data are from titration of reactor coolant system samples. The measurements are adjusted for control rod insertions and deviations from full power, equilibrium conditions. These full-power comparisons serve as conservative estimates of the SIMULATE-3 uncertainties for atpower equilibrium conditions with thermal feedback.

Sections 4.1.1 and 4.1.2 present the comparisons for zero-power and full-power CBC and reactivity, respectively.

Table 4.1 lists the measured and SIMULATE-3 predicted values for BOC, zero-power, xenon free Critical Boron Concentrations (CBC), and SIMULATE-3 calculated reactivities at the measurement conditions for SONGS 1, 2, and 3. Thirty-two measurements from 15 cycles of startup tests are included. Of these measurements, seventeen are unrodded and fifteen are with control rods inserted in the core. Five of the measurements were taken with the reactor critical at low temperatures during initial cycle startups.

The low temperature measurements were taken at $150^{\circ} \mathrm{F}$ and $320^{\circ} \mathrm{F}$ for SONGS 1 and 2, respectively. The low temperature cases were included to show temperature dependencies, if any, in the SIMULATE-3 CBC prediction. Comparing the differences between the low temperature and Hot-Zero-Power ( $>535^{\circ} \mathrm{F}$ ) cases, it is concluded that the SIMULATE-3 CBC predictions are independent of the moderator's temperature.

A three-step statistical analysis was performed on the measured and SIMULATE-3 calculated CBC differences and on the SIMULATE-3 calculated reactivities for the CBCs as measured. First, the sample mean ( $\bar{x}$ ), standard deviation ( $S$ ), and Root-Mean-Squares (RMS) were calculated for CBC and reactivity differences, respectively. The differences are due to SIMULATE-3 calculational uncertainties, variations in B-10 isotopic concentrations, and measurement (titration) uncertainties. For example boron concentration measurement errors can be as high as 5 ppm . For conservatism, all differences are assumed due only to SIMULATE-3 calculational uncertainties.

Second, the two sample distributions were tested for normality using ANSI standard N15.15-1974 (Reference 15). The normality test is needed because the $95 / 95$ tolerance limit assumes that the population has a normal distribution. The test concludes that both distributions, CBC and reactivity differences, are normal. Finally, the bias, $95 / 95$ reliability factor and tolerance limit are calculated. Table 4.2 lists the results for each distribution using the method as described in Reference 16. The 95/95 tolerance limits for zero-power CBC and reactivity, for all temperatures and rodded conditions, are $-7 \pm 26 \mathrm{PPM}$ and $-0.08 \pm 0.26$ $\% \Delta k / k$, respectively.

Table 4.1
Zero Power Critical Boron Comparison
SONGS 1,2 , and 3
(Beginning of Cycle)

CRITICAL PPM S - M REACTIVITY UNIT CYCLE CASE MEAS. SIM-3 $\qquad$ ( $\% \Delta K / K)$

| 1 | 1 | $150^{\circ}{ }^{\circ}$ F, ARO | 2250 | 2268 | 18 | 0.157 |
| :--- | :--- | :--- | ---: | ---: | ---: | ---: |
| 1 | 1 | $150^{\circ}$ F, BANK 2 IN | 2050 | 2052 | 2 | 0.024 |
| 1 | 1 | $150^{\circ}{ }^{\circ}$ F, BANK1 IN | 1898 | 1892 | -6 | -0.047 |
| 1 | 1 | HZP, ARO | 2524 | 2522 | -2 | -0.009 |
| 1 | 1 | HZP, BANK 2 IN | 2197 | 2187 | -10 | -0.067 |
| 1 | 1 | HZP, BANK 1 IN | 1944 | 1929 | -15 | -0.108 |
| 1 | 2 | HZP, ARO | 1609 | 1595 | -14 | -0.093 |
| 1 | 3 | HZP, ARO | 1876 | 1887 | 11 | 0.068 |
| 1 | 4 | HZP, ARO | 1956 | 1952 | -4 | -0.025 |
| 1 | 5 | HZP, ARO | 1822 | 1833 | 11 | 0.072 |
| 1 | 6 | HZP, ARO | 1774 | 1773 | -1 | -0.004 |
|  |  |  |  |  |  |  |
| 2 | 1 | $320^{\circ}{ }^{\circ}$ F, ARO | 869 | 857 | -12 | -0.171 |
| 2 | 1 | $320^{\circ}$ F, BANKS 6-4 IN | 797 | 783 | -14 | -0.208 |
| 2 | 1 | HZP, ARO | 833 | 824 | -9 | -0.115 |
| 2 | 1 | HZP, BANKS 6-3 IN | 629 | 614 | -15 | -0.188 |
| 2 | 1 | HZP, BANKS 6-1 IN | 499 | 472 | -27 | -0.342 |
| 2 | 2 | HZP, ARO | 1198 | 1174 | -24 | -0.249 |
| 2 | 2 | HZP, BANKS 6-1 IN | 883 | 849 | -34 | -0.360 |
| 2 | 3 | HZP, ARO | 1580 | 1561 | -19 | -0.171 |
| 2 | 3 | HZP, BANK B IN | 1382 | 1370 | -12 | -0.104 |
| 2 | 4 | HZP, ARO | 1803 | 1802 | -1 | -0.011 |
| 2 | 4 | HZP, BANK B IN | 1563 | 1547 | -16 | -0.127 |
| 2 | 5 | HZP, ARO | 1620 | 1640 | 20 | 0.164 |
| 2 | 5 | HZP, BANKS 6-1 IN | 1208 | 1208 | 0 | 0.003 |


| UNIT | CYCLE | CASE |  | CRITICAL PPM |  | $\begin{gathered} S-M \\ (\mathrm{PPM}) \end{gathered}$ | REACTIVITY$(\% \Delta K / K)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | MEAS. | SIM-3 |  |  |
| 3 | 1 | HZP, | ARO | 823 | 824 | 1 | -0.001 |
| 3 | 1 | HZP, | BANKS 6-1 IN | 483 | 472 | -11 | -0.149 |
| 3 | 2 | HZP, | ARO | 1174 | 1161 | -13 | -0.139 |
| 3 | 2 | HZP, | BANK B IN | 968 | 953 | -15 | -0.165 |
| 3 | 3 | HZP, | ARO | 1550 | 1550 | 0 | 0.001 |
| 3 | 3 | HZP, | BANK B IN | 1369 | 1361 | -6 | -0.067 |
| 3 | 4 | HZP, | ARO | 1822 | 1831 | 9 | 0.071 |
| 3 | 4 | HZP, | BANKS 6-1 IN | 1403 | 1392 | $-11$ | -0.090 |
|  |  |  |  |  |  | $\overline{\mathrm{x}}$-7 | -0.08 |
|  |  |  |  |  |  | s 12 | 0.12 |
|  |  |  |  |  |  | n 32 | 32 |

## (BOC, No Xenon)

|  | $\triangle \mathrm{PPM}$ | \% $\Delta \mathrm{k} / \mathrm{k}$ |
| :---: | :---: | :---: |
| Mean ( $\overline{\mathrm{x}}$ ) | -7 | -0.08 |
| Standard Deviation (S) | 12 | 0.12 |
| RMS | 14 | 0.14 |
| Normality Test |  |  |
| Test Value (W) | 0.972 | 0.976 |
| Critical Value* | 0.930 | 0.930 |
| Result | Normal | Normal |
| Sample Size | 32 | 32 |
| Degree Of Freedom | 31 | 31 |
| $\mathrm{k}_{95 / 95}$ | 2.197 | 2.197 |
| $\mathrm{k}_{95 / 95}$ * S | 26 | 0.26 |
| Bias | -7 | -0.08 |
| 95/95 Tolerance Limit | $-7 \pm 26$ | $-0.08 \pm 0.26$ |

Tables 4.3 to 4.10 compare the measured HFP CBCs from core follow calculations for SONGS 2 and 3 Cycles $1-4$ to the SIMULATE-3 results. Two low-power CBC measurements, one each from cycle 1 of SONGS 3 and Cycle 2 of SONGS 2 are also included to demonstrate that there is no significant increase in the differences at power levels less than 100\%. There are a total of 112 measurements from eight operating cycles. The reactivity data are plotted against the cycle burnup (GWD/T) in Figure 4.1.

The SIMULATE-3 at-power CBC and reactivity $95 / 95$ tolerance limits were determined using the statistical methods outlined in section 4.1.1. As summarized in Table 4.11, the 95/95 tolerance limits for all at-power and rodded or unrodded conditions for CBC and reactivity are $2 \pm 34 \mathrm{ppm}$ and $0.01 \pm 0.35 \% \Delta \mathrm{k} / \mathrm{k}$, respectively.

Table 4.3
SONGS 2 Cycle 1 HFP Critical Boron Comparison

| CYCLE | BURNUP | CRITICAL PPM |  | S - M | CRITICAL | REACTIVITY |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| GWD/T | EFPD | MEAS. | SIM-3 | (PPM) | K-EFF | (\% $\mathrm{O} / \mathrm{K} / \mathrm{K}$ ) |
| 1.934 | 51.2 | 476 | 461 | -15 | 0.99826 | -0.174 |
| 3.023 | 80.0 | 465 | 441 | -24 | 0.99727 | -0.274 |
| 4.039 | 106.9 | 457 | 421 | -36 | 0.99600 | -0.402 |
| 4.978 | 131.8 | 432 | 399 | -33 | 0.99633 | -0.368 |
| 5.977 | 158.2 | 402 | 380 | -22 | 0.99755 | -0.246 |
| 7.003 | 185.4 | 374 | 348 | -26 | 0.99712 | -0.289 |
| 7.987 | 211.4 | 342 | 311 | -31 | 0.99646 | -0.355 |
| 8.970 | 237.4 | 301 | 274 | -27 | 0.99688 | -0.313 |
| 9.994 | 264.5 | 252 | 229 | -23 | 0.99733 | -0.268 |
| 10.944 | 289.7 | 204 | 183 | -21 | 0.99755 | -0.246 |
| 12.030 | 318.4 | 138 | 125 | -13 | 0.99841 | -0.159 |
| 12.977 | 343.5 | 80 | 70 | -10 | 0.99876 | -0.124 |

Table 4.4
SONGS 3 Cycle 1 HFP Critical Boron Comparison

| CYCLE | BURNUP | CRITICAL PPM |  | $\begin{aligned} & S-M \\ & (P P M) \end{aligned}$ | CRITICAL REACTIVITYK-EFF $(\% \Delta \mathrm{~K} / \mathrm{K})$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| GWD/T | EFPD | MEAS. | SIM-3 |  |  |  |
| 1.323 | 35.0 | 472 | 457 | -15 | 0.99826 | -0.174 |
| 2.356 | 62.4 | 471 | 455 | -16 | 0.99820 | -0.180 |
| 3.345 | 88.5 | 455 | 436 | -19 | 0.99786 | -0.214 |
| 4.955 | 131.2 | 430 | 410 | -20 | 0.99772 | -0.229 |
| 6.160 | 163.1 | 391 | 369 | -22 | 0.99756 | -0.245 |
| 6.935 | 183.6 | 377 | 347 | -30 | 0.99663 | -0.338 |
| 8.075 | 213.7 | 332 | 314 | -18 | 0.99794 | -0.206 |
| 9.370 | 248.0 | 279 | 258 | -21 | 0.99757 | -0.244 |
| 11.590 | 306.8 | 163 | 150 | -13 | 0.99845 | -0.155 |
| 12.357 | 327.1 | 121 | 107 | -14 | 0.99830 | -0.170 |
| 13.972 | 369.8 | 115 | 94 | -21 | 0.99736 | -0.265 |
|  | 5\% POWE |  |  |  |  |  |

Table 4.5
SONGS 2 Cycle 2 HFP Critical Boron Comparison

| CYCLE | BURNUP | CRITICAL PPM |  | $\begin{aligned} & S-M \\ & (P P M) \end{aligned}$ | CRITICAL REACTIVITYK-EFF $(\% \Delta K / K)$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| GWD/T | EFPD | MEAS. | SIM-3 |  |  |  |
| 0.800 | 21.2 | 741 | 750 | 9 | 1.00091 | 0.091 |
| 1.758 | 46.5 | 684 | 675 | -9 | 0.99909 | -0.091 |
| 2.258 | 59.8 | 654 | 636 | -18 | 0.99812 | -0.188 |
| 3.907 | 103.4 | 532 | 501 | -31 | 0.99678 | -0.323 |
| 5.941 | 157.3 | 339 | 332 | -7 | 0.99927 | -0.073 |
| 7.054 | 186.7 | 260 | 243 | -17 | 0.99819 | -0.181 |
| 7.726 | 204.5 | 182 | 187 | 5 | 1.00041 | 0.041 |
| 9.241 | 244.6 | 56 | 65 | 9 | 1.00107 | 0.107 |
| 9.612 | 254.4 | 72 | 77 | 5 | 1.00054 | 0.054 |
|  | (80\% POWER) |  |  |  |  |  |

## Table 4.6 <br> SONGS 3 Cycle 2 HFP Critical Boron Comparison

| CYCLE | BURNUP |
| :--- | ---: |
| GWD/T | EFPD |
| 0.613 | 16.2 |
| 1.133 | 30.0 |
| 2.019 | 53.4 |
| 2.771 | 73.3 |
| 3.929 | 104.0 |
| 4.982 | 131.9 |
| 5.783 | 153.1 |
| 7.041 | 186.4 |
| 7.996 | 211.7 |


| CRITICAL |  |  | PPM |
| :---: | ---: | :---: | :---: |
| MEAS. | SIM-3 |  |  |
| 722 | 750 |  |  |
| 690 | 708 |  |  |
| 623 | 636 |  |  |
| 560 | 575 |  |  |
| 471 | 479 |  |  |
| 376 | 392 |  |  |
| 320 | 326 |  |  |
| 203 | 221 |  |  |
| 122 | 148 |  |  |



Table 4.7

## SONGS 2 Cycle 3 HFP Critical Boron Comparison

| CYCLE | BURNUP |
| ---: | ---: |
| GWD/T | EFPD |
| 1.006 | 27.1 |
| 1.987 | 53.6 |
| 2.965 | 79.9 |
| 3.907 | 105.3 |
| 5.182 | 139.7 |
| 6.015 | 162.1 |
| 6.957 | 187.5 |
| 8.100 | 218.3 |
| 8.965 | 241.6 |
| 10.026 | 270.2 |
| 10.913 | 294.1 |
| 12.078 | 325.5 |
| 13.042 | 351.5 |
| 13.944 | 375.8 |

CRITICAL PPM | MEAS. | SIM-3 |
| :---: | :---: |
| 1045 | 1060 | $977 \quad 981$ $907 \quad 905$ $834 \quad 831$ $733 \quad 731$ 678667 593596 $512 \quad 509$ $441 \quad 445$ $360 \quad 365$ 286299 $205 \quad 214$

$135 \quad 143$ $61 \quad 77$

S - M CRITICAL REACTIVITY
(PPM)
15 $\mathrm{K}-\mathrm{EFF}(\% \Delta \mathrm{~K} / \mathrm{K})$ 0.127
$4 \quad 1.00035 \quad 0.035$
$-2 \quad 0.99986 \quad-0.014$
$-3 \quad 0.99975 \quad-0.025$
$-2 \quad 0.99987 \quad-0.013$
$\begin{array}{lll}-11 & 0.99900 & -0.100\end{array}$
$3 \quad 1.00024 \quad 0.024$
$-3 \quad 0.99973 \quad-0.027$
$4 \quad 1.00031 \quad 0.031$
$5 \quad 1.00045 \quad 0.045$
$13 \quad 1.00127 \quad 0.127$
$9 \quad 1.00084 \quad 0.084$
$8 \quad 1.00081 \quad 0.081$
$16 \quad 1.00164 \quad 0.164$

## Table 4.8 <br> SONGS 3 Cycle 3 HFP Critical Boron Comparison

| CYCLE | BURNUP |
| ---: | ---: |
| GWD/T | EFPD |
| 0.664 | 17.9 |
| 0.961 | 25.9 |
| 1.997 | 53.8 |
| 3.008 | 81.1 |
| 3.860 | 104.0 |
| 5.064 | 136.5 |
| 6.021 | 162.3 |
| 6.981 | 188.1 |
| 8.100 | 218.3 |
| 8.988 | 242.2 |
| 9.944 | 268.0 |
| 10.908 | 294.0 |
| 12.067 | 325.2 |
| 12.950 | 349.0 |
| 13.986 | 376.9 |


| CRITICAL PPM |  | $S-M$ | CRITICAL | REACTIVI |
| :---: | :---: | :---: | :---: | :---: |
| MEAS. | SIM-3 | (PPM) | K-EFF | (\% $\mathrm{O} \mathrm{K} / \mathrm{K}$ ) |
| 1048 | 1070 | 22 | 1.00190 | 0.190 |
| 1026 | 1044 | 18 | 1.00165 | 0.165 |
| 960 | 966 | 6 | 1.00055 | 0.055 |
| 903 | 887 | -16 | 0.99865 | -0.135 |
| 840 | 825 | -15 | 0.99866 | -0.134 |
| 741 | 728 | -13 | 0.99884 | -0.116 |
| 654 | 655 | 1 | 1.00001 | 0.001 |
| 580 | 581 | 1 | 1.00008 | 0.008 |
| 492 | 497 | 5 | 1.00049 | 0.049 |
| 427 | 431 | 4 | 1.00033 | 0.033 |
| 359 | 360 | 1 | 1.00005 | 0.005 |
| 281 | 281 | 0 | 1.00135 | 0.135 |
| 189 | 204 | 15 | 1.00152 | 0.152 |
| 121 | 140 | 19 | 1.00197 | 0.197 |
| 42 | 64 | 22 | 1.00228 | 0.227 |


| CYCLE | BURNUP | CRITICAL PPM |  | $S-M$ | CRITICAL | REACTIVITY |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| GWD/T | EFPD | MEAS. | SIM-3 | (PPM) | K-EFF | (\% $\% \mathrm{~K} / \mathrm{K}$ ) |
| 0.709 | 18.7 | 1253 | 1286 | 33 | 1.00259 | 0.258 |
| 1.993 | 52.6 | 1185 | 1219 | 34 | 1.00274 | 0.273 |
| 2.893 | 76.3 | 1154 | 1174 | 20 | 1.00156 | 0.156 |
| 4.080 | 107.6 | 1081 | 1112 | 31 | 1.00236 | 0.235 |
| 4.986 | 131.5 | 1041 | 1060 | 19 | 1.00149 | 0.149 |
| 5.968 | 157.4 | 992 | 1004 | 12 | 1.00100 | 0.100 |
| 6.962 | 183.6 | 943 | 950 | 7 | 1.00063 | 0.063 |
| 8.008 | 211.2 | 897 | 890 | -7 | 0.99941 | -0.059 |
| 8.899 | 234.7 | 827 | 843 | 16 | 1.00127 | 0.127 |
| 9.897 | 261.0 | 773 | 786 | 13 | 1.00081 | 0.081 |
| 11.091 | 292.5 | 705 | 714 | 9 | 1.00072 | 0.072 |
| 12.069 | 318.3 | 648 | 655 | 7 | 1.00062 | 0.062 |
| 12.976 | 342.2 | 598 | 599 | 1 | 1.00009 | 0.009 |
| 13.616 | 359.1 | 554 | 558 | 4 | 1.00035 | 0.035 |
| 14.837 | 391.3 | 448 | 479 | 31 | 1.00275 | 0.274 |
| 15.835 | 417.6 | 382 | 408 | 26 | 1.00231 | 0.230 |
| 16.680 | 439.9 | 324 | 347 | 23 | 1.00205 | 0.205 |
| 17.605 | 464.3 | 243 | 284 | 41 | 1.00379 | 0.378 |
| 19.054 | 502.5 | 131 | 172 | 41 | 1.00394 | 0.392 |
| 20.028 | 528.2 | 65 | 98 | 33 | 1.00323 | 0.322 |


| CYCLE | BURNUP | CRITICAL PPM |  | S - M | CRITICAL | REACTIVITY |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| GWD/T | EFPD |  |  | (PPM) | K-EFF | (\% $\Delta \mathrm{K} / \mathrm{K}$ ) |
| 0.482 | 12.7 | 1291 | 1334 | 43 | 1.00338 | 0.337 |
| 1.388 | 36.6 | 1264 | 1282 | 18 | 1.00143 | 0.143 |
| 2.101 | 55.4 | 1248 | 1232 | -16 | 1.00127 | 0.127 |
| 3.033 | 80.0 | 1198 | 1199 | 1 | 1.00010 | 0.010 |
| 3.974 | 104.8 | 1153 | 1147 | -6 | 0.99964 | -0.036 |
| 4.937 | 130.2 | 1118 | 1096 | -22 | 0.99825 | -0.175 |
| 6.086 | 160.5 | 1032 | 1031 | -1 | 0.99990 | -0.010 |
| 6.977 | 184.0 | 983 | 980 | -3 | 0.99977 | -0.023 |
| 7.955 | 209.8 | 938 | 924 | -14 | 0.99892 | -0.108 |
| 9.123 | 240.6 | 851 | 859 | 8 | 1.00069 | 0.069 |
| 10.105 | 266.5 | 803 | 801 | -2 | 0.99987 | -0.013 |
| 11.417 | 301.1 | 720 | 731 | 11 | 1.00089 | 0.089 |
| 12.312 | 324.7 | 666 | 670 | 4 | 1.00029 | 0.029 |
| 13.286 | 350.4 | 610 | 608 | -2 | 0.99986 | -0.014 |
| 14.041 | 370.3 | 557 | 559 | 2 | 1.00013 | 0.013 |
| 15.338 | 404.5 | 468 | 469 | 1 | 1.00004 | 0.004 |
| 16.316 | 430.3 | 401 | 398 | -3 | 0.99977 | -0.023 |
| 17.211 | 453.9 | 329 | 333 | 4 | 1.00034 | 0.034 |
| 18.151 | 478.7 | 257 | 264 | 7 | 1.00065 | 0.065 |
| 19.168 | 505.5 | 173 | 187 | 14 | 1.00135 | 0.135 |
| 20.093 | 529.9 | 89 | 120 | 31 | 1.00299 | 0.298 |
| 20.863 | 550.2 | 24 | 55 | 31 | 1.00311 | 0.310 |

Figure 4.1
SIMULATE-3 Critical Reactivity at HFP vs. Burnup
A14. S2C1 a $a \Delta a \triangle 53 C 1$
$\begin{array}{ll}0.0 .52 C 2 & 0000 \\ \text { SJC2 } \\ \text { S2C3 }\end{array}$

- men S2C3 oooeo S3C3
***S2C4 SBC4 FROM SONGS 2 AND 3 CORE FOLLOW CALCULATIONS

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## Critical Boron Results

|  | $\triangle \mathrm{PPM}$ | $\% \Delta \mathrm{k} / \mathrm{k}$ |
| :---: | :---: | :---: |
| Mean ( $\overline{\mathrm{x}}$ ) | +2 | 0.0121 |
| Standard Deviation (S) | 18 | 0.1810 |
| RMS | 18 | 0.1806 |
| Normality Test |  |  |
| Test Value ( ${ }^{\prime}$ ) | 338.1 | 336.5 |
| Critical Values* | 326.8 | 326.8 |
|  | 339.8 | 339.8 |
| Result | Normal | Normal |
| Sample Size | 112 | 112 |
| Degree of Freedom | 111 | 111 |
| $\mathbf{k}_{95 / 95}$ | 1.909 | 1.909 |
| $\mathrm{K}_{95 / 95}$ * S | 34 | 0.35 |
| Bias | 2 | 0.01 |
| 95/95 Tolerance Limit | $2 \pm 34$ | $0.01 \pm 0.35$ |

### 4.2 ISOTHERMAL TEMPERATURE COEFFICIENT

The Isothermal Temperature Coefficient (ITC) is the change in the reactivity due to a $1^{\circ} \mathrm{F}$ change in the core average moderator and fuel temperature. Tables 4.12 and 4.13 list the comparisons of the calculated ITC's with measurements at SONGS 1,2 , and 3 . The temperature, power level, control rod position, and soluble boron concentration are also included. The measurements span a wide range of soluble boron concentrations (145 PPM to 2524 PPM ) and temperatures $\left(150^{\circ} \mathrm{F}\right.$ to $\left.583^{\circ} \mathrm{F}\right)$. There are a total of 54 measurements from 14 cycles of operation. The measured and SIMULATE-3 calculated ITC differences have been plotted in Figure 4.2.

A statistical analysis has been performed on the ITC difference, (Calculated - Measured), using the process outlined in section 4.1.1 to determine the $95 / 95$ tolerance limit for all power, moderator temperature and rodded conditions. As summarized in Table 4.14, the $95 / 95$ tolerance limit (bias $\pm$ reliability factor) is $(0.05 \pm 0.24) * 10^{-4} \Delta \mathrm{~K} / \mathrm{K} /{ }^{\circ} \mathrm{F}$.

## Zero-Power ITC comparison

| UNIT | CYCLE | (DEG. F) | CONTROL <br> ROD POSITION | BORON <br> (PPM) | $\begin{aligned} & \text { ITC }\left(10^{-4}\right. \\ & \text { MEASURED } \end{aligned}$ | $\begin{gathered} \Delta K / K /{ }^{\circ} \\ \text { SIM }-3 \\ \hline \end{gathered}$ | F) $P-M$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1 | 150 | ARO | 2250 | 0.340 | 0.257 | -0.083 |
|  | 1 | 150 | BANK 2 IN | 2050 | 0.240 | 0.140 | -0.100 |
|  | 1 | 150 | BANK 1 IN | 1898 | 0.160 | 0.045 | -0.115 |
|  | 1 | 535 | ARO | 2524 | 0.740 | 0.902 | 0.162 |
|  | 1 | 535 | BANK 2 IN | 2197 | 0.230 | 0.387 | 0.157 |
|  | 1 | 535 | BANK 1 IN | 1944 | -0.170 | -0.046 | 0.124 |
|  | 2 | 535 | ARO | 1609 | -0.590 | -0.482 | 0.108 |
|  | 2 | 535 | BANK 2 IN | 1160 | -1.357 | -1.224 | 0.133 |
|  | 3 | 535 | ARO | 1876 | -0.350 | -0.247 | 0.103 |
|  | 3 | 535 | BANK 1 IN | 1318 | -1.190 | -1.081 | 0.109 |
|  | 4 | 535 | ARO | 1956 | -0.338 | -0.157 | 0.181 |
|  | 4 | 535 | BANK 1 IN | 1425 | -1.204 | -0.983 | 0.221 |
|  | 6 | 535 | ARO | 1774 | -0.604 | -0.390 | 0.214 |
| 2 | 1 | 320 | ARO | 869 | -0.143 | -0.093 | 0.050 |
|  | 1 | 320 | BANKS 6-4 IN | 797 | -0.346 | -0.325 | 0.021 |
|  | 1 | 545 | ARO | 833 | -0.380 | -0.326 | 0.054 |
|  | 2 | 545 | ARO | 1198 | 0.075 | 0.180 | 0.105 |
|  | 2 | 545 | BANKS 6-1 IN | 883 | -0.914 | -0.851 | 0.063 |
|  | 3 | 545 | ARO | 1580 | 0.050 | 0.183 | 0.133 |
|  | 3 | 545 | BANK B IN | 1382 | -0.588 | -0.545 | 0.043 |
|  | 4 | 545 | ARO | 1803 | 0.077 | 0.212 | 0.135 |
|  | 4 | 545 | BANK B IN | 1563 | -0.364 | -0.331 | 0.033 |
|  | 5 | 545 | ARO | 1620 | -0.082 | 0.013 | 0.095 |
|  | 5 | 545 | BANKS 6-1 IN | 1208 | -0.860 | -0.874 | -0.014 |
| 3 | 1 | 545 | ARO | 823 | -0.450 | -0.343 | 0.107 |
|  | 1 | 545 | BANKS 6-1 IN | 484 | -1.512 | -1.388 | 0.124 |
|  | 2 | 545 | ARO | 1175 | 0.052 | 0.141 | 0.089 |
|  | 2 | 545 | BANK B IN | 968 | -0.570 | -0.586 | -0.016 |
|  | 3 | 545 | ARO | 1550 | 0.043 | 0.143 | 0.100 |
|  | 3 | 545 | BANK B IN | 1369 | -0.613 | -0.570 | 0.043 |
|  | 4 | 545 | ARO | 1822 | 0.113 | 0.242 | 0.129 |
|  | 4 | 545 | BȦNKS 6-1 IN | 1403 | -0.660 | -0.612 | 0.048 |

## At-Power ITC comparison

| UNIT | CYCLE | POWER <br> (\%) | $\begin{gathered} \text { BURNUP } \\ \text { (GWD/T) } \end{gathered}$ | $\begin{gathered} \mathrm{CBC} \\ (\mathrm{PPM}) \end{gathered}$ | ITC (10 MEASURED | $\begin{gathered} \Delta K / K / \\ S I M-3 \end{gathered}$ | P - M |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 1 | 20 | 0.103 | 660 | -0.628 | -0.632 | -0.004 |
|  | 1 | 50 | 0.539 | 559 | -0.824 | -0.841 | -0.017 |
|  | 1 | 80 | 1.250 | 512 | -0.942 | -0.983 | -0.041 |
|  | 1 | 100 | 2.050 | 483 | -1.037 | -1.156 | -0.119 |
|  | 1 | 100 | 9.180 | 287 | -1.647 | -1.575 | 0.072 |
|  | 2 | 98 | 0.208 | 818 | -0.730 | -0.760 | -0.030 |
|  | 2 | 100 | 1.466 | 693 | -1.250 | -1.043 | 0.207 |
|  | 2 | 100 | 6.650 | 268 | -2.230 | -2.037 | 0.193 |
|  | 2 | 100 | 8.123 | 145 | -2.542 | -2.333 | 0.209 |
|  | 3 | 100 | 0.380 | 1095 | -0.781 | -0.761 | 0.020 |
|  | 3 | 100 | 1.336 | 1024 | -0.923 | -0.875 | 0.048 |
|  | 3 | 100 | 10.202 | 351 | -1.920 | -2.152 | -0.232 |
|  | 3 | 100 | 12.762 | 156 | -2.300 | -2.579 | -0.279 |
|  | 5 | 100 | 1.464 | 1063 | -0.983 | -1.067 | -0.084 |
| 3 | 1 | 50 | 0.288 | 540 | -0.826 | -0.915 | -0.089 |
|  | 1 | 100 | 1.360 | 471 | -1.072 | -1.213 | -0.141 |
|  | 1 | 98 | 9.067 | 277 | -1.478 | -1.562 | -0.084 |
|  | 2 | 50 | 0.150 | 893 | -0.559 | -0.321 | 0.238 |
|  | 2 | 89 | 0.378 | 758 | -1.084 | -0.862 | 0.222 |
|  | 3 | 100 | 1.447 | 991 | -0.964 | -0.932 | 0.032 |
|  | 3 | 100 | 9.867 | 367 | -2.220 | -2.117 | 0.103 |
|  | 4 | 100 | 1.520 | 1255 | -0.823 | -0.761 | 0.062 |

Figure 4.2
Observed ITC Differences vs. Soluble Boron Concentration


Table 4.14
Statistical Analysis of ITC Differences

Normality Test
Test value ( $D^{\prime}$ ).
Critical Values*
111.9

Result
Normal
Sample Size
Degree of Freedom
$k_{95 / 95}$
$\mathrm{k}_{95 / 95}$ * S 0.24
Bias 0.05
95/95 Tolerance Limit 0.05士0.24 I
I
||

* Level of significance $(\alpha)=0.05$


### 4.3 POWER COEFFICIENT

The power coefficient is defined as the change in reactivity due to a change in the core power level. SIMULATE-3 power coefficient predictions were compared with measurements from early cycles of SONGS 2 and 3, summarized in Table 4.15. The differences are given in absolute terms, (Calculated - Measured).

Due to the limited size of the database, a meaningful 95/95 tolerance limit could not be derived. However, all of the differences are within $0.2 \times 10^{-4} \Delta \mathrm{k} / \mathrm{k} / \% \mathrm{P}$, and the sample mean and standard deviation are 0.03 and 0.09 , respectively. Since the differences include both the calculational and the measurement uncertainties, a conservative 95/95 tolerance limit of $0.2 \times 10^{-4}$ $\Delta k / k / \% \mathrm{P}$ can be assumed based on engineering judgment.

Table 4.15
Comparison of Measured and Calculated Power Coefficients

| UNIT | CYCLE | $\begin{gathered} \text { POWER } \\ \vdots \\ \hline \end{gathered}$ | $\begin{gathered} \text { BURNUP } \\ \text { MWD/T } \end{gathered}$ | $\begin{gathered} \text { BORON } \\ \text { PPM } \\ \hline \end{gathered}$ | COEFFICIENT ( $10^{-4} \Delta \mathrm{k} / \mathrm{k} / \% \mathrm{P}$ ) |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | MEASURED | CALCULATED | DIFF. |
| 2 | 1 | 50 | 539 | 559 | -1.104 | -1.124 | -0.020 |
| 2 | 1 | 80 | 1250 | 512 | -0.946 | -0.981 | -0.035 |
| 2 | 1 | 100 | 2050 | 483 | -0.947 | -0.879 | 0.068 |
| 2 | 2 | 98 | 208 | 818 | -0.990 | -0.911 | 0.079 |
| 2 | 3 | 100 | 380 | 1095 | -1.103 | -0.907 | 0.196 |
| 3 | 1 | 50 | 288 | 540 | -1.041 | -1.119 | -0.078 |
| 3 | 1 | 100 | 1360 | 471 | -0.893 | -0.893 | -0.000 |
|  |  |  |  |  |  | Mean | 0.030 |
|  |  |  |  |  | andard De | iation | 0.092 |

### 4.4 CONTROL ROD WORTH

SIMULATE-3's predictions for control rod worth were compared to the zero-power startup measurements from SONGS 1, 2, and 3.

Tables 4.16 through 4.19 list the measured and the calculated control rod worths with the differences (in percent) for beginning-of-cycle, zero power, nominal and off-nominal cases. The differences are plotted in Figure 4.3. Two cases have very small measured rod worths (less than $0.03 \% \Delta \mathrm{~K} / \mathrm{K}$ ). These two cases (Cases 1 and 4 in Table 4.19) were excluded from the statistical analysis to avoid skewing.

A statistical analysis was performed on the control rod worth differences. The analysis determined the bias, standard deviation, and the normality of the difference distribution. The results are summarized in Table 4.20. The bias and standard deviation are $1.18 \%$ and $4.89 \%$, respectively.

The uncertainty ( $\mathrm{S}_{\mathrm{OBs}}$ ) has two components: the measurement uncertainty $\left(S_{M}\right)$, and the calculational uncertainty $\left(S_{C}\right)$. These two components are related to the observed uncertainty by,

$$
S_{\mathrm{OBS}}^{2}=S_{M}^{2}+S_{C}^{2}
$$

(Eq. 4.4.1)
The measurement uncertainty can be quantified by comparing the measured control rod worths from the initial startup of SONGS 2 and 3. Since these two units are duplicate plants (identical fuel management, enrichments, burnable absorber worth, etc., ) one would expect the measured control rod worths at the beginning of the first cycle to be exactly the same. Therefore, the observed difference in SONGS 2 and 3 measurements can be attributable to the measurement uncertainty. Table 4.21 presents the comparison for a total of seven rod worth measurements. The standard deviation ( $S_{D}$ ) of the difference in the measured rod worths, which includes measurement uncertainties from two measurements, is four percent. Therefore, the net measurement uncertainty can be calculated:

$$
\begin{equation*}
S_{M}^{2}=1 / 2 * S_{D}^{2}=8.00 \% \tag{Eq.4.4.2}
\end{equation*}
$$

Once the measurement uncertainty is quantified, the control rod worth calculational uncertainty can be calculated:

$$
\begin{aligned}
S_{C} & =\left(S_{O B S}^{2}-S_{M}^{2}\right)^{1 / 2} \\
& =\left((4.89)^{2}-(8.00)\right)^{1 / 2} \\
& =3.99(\%)
\end{aligned}
$$

Finally, the 95/95 reliability factor for the calculational error can be calculated:

$$
\text { Reliability Factor }=\mathrm{K}_{95 / 95} * \mathrm{~S}_{\mathrm{c}}
$$

(Eq. 4.4.5)
$\mathrm{K}_{95 / 95}$ is the critical factor associated with the sample size of 54. From Reference 16, the critical value has been found to be 2.046. Substituting the appropriate values into the above formula, as shown in Table 4.22, the $95 / 95$ tolerance limit (bias $\pm$ reliability factor) becomes $-1.2 \pm 8.2 \%$.

The tolerance limit will be applied to the SIMULATE-3 calculation of CEA worth at all power and moderator temperature conditions by,

Predicted CEA Worth $=$ (Calculated CEA Worth) *

$$
(1-\operatorname{Bias} \pm \mathrm{R} \cdot \mathrm{~F} .)
$$

(Eq. 4.4.6)

## SONGS 1 Control Rod Worth Comparison

## Cycle Case

1 150F BANK 2
150F BANK 1
HZP, BANK 2 HZP, BANK 1

2 BANK 2
SHUTDOWN BANK
3. BANK 2

BANK 1
4 BANK 2
BANK 1
6 BANK 2

Reactivity Worth Measured Calculated

Diff. (\%)
1.999
1.918
$-4.23$
1.484
1.436
-3. 34
2.504
2.375
$-5.43$
2.001
1.846
$-8.40$
2.103
3.394
2.008
$-4.73$
3.156
$-7.54$
2.465
1.378
2.369
1.373
$-4.05$
2.113
$-6.72$
2.255
1.554
2.123
1.441
$-7.84$
1.72

## Case List

Reactivity worth
Measured calculated

Diff. (\%)

Cycle 1
A. CEA Banks Sequentially Inserted :

| 1. Bank 6 Worth |  | 0.411 | 0.395 | -4.05 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 2. Bank 5 Worth | 0.383 | 0.370 | -3.51 |  |
| 3. Bank 4 Worth |  | 0.928 | 0.892 | -4.04 |
| 4. Bank 3 Worth |  | 1.029 | 0.976 | -5.43 |
| 5. Bank 2 Worth |  | 0.662 | 0.638 | -3.76 |
| 6. Bank 1 Worth |  | 1.203 | 1.197 | -0.50 |
| 7. Bank B Worth (Banks 6-1 \& P in) | 3.143 | 3.020 | -4.07 |  |

B. Other CEA worth :
8. Bank P Worth (Other Rods Out)
0.211
0.196
$-7.65$
9. Bank P Worth (Banks 6-1 In)
$0.390 \quad 0.353 \quad-10.48$
10. Center CEA (2-1) Worth, Other Rods Out

Cycle 2
A. CEA Banks Sequentially Inserted :
11. Bank 6 Worth

| 0.315 | 0.320 | 1.56 |
| :--- | :--- | :--- |
| 0.275 | 0.279 | 1.43 |
| 0.542 | 0.562 | 3.56 |
| 0.950 | 0.986 | 3.65 |
| 0.450 | 0.453 | 0.66 |
| 0.819 | 0.852 | 3.87 |
| 1.395 | 1.424 | 2.04 |

Cycle 3
18. Bank B Worth, Other Rods Out $1.608 \quad 1.705 \quad 5.69$

## Cycle 4

19. Bank B Worth, Other Rods Out $\quad 1.899 \quad 2.052 \quad 7.46$

Table 4.18
SONGS 3 Control Rod Worth Comparison

## Case List

## Reactivity Worth

 Measured CalculatedDiff. (\%)

## Cycle 1

A. CEA Banks Sequentially Inserted :

| 1. Bank 6 Worth | 0.392 | 0.397 | 1.26 |
| :--- | :--- | :--- | ---: |
| 2. Bank 5 Worth | 0.385 | 0.370 | -4.05 |
| 3. Bank 4 Worth | 0.894 | 0.892 | -0.22 |
| 4. Bank 3 Worth | 1.054 | 0.978 | -7.77 |
| 5. Bank 2 Worth | 0.698 | 0.636 | -9.75 |
| 6. Bank 1 Worth | 1.213 | 1.198 | -1.25 |
| 7. Bank P in, Other Rods Out | 0.200 | 0.195 | -2.56 |
| 8. Center CEA(2-1) Worth, | 0.089 | 0.089 | 0.00 |
| Other Rods Out |  |  |  |

Cycle 2
9. Bank 3 Worth, Other Rods Out 10. Bank B Worth, Other Rods Out
0.686
0.709
3.24
2.183
2.227
1.98

## Cycle 3

| 11. Bank B Worth, Other Rods Out | 1.605 | 1.695 | 5.31 |
| :--- | :--- | :--- | :--- |
| 12. Bank 1 Worth, | 0.416 | 0.440 | 5.45 |
| 13. Bank 4 Worth, | 0.683 | 0.726 | 5.92 |

SONGS - 3 Cycle 4

| 14 | Bank 6 Worth | 0.268 | 0.284 | 5.63 |
| :--- | :--- | :--- | ---: | ---: |
| 15. Bank 5 Worth | 0.410 | 0.430 | 4.65 |  |
| 16. Bank 4 Worth | 0.680 | 0.706 | 3.68 |  |
| 17. Bank 3 Worth | 0.760 | 0.783 | 2.94 |  |
| 18. Bank 2 Worth | 0.980 | 0.995 | 1.51 |  |
| 19. Bank 1 Worth | 0.345 | 0.325 | -6.15 |  |

## Table 4.19 <br> Control Rod Worths for Off-Nominal conditions

(SONGS 2 Cycle 1)

Case List
A. Hot Zero Power Dropped Rod Worth

| 1. Worst PLCEA $($ CEA $P-30)$ | 0.028 | 0.024 | -16.67 |
| :--- | :--- | :--- | :--- | ---: |
| 2. Worst SUBGP (CEA P-1) | 0.108 | 0.109 | 0.92 |

B. Hot Zero Power Ejected Rod Worth

| 3. From ZPDIL (CEA 5-45) | 0.257 | 0.259 | 0.77 |
| :--- | :--- | :--- | :--- |
| (Banks 3 at $47 \%$ ) |  |  |  |
| 4. From FPDIL (CEA 6-20) |  |  |  |
| (Bank 6 at 71\%) | 0.014 | 0.014 | 0.00 |

C. Cold Zero Power - Inlet temperature 320 F System Pressure 600 psi
5. Rod Group 6 Worth
0.230
0.218
$-5.51$
6. Rod Group 5 Worth
0.270
0.247 -9.31
7. Rod Group 4 Worth
0.616
0.608
$-1.32$

Figure 4.3
Relative Control Rod Worth Differences vs. the Measured Worth


Table 4.20
Statistical Analysis of the Observed Control Rod Worth Differences

|  | \%Worth |
| :--- | ---: |
| Mean | -1.18 |
| Standard Deviation (S) | 4.89 |
| RMS | 4.99 |

Normality Test Test Value ( ${ }^{\prime}$ ) Critical Values* 113.0 Result 107.5, 113.7 Normal

| Sample Size | 54 |
| :--- | :---: |
| Degree Of Freedom | 53 |
| $\mathrm{k}_{95 / 95}$ | 2.046 |

* Level of significance $(\alpha)=0.05$


## Table 4.21

## SONGS 2 and 3

Measured Control Rod Worths in Cycle 1

SONGS 2
 6 5 4
3
2
1
P

SONGS 3

| Boron <br> (PPM) | Rod Worth <br> $(\%)$ | Difference <br> (PERCENT) |
| :---: | :---: | ---: |
| 823 | 0.392 | 4.62 |
| 794 | 0.385 | -0.52 |
| 766 | 0.894 | 3.66 |
| 701 | 1.054 | -2.43 |
| 624 | 0.698 | -5.44 |
| 573 | 1.213 | -0.83 |
| 823 | 0.200 | 5.21 |
|  |  |  |
|  | MEAN (\%) | 0.61 |
|  | RMS (\%) | 3.75 |
|  | S.D. (\%) | 3.99 |

Observed Mean ..... $-1.18$
Observed S ..... 4.89
Observed RMS ..... 4.95
Normality TestTest Value ( $\mathrm{D}^{\prime}$ )Critical Values*Result
Measurement error
Observed $S_{D}$ ..... 3.99
Measurement $S_{M}$ ..... 2.83
Model $S_{c}$ ..... 3.99
Sample Size ..... 54
Degree Of Freedom ..... 53
k $\mathbf{k S / 9 5}^{\prime}$ ..... 2.046
$k_{95 / 95} * S_{C}$

$$
8.16
$$

95/95 Tolerance Limit (Rounded)

$$
-1.2
$$

$-1.2 \pm 8.2$
113.0

$$
107.5, \quad 113.7
$$ Normal

[^0]
### 4.5 NET ( $\mathrm{N}-1$ ) ROD WORTH

The net ( $\mathrm{N}-1$ ) rod worth is defined as the reactivity worth of the insertion of all of the control rods except the most reactive rod, which remains stuck out. Due to the intense peaking in the assembly in which the stuck control rod is located, this configuration represents the most severe challenge to any reactor physics method.

SIMULATE-3 capabilities in predicting the net rod worth and the worst stuck rod worth are verified in this section by simulating the measurement performed during the initial startup of Arkansas Nuclear One - Unit 2 (ANO-2). ANO-2 is a Combustion Engineering PWR owned by the Arkansas Power And Light Company. As has been described in Section 3, the basic parameters of this reactor are very similar to those of SONGS 2 and 3. The worst stuck rod was CEA A-52 as identified in Figure 3.7.

Table 4.23 lists the comparison of the SIMULATE-3 calculated All-Rods-In (ARI), Net ( $N-1$ ), and the worst (most reactive) stuck rod worth with the measurement. The agreement is good, and the observed differences for these cases are all within the 95/95 tolerance limits of $-9.4 \%$ and $+7.0 \%$, as established in the control rod worth comparison in Section 4.4. Therefore, it is concluded that the $95 / 95$ tolerance limit for the control rod worth (Section 4.4) is applicable to the net ( $\mathrm{N}-1$ ) worth also.

Table 4.23

## ANO-2 Net (N-1) Rod Worth Comparison

| Case | Measured |  | Calculated |  |
| :--- | :---: | :---: | :---: | :---: |
| ARI Worth | 12.188 | 11.587 | -5.19 |  |
| Net (N-1) Worth | 10.666 | 10.177 | -4.80 |  |
| Worst Stuck Rod Worth | 1.522 | 1.410 | -7.94 |  |

### 4.6 INVERSE BORON WORTH

This section compares the SIMULATE-3 Inverse Boron Worths (IBW) to the SONGS 1, 2, and 3 measurements. The 95/95 tolerance limit for the IBW using the SIMULATE-3 methodology is also derived.

The IBW is calculated using:

$$
\text { IBW }=-\left(\mathrm{CBC}_{1}-\mathrm{CBC}_{2}\right) /(\text { (AReactivity }) \quad(\text { Eq. 4.6.1) }
$$

where,
$C B C_{1}$ is the critical boron concentration for state-point \#1,
$C B C_{2}$ is the critical boron concentration for state-point \#2,
$\Delta$ Reactivity is the required reactivity change ( $\% \Delta k / k$ ) to go from state-point \#1 to \#2. Normally, this reactivity change is accomplished by control rod insertion/withdrawal.

Table 4.24 compares the calculated IBWs with measurements at BOC, zero-power conditions, for a total of 16 measurements from 14 cycles of operations. The differences are all within $10 \%$. The mean and standard deviation are $2.5 \%$ and $5.6 \%$, respectively.

The differences include both the calculational and measurement uncertainties. The measurement uncertainty, which includes boron titration errors and control rod worth measurement errors, could not be quantified due to the insufficient number of duplicate IBW measurements at SONGS 2 and 3. A realistic estimate of the 95/95 tolerance limit associated with the SIMULATE-3 prediction of IBW was not possible. Therefore, an alternative method was used to quantify the reliability factor (RF).

Equation 4.6.1 relates the IBW to the calculated rod worth and CBCs for the two state-points. Assuming that all three variables $\left(C B C_{1}, C B C_{2}\right.$, and rod worth) are independent estimates, the IBW error can be calculated using:

$$
(\text { R. F. })_{\text {IBW }}=\left((\text { R. F. })_{C B C 1}^{2}+(R \cdot F \cdot)_{C B C 2}^{2}+(R \cdot F \cdot)_{C E A}^{2}\right)^{1 / 2}(\text { Eq. } 4 \cdot 6 \cdot 2)
$$

Where,
(R. F.) ${ }_{c B c}$ is the critical boron concentration reliability
factor in percent
(R. F.) ${ }_{\text {ceA }}$ is the control rod worth reliability factor in
percent

Using Table 4.1, a $95 / 95$ reliability factor of $3.1 \%$ for the relative (percent) uncertainty in the calculation of the critical boron concentration was derived. In Section 4.4, the 95/95 reliability factor for the control rod worth was found to be 8.2\%. Substituting these two values into Eq. 4.6.2, a 95/95 reliability factor of $9.3 \%$ was calculated. For conservatism, this reliability factor was rounded to $10 \%$. The conservatism of this $10 \%$ reliability factor was corroborated by the fact that all of the IBW differences listed in Table 4.24 were within $10 \%$.

Unit Cycle Tmod ( $\left.{ }^{\circ} \mathrm{F}\right) \quad$\begin{tabular}{c}
IBW (PPM/ $\% \Delta \mathrm{~K} / \mathrm{k})$

 

Difference
\end{tabular}

| 1 | 1 | 150 | 101 | 112 | 9.8 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 535 | 129 | 141 | 8.5 |
|  | 2 | 535 | 135 | 148 | 8.8 |
|  | 3 | 535 | 152 | 156 | 2.6 |
|  | 4 | 535 | 156 | 158 | 1.3 |
|  | 5 | 535 | 162 | 158 | -2.5 |
|  | 6 | 535 | 162 | 158 | -2.5 |
| 2 | 1 | 320 | -65 | -69 | 6.0 |
|  | 1 | 545 | -72 | -79 | 8.6 |
|  | 2 | 545 | -94 | -94 | 0.1 |
|  | 3 | 545 | -123 | -112 | -9.9 |
|  | 4 | 545 | -126 | -124 | -1.7 |
| 3 | 1 | 545 | -73 | -79 | 7.0 |
|  | 2 | 545 | -95 | -93 | -1.3 |
|  | 3 | 545 | -113 | -112 | -1.2 |
|  | 4 | 545 | -118 | -125 | 5.4 |
|  |  |  |  | Mean | 2.5 |
|  |  |  |  | S | 5.6 |
|  |  |  |  | RMS | 6.0 |

### 4.7 ASSEMBLY POWER DISTRIBUTION

The SIMULATE-3 assembly power distribution predictions were verified. The calculated radial and axial power distributions and the calculated rhodium incore detector signals were compared to measurements from Cycles 1 through 4 of SONGS 2 and 3.

SONGS 2 and 3 are equipped with fixed rhodium incore detector systems consisting of 56 strings of detectors. Each string has five detectors of 40 cm in length, centered at axial core heights of $10 \%, 30 \%, 50 \%, 70 \%$, and $90 \%$, respectively. The core power distribution is measured by first taking a snapshot of the detector signals. A snapshot contains signals for all of the detectors at the specific moment. Signals in the snapshot are then corrected for sensitivity depletion and background effects. Finally, a computer program, CECOR (Reference 14), is executed to determine the core power distribution based on the sensitivity and background corrected signals and pre-calculated assembly coupling coefficients and axial boundary conditions.

Section 4.7.1 compares the SIMULATE-3 calculated radial and axial power distributions with CECOR measurements.

Section 4.7.2 details the comparison of the axial offsets for the snapshots used in the axial power distribution comparison in Section 4.7.1. The 95/95 tolerance limit is also derived.

Section 4.7.3 compares the calculated rhodium detector signals with measurements from detector snapshots. Since the detector signals are the true measured quantities, results from these comparisons are also used in the derivation of $95 / 95$ tolerance limits for assembly/nodal peaking factors.

### 4.7.1 RADIAL AND AXIAL POWER DISTRIBUTIONS

Figures 4.4 to 4.15 compare the SIMULATE-3 axially integrated, quarter core assembly power distributions to CECOR measurements from SONGS 2 Cycles 1 through 4 and SONGS 3 Cycle 3 with burnups close to BOC, MOC, and EOC. These measurements were taken close to Hot-Full-Power and All-Rods-Out conditions. Exact power levels and burnup values are shown in the figures. The CECOR powers shown in these figures are average values from quarter core symmetric locations.

The comparisons demonstrate that the SIMULATE-3 assembly powers agree very well with the CECOR measured powers. The RMS error listed in Table 4.25 for each case is within 0.020 (absolute difference).

Figures 4.16 to 4.27 compare the core average axial power distribution for the corresponding snapshots presented in the assembly power comparison. The 51-node SIMULATE-3 axial powers were derived from the spline-fitting of the 20 -node SIMULATE-3 solution. The SIMULATE-3 results agree well with the CECOR measurements. The RMS values of differences, (Calculated Measured), are well below 0.05 (absolute difference). For those state-points with RMS error greater than 0.02 , the two power distributions agree very well except in the top 5\% and bottom 5\% axial zones of the core. Since the CECOR powers in these regions are inferred using pre-calculated extrapolation distances, one would expect the "measured" CECOR powers to be less accurate. In fact, when these two regions are removed from the comparison, the RMS errors all drop below 0.02. Table 4.25 summarizes the RMS errors for core axial power distributions in the axial region from 5\% to 95\% core height.

The excellent agreement between SIMULATE-3 and CECOR results demonstrates the ability of the SIMULATE-3 methodology to predict the assembly power distribution accurately. Therefore, the SIMULATE-3 computer program can be used to generate representative power distributions of the reactor core for use in the statistical evaluation of overall uncertainties associated with safety system setpoints as per Reference 17.

Figure 4.4 Axially Integrated Radial Power Density - S2C1F026


Figure 4.5 Axially Integrated Radial Power Density - S2C1F038


Figure 4.6 Axially Integrated Radial Power Density - S2C2F051


Figure 4.7 Axially Integrated Radial Power Density - S2C2F055

Date $=09 / 11 / 85$
Power Level $=100.1 \%$
Burnup $=4970 . \mathrm{NWd} / \mathrm{T}$
Absolute Difference
RMS Error $=0.010$
Max Positive Error $=0.022$
Box $=6$
Max Negative Error $=-0.026$ Box $=24$


Figure 4.8 Axially Integrated Radial Power Density - S2C3F005


Figure 4.9 Axially Integrated Radial Power Density - S2C3F027

Date $=02 / 25 / 87$
Power Level $=99.1 \%$
Burnup $=8746 . \mathrm{MWd} / T$
Absolute Difference
RMS Error $=0.013$
Max Positive Error $=0.035$
Box $=44$
Mox Negative Error $=-0.023$

$$
\text { Box }=3
$$

Figure 4.10 Axially Integrated Radial Power Density - S2C3F048


Figure 4.11 Axially Integrated Radial Power Density - S2C4F007

Daie $=2 / 17 / 88$
Power Level $=99.9 \%$
Burnup $=2214 . \mathrm{MWd} / \mathrm{T}$
Absolute Difference
RMS Error $=0.019$
Max Positive Error $=0.032$
Box $=7$
Max Negative Error $=-0.054$
Box $=60$


Figure 4.12 Axially Integrated Radial Power Density - S2C4F042

$$
\text { Date }=10 / 31 / 88
$$

Power Level $=99.1 \%$
Burnup $=10983 . \mathrm{MWd} / \mathrm{T}$
Absolute Difference RMS Error $=0.010$
Max Positive Error $=0.020$

$$
\text { Box }=18
$$

Mox Negative Error $=-0.024$

$$
80 x=61
$$

| CECOR |
| :--- |
| CECOR SIMULATE- 3 |

Figure 4.13 Axially Integrated Radial Power Density - S3C3F011


Figure 4.14 Axially Integrated Radial Power Density - S3C3F026


Figure 4.15 Axially Integrated Radial Power Density - S3C3F044

Date $=03 / 23 / 88$
Power Level $=99.8 \%$
Burnup $=12974$. MWd $/ T$
Absolute Difference
RMS Error $=0.012$
Mox Positive Error $=0.027$
Box $=44$
Max Negative Error $=-0.025$

## Box $=1$

|  |  |  |
| :--- | ---: | ---: |
| CECOR |  |  |
| CECOR - SINULATE-3 | 0.689 | $0.841^{2}$ |


|  |  | $\begin{gathered} 0.792^{14} \\ 0.018 \end{gathered}$ | $\begin{aligned} & 1.129^{15} \\ & 0.009 \end{aligned}$ | $\begin{aligned} & 1.139^{16} \\ & 0.009 \end{aligned}$ | $\begin{aligned} & 17 \\ & 1.264 \\ & 0.004 \end{aligned}$ | $\begin{aligned} & 18 \\ & 0.956 \\ & 0.004 \end{aligned}$ | $\begin{aligned} & 1.273^{19} \\ & 0.005 \end{aligned}$ | $1.063^{20}$ $0.009^{20}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{array}{r} { }^{21} \\ 0.674 \\ -0.022 \end{array}$ | $\begin{aligned} & { }^{22} \\ & 0.994^{2} \\ & 0.006 \end{aligned}$ | $1.133^{23}$ | $0.922^{24}$ 0.004 | 0.995 ${ }^{25}$ | $1.273^{26}$ 0.009 | $\begin{aligned} & { }^{27} \\ & 0.966^{27} \\ & 0.012 \end{aligned}$ | $\begin{aligned} & 1.309^{28} \\ & 0.007^{28} \end{aligned}$ |
|  | $\begin{aligned} & 0.877^{29} \\ & -0.019 \end{aligned}$ | $\begin{aligned} & { }^{30} \\ & 0.849^{30} \\ & 0.002 \end{aligned}$ | $1.261^{31} 0.002{ }^{3}$ | $\begin{aligned} & 0.992^{32} \\ & 0.002 \end{aligned}$ | $0.92{ }^{33}$ | $1.131^{34}$ | 1.115 0.014 | $\begin{aligned} & 38 \\ & 0.961 \\ & 0.019 \end{aligned}$ |
| $0.690^{45}$ | $1.049^{37}$ | $1.065^{38}$ | $\begin{aligned} & 0.955^{39} \\ & 0.003 \end{aligned}$ | $\begin{aligned} & 1.269^{40} \\ & 0.007 \end{aligned}$ | $\begin{aligned} & 1.130 \\ & 0.008 \end{aligned}$ | $0.897^{42}$ 0.007 | $1.109^{43}$ 0.009 | $1.223^{44}$ 0.027 |
| $-0.024$ | $991{ }^{46}$ | 934 ${ }^{47}$ | $71^{18}$ | $0.961{ }^{49}$ | $1.113^{50}$ | $1.110^{51}$ | $0.840^{32}$ | $0.822^{53}$ |
| $0.841^{54}$ | 0.000 | 0.001 | 0.003 | $0.007$ | $0.015$ | $0.011$ | $0.003$ | $0.020$ |
| $\begin{array}{r}0.841 \\ -0.024 \\ \hline\end{array}$ | ${ }^{55}$ | $1.245^{56}$ | $1.069^{57}$ | $1.314^{58}$ | $0.59{ }^{59}$ | $1.203^{60}$ | $0.79{ }^{61}$ | 0.708 |
|  |  |  |  |  |  | 0.007 | -0.009 | -0.014 |

Figure 4.16 Core Average Axial Power Distribution - S2C1F026


Figure 4.17 Core Average Axial Power Distribution - S2C1F038


Figure 4.18 Core Average Axial Power Distribution - S2C2F051


Figure 4.19 Core Average Axial Power Distribution - S2C2F055


Figure 4.20 Core Average Axial Power Distribution - S2C3F005


Figure 4.21 Core Average Axial Power Distribution - S2C3F027


Figure 4.22 Core Average Axial Power Distribution - S2C3F048


Figure 4.23 Core Average Axial Power Distribution - S2C4F007


Figure 4.24 Core Average Axial Power Distribution - S2C4F042


Figure 4.25 Core Average Axial Power Distribution - S3C3F011


Figure 4.26 Core Average Axial Power Distribution - S3C3F026


Figure 4.27 Core Average Axial Power Distribution - S3C3F044


| SNAPSHOT ID | RADIAL <br> RMS ERROR |
| :--- | :---: |
| S2C1F026 | 0.008 |
| S2C1F038 | 0.008 |
| S2C2F051 | 0.011 |
| S2C2F055 | 0.010 |
| S2C3F005 | 0.012 |
| S2C3F027 | 0.013 |
| S2C3F048 | 0.013 |
| S2C4F007 | 0.019 |
| S2C4F042 | 0.010 |
| S3C3F011 | 0.011 |
| S3C3F026 | 0.011 |
| S3C3F044 | 0.012 |

AXIAL
RMS ERROR
0.0177
0.0127
0.0195
0.0157
0.0126
0.0108
0.0133
0.0154
0.0182
0.0160
0.0135
0.0151

### 4.7.2 AXIAL OFFSET

Table 4.26 compares the axial offset, as defined in Eq. 4.7.1, for the axial power distributions shown in Figures 4.16 through 4.27. Altogether, 12 measurements from five cycles of operation were compared.

$$
\text { Axial Offset }=\left(P_{T}-P_{B}\right) /\left(P_{T}+P_{B}\right)
$$

(Eq. 4.7.1)

$$
\begin{aligned}
& P_{T}=\text { Power in the top half of the core, and } \\
& P_{B}=\text { Power in the bottom half of the core. }
\end{aligned}
$$

As summarized in Table 4.26 , the mean and the standard deviation for the differences, (Calculated - Measured), are -0.003 and 0.005 , respectively. The maximum difference is -0.011 .

The 95/95 reliability factor for the calculation of the axial offset is determined using:

$$
\begin{aligned}
\text { Reliability Factor } & =\mathrm{K}_{95 / 95} * \text { (Standard Deviation) } \\
& =\mathrm{K}_{95 / 95} * 0.005
\end{aligned}
$$

From Reference 16 , the critical factor, $\mathrm{K}_{95 / 95}$, for the sample size of 12 is 2.736 . Using this value, the $95 / 95$ reliability factor becomes 0.014 .

The mean and the reliability factor are applied to the SIMULATE-3 calculation of the axial offset using:
$\begin{aligned} \text { Predicted Axial Offset }= & \text { (Calculated Axial Offset) * } \\ & (1-\text { Bias } \pm \text { Reliability Factor })\end{aligned}$
(Eq. 4.7.3)

Table 4.26

## Axial Offset Comparison

| Axial Offset |  |  | Difference |
| :---: | :---: | :---: | :---: |
| S2C1F026 | -0.028 | -0.025 | 0.003 |
| S2C1F038 | 0.008 | 0.005 | -0.003 |
| S2C2F051 | 0.001 | -0.010 | -0.011 |
| S2C2F055 | -0.004 | -0.009 | -0.005 |
| S2C3F005 | -0.008 | -0.013 | -0.005 |
| S2C3F027 | -0.020 | -0.018 | 0.002 |
| S2C3F048 | -0.021 | -0.024 | -0.003 |
| S2C4F007 | -0.001 | -0.004 | -0.004 |
| S2C4F042 | -0.022 | -0.013 | 0.008 |
| S3C3F011 | -0.007 | -0.014 | -0.007 |
| S3C3F026 | -0.020 | -0.021 | -0.001 |
| S3C3F044 | -0.015 | -0.021 | -0.007 |
|  |  | $\begin{aligned} & \text { Mean } \\ & \mathrm{S} \end{aligned}$ | $\begin{array}{r} -0.003 \\ 0.005 \end{array}$ |

This section compares the SIMULATE-3 predicted rhodium detector reaction rates with the measured rhodium detector signals for SONGS 2 and 3. Also, the 95/95 tolerance limits were derived for the following assembly peaking factors: $F_{X Y}^{S}$ - planar peak power, $F_{Q}^{S}$ - overall peak power, and $F_{R}^{S}$ - radial power sharing ( $F_{\Delta H}^{S}$ ).

Seventy-two incore detector snapshots taken close to All-Rods-Out and Hot-Full-Power conditions from Cycles 1 through 4 of SONGS 2 and 3 were used. Tables 4.27 and 4.28 summarize the conditions of these snapshots.

The detector comparison was performed in the following manner:

1. Corrected each measured detector signal for self-shielding effects based on the fraction of rhodium atoms remaining.
2. Determined Overall peak power ( $\mathrm{F}_{\mathrm{Q}}^{\mathrm{S}}$ ):

At each instrumented location the difference between the SIMULATE-3 calculated signal and the corrected detector signal was found (Calculated - Measured).
3. Determined Assembly power sharing ( $F_{R}^{S}, F_{\Delta \mathrm{B}}^{\mathrm{S}}$ ):

At each instrumented assembly all five levels of the predicted and measured signals were summed up separately, and the difference was found.
4. Determined Planar peak power ( $\mathrm{F}_{\mathrm{XY}}^{\mathrm{S}}$ ):

For each level, the predicted and measured signals were normalized, and the difference at each detector location was calculated.
5. Calculated the mean $(\bar{x})$ and the standard deviation ( $S_{o b s}$ ) for the differences in 2,3 , and 4.
6. The detector measurement uncertainty at any axial level was reflected in the variations in the detector signals from symmetric core locations. The measurement uncertainty was estimated using:

$$
\begin{align*}
& S_{\text {meas }}^{2}(l)=\left(1 . /\left(N_{\ell}-1\right)\right) * \\
& \left(\sum_{g} \sum_{k}\left(\left(R_{m}(k, g, \ell)-\overline{R R}_{m}(g, \ell)\right) / \overline{R R}_{m}(g, \ell)\right)^{2}\right. \tag{Eq.4.7.1}
\end{align*}
$$

Where,
$\ell=$ axial detector level index from 1 to 5
$g=$ symmetric detector group index from Table 4.29
$k=$ detector location index within each symmetric group
$\mathrm{N}_{\ell}=$ total number of comparisons in level $\ell$.
$R R_{m}(k, g, \ell)=$ measured individual detector signal
$\overline{\mathrm{RR}}_{\mathrm{m}}(\mathrm{g}, \ell)=$ average signal at level $\ell$ in group $g$
7. Similar to the level-by-level measurement uncertainties, the detector channel (sum of five levels) measurement uncertainty was determined using:

$$
S_{\text {meas }}^{2}=(1 . /(N-1)) *\left(\sum_{g} \sum_{k}\left(\left(R R_{m}(k, g)-\overline{R R}_{m}(g)\right) /{\overline{R R_{m}}}_{m}(g)\right)^{2}\right.
$$

(Eq. 4.7.2)
Where,

$$
\begin{aligned}
& N=\text { total number of detector channels } \\
& \mathrm{RR}_{\mathrm{m}}(k, g)=\text { measured signal in channel } k \text {, group } g \\
& \overline{\mathrm{RR}}_{\mathrm{m}}(g)=\text { average signal in group } g
\end{aligned}
$$

8. Calculated the model uncertainties for planar peak power, overall peak power, and assembly power sharing by subtracting the measurement uncertainties from the variances of the observed differences using:

$$
\begin{equation*}
S_{\text {model }}^{2}=S_{o b s}^{2}-S_{\text {meas }}^{2} \tag{Eq.4.7.3}
\end{equation*}
$$

Using the above procedure, the standard deviations for the snapshots listed in Tables 4.27 and 4.28 were calculated. Tables 4.30 and 4.31 summarize the results, including the assembly power peaking factors. Bartlett's test (Reference 18) was used to determine the poolability of standard deviations from all the snapshots for each reactor unit. Passing the poolability test
snapshots for each reactor unit. Passing the poolability test would allow for the pooling of the comparisons from all of the snapshots into one large sample to take advantage of the combined sample size and the reduced 95/95 (probability/confidence) k -value.

Table 4.3.2 summarizes the parameters used to determine whether the snapshot data could be combined into a single statistical sample. When compared with the critical values from a $\chi^{2}$ distribution, the individual snapshot results cannot be pooled. For conservatism then, the maximum standard deviations were used. Table 4.33 lists the maximum standard deviations for both reactor units.

For the purpose of calculating the relative (\%) uncertainties associated with SIMULATE-3 predictions of peak assembly/nodal powers, the standard deviations can be converted from power fraction (absolute) units to a percentage basis by dividing by the minimum peak assembly power for each reactor unit. Table 4.34 summarizes the maximum standard deviations $S_{F X Y}^{s}, S_{F Q}^{s}, ~ a n d ~ S_{F R}^{s}$ in percent.

The 95/95 tolerance limits for assembly peaking factors ( $F_{X Y}^{S}, F_{Q}^{S}$, and $F_{R}^{S}$ ) were calculated by multiplying the standard deviations listed in Table 4.34 with the k-value corresponding to the size of each sample. Table 4.35 summarizes the $95 / 95$ tolerance limits for the assembly peaking factors. The 95/95 tolerance limits for $\mathrm{F}_{\mathrm{XY}}^{\mathrm{S}}, \mathrm{F}_{\mathrm{Q}}^{\mathrm{S}}$, and $\mathrm{F}_{\mathrm{R}}^{\mathrm{S}}$ are $4.80 \%, 4.17 \%$, and $3.34 \%$, respectively for all power levels and rodded conditions.

| .CYCLE | $\begin{aligned} & \text { SNAPSHOT } \\ & \quad \text { ID } \\ & \hline \end{aligned}$ | DATE | TIME | $\begin{gathered} \text { BURNUP } \\ \text { GWD } / T \end{gathered}$ | POWER $(\%)$ | $\begin{array}{r} \text { BANK } 6 \\ \text { POSITION } \\ \hline \end{array}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | S2C1F011 | 08/30/83 | 10:54:24 | 3.017 | 99.8 | 150.0 |
| 1 | S2C1F014 | 09/20/83 | 11:04:11 | 3.747 | 99.7 | 150.0 |
| 1 | S2C1F026 | 03/08/84 | 05:02:00 | 7.289 | 99.5 | 150.0 |
| 1 | S2C1F034 | 05/17/84 | 14:01:53 | 9.689 | 99.9 | 150.0 |
| 1 | S2C1F037 | 06/08/84 | 15:10:43 | 10.523 | 99.4 | 150.0 |
| 1 | S2C1F038 | 06/13/84 | 15:09:48 | 10.687 | 99.8 | 150.0 |
| 1 | S2C1F039 | 08/01/84 | 10:14:13 | 11.088 | 100.4 | 142.5 |
| 2 | S2C2F046 | 06/24/85 | 18:29:32 | 2.092 | 99.8 | 144.0 |
| 2 | S2C2F051 | 08/08/85 | 14:28:57 | 3.701 | 99.9 | 142.5 |
| 2 | S2C2F053 | 08/28/85 | 09:52:12 | 4.433 | 99.5 | 124.5 |
| 2 | S2C2F055 | 09/11/85 | 16:41:14 | 4.972 | 100.0 | 150.0 |
| 2 | S2C2F064 | 12/14/85 | 08:51:59 | 7.019 | 99.5 | 145.5 |
| 2 | S2C2F067 | 01/02/86 | 14:36:28 | 7.690 | 100.2 | 145.5 |
| 2 | S2C2F069 | 01/23/86 | 09:30:18 | 8.402 | 99.6 | 150.0 |
| 2 | S2C2F077 | 03/12/86 | 13:02:45 | 10.009 | 70.2 | 142.5 |
| 3 | S2C3F005 | 08/22/86 | 09:36:13 | 2.240 | 100.0 | 142.5 |
| 3 | S2C3F012 | 09/10/86 | 10:38:35 | 2.898 | 100.0 | 147.0 |
| 3 | S2C3F021 | 12/17/86 | 02:44:28 | 6.263 | 98.8 | 150.0 |
| 3 | S2C3F027 | 02/18/87 | 08:43:24 | 8.746 | 99.1 | 150.0 |
| 3 | S2C3F034 | 02/25/87 | 08:43:24 | 10.653 | 100.0 | 150.0 |
| 3 | S2C3F035 | 04/22/87 | 08:26:46 | 10.911 | 99.7 | 150.0 |
| 3 | S2C3F040 | 04/29/87 | 08:37:35 | . 12.227 | 99.7 | 142.5 |
| 3 | S2C3F041 | 06/03/87 | 10:28:45 | 12.445 | 100.0 | 150.0 |
| 3 | S2C3F042 | 06/10/87 | 07:17:22 | 12.704 | 100.0 | 150.0 |
| 3 | S2C3F04.7 | 06/17/87 | 07:20:24 | 13.684 | 99.9 | 150.0 |
| 3 | S2C3F048 | 07/15/87 | 07:54:08 | 13.943 | 99.8 | 150.0 |
| 4 | S2C4F001 | 07/29/87 | 09:37:12 | 0.471 | 99.2 | 150.0 |
| 4 | S2C4F005 | 12/31/87 | 10:11:57 | 1.691 | 99.8 | 150.0 |
| 4 | S2C4F007 | 2/3/88 | 10: 6: 5 | 2.214 | 99.9 | 150.0 |
| 4 | S2C4F008 | 2/17/88 | 6:13: 7 | 2.480 | 99.6 | 150.0 |
| 4 | S2C4F010 | 2/29/88 | 14:22:51 | 2.746 | 100.0 | 150.0 |
| 4 | S2C4F012 | 3/ 2/88 | 10:33:16 | 3.273 | 99.4 | 150.0 |
| 4 | S2C4F016 | 4/27/88 | 8:36:27 | 4.347 | 99.8 | 150.0 |
| 4 | S2C4F020 | 5/18/88 | 11: 3:34 | 5.130 | 99.8 | 150.0 |
| 4 | S2C4F024 | 6/15/88 | 8:43:42 | 6.191 | 99.5 | 150.0 |
| 4 | S2C4F025 | 6/22/88 | 5: 0:23 | 6.454 | 99.8 | 150.0 |
| 4 | S2C4F030 | 7/27/88 | 7:49:54 | 7.754 | 99.9 | 150.0 |
| 4 | S2C4F032 | 8/10/88 | 8:42:55 | 8.273 | 99.3 | 150.0 |
| 4 | S2C4F039 | 9/28/88 | 11:36:52 | 10.009 | 99.7 | 150.0 |
| 4 | S2C4F043 | 10/26/88 | 7: 4:13 | 10.983 | 99.1 | 150.0 |

Table 4.28
SONGS 3 Snapshot Information

| CYCLE | $\begin{gathered} \text { SNAPSHOT } \\ \text { ID } \\ \hline \end{gathered}$ | DATE | TIME | BURNUP GWD/T | POWER <br> (\%) | $\begin{array}{r} \text { BANK } 6 \\ \text { POSITION } \end{array}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | S3C1F013 | 05/31/84 | 10:01:17 | 4.051 | 99.8 | 145.5 |
| 1 | S3C1F039 | 05/02/85 | 18:15:47 | 10.736 | 99.4 | 148.5 |
| 2 | S3C2F019 | 05/07/86 | 12:52:37 | 2.779 | 99.5 | 145.5 |
| 2 | S3C2F020 | 05/14/86 | 09:37:58 | 3.035 | 99.9 | 145.5 |
| 2 | S3C2F022 | 05/27/86 | 13:54:17 | 3.531 | 99.6 | 148.5 |
| 2 | S3C2F023 | 06/04/86 | 10:43:12 | 3.829 | 96.8 | 144.0 |
| 2 | S3C2F027 | 07/09/86 | 10:46:46 | 5.122 | 85.1 | 148.5 |
| 2 | S3C2F028 | 07/16/86 | 09:36:08 | 5.305 | 100.0 | 148.5 |
| 2 | S3C2F032 | 08/20/86 | 10:34:18 | 6.433 | 99.7 | 150.0 |
| 2 | S3C2F039 | 11/05/86 | 10:25:17 | 8.167 | 83.6 | 150.0 |
| 2 | S3C2F040 | 11/12/86 | 09:23:21 | 8.411 | 83.2 | 145.5 |
| 2 | S3C2F043 | 12/03/86 | 08:49:41 | 9.029 | 84.3 | 148.5 |
| 2 | S3C2F044 | 12/11/86 | 09:17:27 | 9.319 | 83.6 | 148.5 |
| 2 | S3C2F046 | 12/31/86 | 08:49:49 | 9.913 | 66.4 | 144.0 |
| 3 | S3C3F007 | 05/06/87 | 09:04:16 | 1.963 | 99.8 | 150.0 |
| 3 | S3C3F010 | 06/03/87 | 15:05:13 | 2.981 | 99.8 | 150.0 |
| 3 | S3C3F011 | 06/17/87 | 07:25:59 | 3.481 | 100.2 | 148.5 |
| 3 | S3C3F017 | 08/26/87 | 08:44:32 | 5.801 | 99.9 | 148.5 |
| 3 | S3C3F021 | 09/23/87 | 07:46:15 | 6.911 | 99.5 | 150.0 |
| 3 | S3C3F023 | 10/07/87 | 08:40:11 | 7.884 | 99.4 | 150.0 |
| 3 | S3C3F026 | 11/04/87 | 07:36:17 | 8.398 | 99.8 | 150.0 |
| 3 | S3C3F030 | 12/02/87 | 07:34:13 | 9.431 | 100.0 | 150.0 |
| 3 | S3C3F032 | 12/23/87 | 08:27:08 | 10.373 | 99.7 | 150.0 |
| 3 | S3C3F034 | 01/06/88 | 08:38:42 | 10.891 | 99.8 | 150.0 |
| 3 | S3C3F035 | 01/13/88 | 13:35:31 | 11.527 | 95.3 | 148.5 |
| 3 | S3C3F039 | 02/17/88 | 06:29:10 | 12.043 | 99.8 | 148.5 |
| 3 | S3C3F041 | 03/02/88 | 09:52:15 | 12.455 | 99.6 | 148.5 |
| 3 | S3C3F043 | 03/16/88 | 07:36:58 | 12.963 | 99.9 | 150.0 |
| 3 | S3C3F046 | 04/06/88 | 09:09:44 | 13.497 | 99.7 | 150.0 |
| 4 | S3C4F005 | 9/21/88 | 13: 2:43 | 1.035 | 99.7 | 150.0 |
| 4 | S3C4F006 | 9/28/88 | 13:35: 6 | 1.299 | 99.6 | 150.0 |
| 4 | S3C4F007 | 10/5/88 | 9:10:31 | 1.564 | 99.9 | 150.0 |

$\frac{\text { Group }}{1}$

| Detector |  |  |  |
| :--- | :--- | :--- | :--- |
| Number* |  |  |  |
| 1, | 5, | 52, | 56 |
| 2, | 4, | 53, | 55 |
| 3, | 54, |  |  |
| 6, | 12, | 45, | 51 |
| 7, | 11, | 46, | 50 |
| 8, | 10, | 47, | 49 |
| 9, | 48 |  |  |
| 13, | 19, | 38, | 44 |
| 14, | 18, | 39, | 43 |
| 15, | 17, | 40, | 42 |
| 16, | 41, |  |  |
| 20, | 21, | 36, | 37 |
| 22, | 28, | 29, | 35 |
| 23, | 27, | 30, | 34 |
| 24, | 26, | 31, | 33 |
| 25, | 32 |  |  |

* Detector locations are shown in Figure 3.6

SONGS 2 Incore Detector Statistics

| SNAPSHOT | BURNUP <br> GWD/T | $\begin{aligned} & \text { TOTAL } \\ & \mathrm{S} \\ & \hline \end{aligned}$ | SHARING S DF |  | $\begin{array}{cc} \text { LEVEL } & 5 \\ S \end{array}$ |  | $\begin{array}{cc} \text { LEVEL } \\ S \end{array}$ |  | $\text { LEVEL - } 3$ |  | $\begin{gathered} \text { LEVEL }-2 \\ \mathrm{~S} \end{gathered}$ |  | $\underset{S}{\text { LEVEL }}-\frac{1}{D F}$ |  | RADIAL PEAKING |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| S2C1F011 | 3.017 | 0.0195273 | 0.0039 | 50 | 0.0121 | 55 | 0.0069 | 54 | $\overline{0.0042}$ | 55 | 0.0028 | 55 | 0.0157 | 50 | 1.240 |
| S2C1F014 | 3.747 | 0.0219275 | 0.0036 | 52 | 0.0123 | 55 | 0.0070 | 54 | 0.0032 | 55 | 0.0039 | 55 | 0.0157 | 52 | 1.235 |
| S2C1F026 | 7.289 | 0.0213273 | 0.0055 | 53 | 0.0169 | 54 | 0.0089 | 53 | 0.0086 | 54 | 0.0107 | 54 | 0.0116 | 54 | 1.231 |
| S2C1F034 | 9.689 | 0.0154268 | 0.0060 | 52 | 0.0119 | 53 | 0.0063 | 52 | 0.0089 | 53 | 0.0095 | 53 | 0.0133 | 53 | 1.204 |
| S2C1F037 | 10.523 | 0.0150268 | 0.0062 | 52 | 0.0122 | 53 | 0.0068 | 52 | 0.0097 | 53 | 0.0090 | 53 | 0.0136 | 53 | 1.196 |
| S2C1F038 | 10.687 | 0.0159268 | 0.0067 | 52 | 0.0129 | 53 | 0.0077 | 52 | 0.0097 | 53 | 0.0094 | 53 | 0.0133 | 53 | 1.195 |
| S2C1F039 | 11.088 | 0.0219266 | 0.0048 | 48 | 0.0155 | 53 | 0.0061 | 52 | 0.0072 | 54 | 0.0060 | 53 | 0.0098 | 50 | 1.187 |
| S2C2F046 | 2.092 | 0.0234259 | 0.0152 | 47 | 0.0143 | 51 | 0.0145 | 51 | 0.0130 | 52 | 0.0181 | 51 | 0.0248 | 50 | 1.284 |
| S2C2F051 | 3.701 | 0.0180256 | 0.0086 | 47 | 0.0132 | 51 | 0.0091 | 52 | 0.0085 | 51 | 0.0103 | 50 | 0.0171 | 48 | 1.267 |
| S2C2F053 | 4.433 | 0.0229256 | 0.0079 | 47 | 0.0138 | 51 | 0.0090 | 52 | 0.0087 | 51 | 0.0096 | 50 | 0.0159 | 48 | 1.261 |
| S2C2F055 | 4.972 | 0.0129254 | 0.0076 | 46 | 0.0108 | 51 | 0.0091 | 52 | 0.0066 | 50 | 0.0098 | 50 | 0.0144 | 47 | 1.258 |
| S2C2F064 | 7.019 | 0.0182266 | 0.0087 | 47 | 0.0158 | 52 | 0.0100 | 52 | 0.0089 | 52 | 0.0117 | 54 | 0.0115 | 52 | 1.237 |
| S2C2F067 | 7.690 | 0.0189265 | 0.0090 | 46 | 0.0123 | 51 | 0.0113 | 52 | 0.0102 | 52 | 0.0134 | 54 | 0.0127 | 52 | 1.231 |
| S2C2F069 | 8.402 | 0.0195264 | 0.0095 | 45 | 0.0123 | 50 | 0.0122 | 52 | 0.0109 | 52 | 0.0138 | 54 | 0.0127 | 52 | 1.227 |
| S2C2F077 | 10.009 | 0.0191266 | 0.0130 | 47 | 0.0156 | 52 | 0.0131 | 52 | 0.0133 | 52 | 0.0173 | 54 | 0.0137 | 52 | 1.210 |
| S2C3F005 | 2.240 | 0.0154263 | 0.0083 | 44 | 0.0101 | 52 | 0.0086 | 52 | 0.0054 | 52 | 0.0099 | 54 | 0.0193 | 49 | 1.245 |
| S2C3F012 | 2.898 | 0.0141263 | 0.0078 | 44 | 0.0090 | 52 | 0.0077 | 51 | 0.0052 | 52 | 0.0086 | 54 | 0.0182 | 50 | 1.244 |
| S2C3F021 | 6.263 | 0.0170264 | 0.0073 | 45 | 0.0079 | 52 | 0.0101 | 52 | 0.0091 | 52 | 0.0111 | 54 | 0.0127 | 50 | 1.245 |
| S2C3F027 | 8.746 | 0.0139265 | 0.0098 | 46 | 0.0122 | 52 | 0.0133 | 52 | 0.0115 | 52 | 0.0134 | 54 | 0.0130 | 51 | 1.266 |
| S2C3F034 | 10.653 | 0.0141265 | 0.0105 | 46 | 0.0103 | 52 | 0.0138 | 52 | 0.0122 | 52 | 0.0149 | 54 | 0.0145 | 51 | 1.288 |
| S2C3F035 | 10.911 | 0.0144265 | 0.0109 | 46 | 0.0112 | 52 | 0.0141 | 52 | 0.0123 | 52 | 0.0154 | 54 | 0.0146 | 51 | 1.291 |
| S2C3F040 | 12.227 | 0.0204265 | 0.0122 | 46 | 0.0166 | 52 | 0.0154 | 52 | 0.0128 | 52 | 0.0161 | 54 | 0.0156 | 51 | 1.283 |
| S2C3F041 | 12.445 | 0.0159265 | 0.0120 | 46 | 0.0120 | 52 | 0.0153 | 52 | 0.0132 | 52 | 0.0167 | 54 | 0.0157 | 51 | 1.300 |
| S2C3F042 | 12.704 | 0.0169265 | 0.0120 | 46 | 0.0131 | 52 | 0.0151 | 52 | 0.0128 | 52 | 0.0166 | 54 | 0.0155 | 51 | 1.301 |
| S2C3F047 | 13.684 | 0.0216265 | 0.0129 | 46 | 0.0139 | 52 | 0.0158 | 52 | 0.0137 | 52 | 0.0175 | 54 | 0.0162 | 51 | 1.302 |
| S2C3F048 | 13.943 | 0.0179265 | 0.0130 | 46 | 0.0138 | 52 | 0.0159 | 52 | 0.0140 | 52 | 0.0179 | 54 | 0.0163 | 51 | 1.302 |
| S2C4F001 | 0.471 | 0.0210257 | 0.0175 | 42 | 0.0194 | 49 | 0.0176 | 52 | 0.0160 | 52 | 0.0182 | 52 | 0.0229 | 48 | 1.309 |
| S2C4F005 | 1.691 | 0.0195255 | 0.0166 | 40 | 0.0196 | 49 | 0.0181 | 52 | 0.0127 | 50 | 0.0190 | 52 | 0.0239 | 48 | 1.318 |
| S2C4F007 | 2.214 | 0.0200256 | 0.0185 | 41 | 0.0183 | 49 | 0.0182 | 52 | 0.0158 | 51 | 0.0196 | 52 | 0.0231 | 48 | 1.320 |
| S2C4F008 | 2.480 | 0.0208256 | 0.0188 | 41 | 0.0184 | 49 | 0.0179 | 52 | 0.0165 | 51 | 0.0197 | 52 | 0.0238 | 48 | 1.321 |
| S2C4F010 | 2.746 | 0.0198255 | 0.0166 | 40 | 0.0178 | 49 | 0.0178 | 52 | 0.0132 | 50 | 0.0194 | 52 | 0.0235 | 48 | 1.322 |
| S2C4F012 | 3.273 | 0.0204255 | 0.0158 | 40 | 0.0180 | 49 | 0.0170 | 52 | 0.0134 | 50 | 0.0181 | 52 | 0.0225 | 48 | 1.324 |
| S2C4F016 | 4.347 | 0.0211245 | 0.0154 | 34 | 0.0177 | 48 | 0.0174 | 52 | 0.0138 | 49 | 0.0183 | 50 | 0.0196 | 42 | 1.327 |
| S2C4F020 | 5.130 | 0.0206245 | 0.0152 | 34 | 0.0172 | 48 | 0.0174 | 52 | 0.0139 | 49 | 0.0181 | 50 | 0.0195 | 42 | 1.330 |
| S2C4F024 | 6.191 | 0.0202244 | 0.0152 | 34 | 0.0175 | 48 | 0.0180 | 51 | 0.0142 | 49 | 0.0172 | 50 | 0.0201 | 42 | 1.334 |
| S2C4F025 | 6.454 | 0.0187243 | 0.0151 | 34 | 0.0168 | 48 | 0.0177 | 51 | 0.0135 | 49 | 0.0155 | 49 | 0.0196 | 42 | 1.334 |
| S2C4F030 | 7.754 | 0.0175241 | 0.0130 | 32 | 0.0175 | 48 | 0.0132 | 49 | 0.0147 | 48 | 0.0174 | 50 | 0.0193 | 42 | 1.339 |
| S2C4F032 | 8.273 | 0.0187241 | 0.0128 | 32 | 0.0181 | 48 | 0.0132 | 49 | 0.0143 | 48 | 0.0176 | 50 | 0.0199 | 42 | 1.341 |
| S2C4F039 | 10.009 | 0.0170249 | 0.0126 | 37 | 0.0191 | 49 | 0.0140 | 49 | 0.0126 | 48 | 0.0138 | 52 | 0.0182 | 47 | 1.344 |
| S2C4F043 | 10.983 | 0.0183250 | 0.0133 | 37 | 0.0186 | 49 | 0.0143 | 49 | 0.0136 | 48 | 0.0170 | 53 | 0.0193 | 47 | 1.344 |

$\begin{array}{llllllllllll}0.0187 & 10379 & 0.0116 & 1750 & 0.0149 & 2037 & 0.0134 & 2069 & 0.0117 & 2053 & 0.0147 & 2103\end{array} 0.01741957$

* DF: Degrees-of-Freedom

Table 4.31
SONGS 3 Incore Detector Statistics


DF: Degrees-of-Freedom

Table 4.32
Bartlett's Test Results for Assembly Peaking Factors

SONGS 2

|  | Total | Sharing | Level-5 | Level-4 | Level-3 | Level-2 | Level-1 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| b-value | 447.6 | 528.5 | 192.0 | 412.8 | 413.2 | 512.5 | 208.2 |
| DF* | 39 | 39 | 39 | 39 | 39 | 39 | 39 |
| $\chi_{0.05}^{2}$ | 55.6 | 55.6 | 55.6 | 55.6 | 55.6 | 55.6 | 55.6 |
| Conclusion | Fail | Fail | Fail | Fail | Fail | Fail | Fail |

SONGS 3
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|  | Total | Sharing | Level-5 | Level-4 | Level-3 | Level-2 | Level-1 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| b-value | 487.5 | 380.1 | 384.4 | 745.2 | 386.2 | 354.3 | 250.0 |
| DF* | 31 | 31 | 31 | 31 | 31 | 31 | 31 |
| $\chi_{0.05}^{2}$ | 40.3 | 40.3 | 40.3 | 40.3 | 40.3 | 40.3 | 40.3 |
| Conclusion | Fail | Fail | Fail | Fail | Fail | Fail | Fail |

Table 4.33
The Least Favorable Standard Deviations

## for Assembly Peaking Factors

|  | $\underline{\text { SONGS-2 }}$ | $\underline{\text { SONGS-3 }}$ |
| :--- | :---: | :---: |
| $\mathrm{S}_{\mathrm{FXY}}^{\mathrm{S}}$ | 0.0248 | 0.0280 |
| Degrees-of-Freedom | 50 | 54 |
|  |  |  |
| $\mathrm{~S}_{\mathrm{FQ}}^{\mathrm{S}}$ | 0.0234 | 0.0275 |
| Degrees-of-Freedom | 259 | 258 |
|  |  |  |
| $\mathrm{~S}_{\mathrm{FR}}^{\mathrm{S}}$ | 0.0188 | 0.0190 |
| Degrees-of-Freedom | 41 | 50 |

Table 4.34

## Calculation of Maximum Standard Deviations <br> in Terms of Percent

|  | SONGS-2 | SONGS-3 | MAXIMUM |
| :---: | :---: | :---: | :---: |
| $S_{\text {FXY }}^{\text {S }}$ (Absolute) | 0.0248 | 0.0280 |  |
| Minimum $\mathrm{F}^{\text {R }}$ | 1.187 | 1.194 |  |
| $S_{\text {FXY }}^{\text {S }}$ (\%) | 2.09 | 2.35 | 2.35 |
| Degrees-of-Freedom | 50 | 54 |  |
| $S_{\text {FQ }}^{\text {S }}$ (Absolute) | 0.0234 | 0.0275 |  |
| Minimum $\mathrm{F}_{\mathrm{R}}$ | 1.187 | 1.194 |  |
| $\mathrm{S}_{\mathrm{FQ}}^{\mathrm{S}}$ (\%) | 1.97 | 2.30 | 2.30 |
| Degrees-of-Freedom | 259 | 258 |  |
| $\mathrm{S}_{\mathrm{FR}}^{\mathrm{S}}$ (Absolute) | 0.0188 | 0.0190 |  |
| Minimum $\mathrm{F}_{\mathrm{R}}$ | 1.187 | 1.194 |  |
| $\mathrm{S}_{\mathrm{FR}}^{\mathrm{S}}$ (\%) | 1.58 | 1.59 | 1.59 |
| Degrees-of-Freedom | 41 | 50 |  |

Table 4.35
Calculation of $95 / 95$ Tolerance Limits
for Assembly Power Peaking

## SONGS-2

2.09

50
2.060
4.30
1.97

259
1.812
3.57
4.17
4.17
$S_{\mathrm{FR}}^{\mathrm{S}}$
Degrees-of-Freedom
$\mathrm{K}_{95 / 95}$
$\mathrm{K}_{95 / 95} \mathrm{~S}$ (\%)
1.58

41
2.111
3.34

SONGS-3
2.35

54
2.042
4.80
4.80

$$
2.30
$$

$$
2.30
$$

Degrees-of Freedom
258
1.813
$\mathrm{K}_{95 / 95} \mathrm{~S}$ (\%)
1.59
1.59

## 50

2.060
3.28
3.34

## PIN PEAKING FACTOR UNCERTAINTIES

### 5.0 INTRODUCTION

The SIMULATE-3 pin peaking factor uncertainties for the Planar Radial Peaking Factor ( $F_{x y}$ ), One-Pin Peaking Factor ( $F_{Q}$ ), and Integrated Radial Peaking Factor ( $F_{R}, F_{\Delta H}$ ) were determined by combining the assembly power peaking uncertainties $\left(S_{F X Y}^{S}, S_{F Q}^{S}\right.$, and $S_{\mathrm{FR}}^{\mathrm{S}}$ ) from Section 4.7.3 with an appropriate uncertainty factor for the pin power reconstruction.

Yankee Atomic Electric Company verified the pin power reconstruction capabilities of SIMULATE-3 in extensive benchmarking (Reference 8). Three of the benchmark problems; B\&W critical experiments: Core 01, Core 12, and Core 18; were lattice configurations (pin dimensions, water hole, etc.) similar to the SONGS lattices.

Section 5.1 describes the three $B \& W$ cases and the results which were used as an estimate of the pin power reconstruction uncertainty. Since the lattice configurations are explicitly represented in the model, the pin power reconstruction uncertainty is applicable to lattices with small water holes (W) and large water holes (CE).

In Section 5.2 the uncertainties for pin peaking factors were calculated by combining the assembly power peaking uncertainties (Section 4.7.3) with the pin power reconstruction uncertainty (Section 5.1).

### 5.1 PIN POWER RECONSTRUCTION UNCERTAINTY

This section compares the SIMULATE-3 predicted pin-by-pin power distributions with the measured data from B\&W critical core configurations 01, 12, and 18 described in Reference 19.

Figures 5.1 through 5.3 show the SIMULATE-3 pin power distributions and the measurements. The differences, (Calculated - Measured)/Calculated, are also shown for each pin location. The SIMULATE-3 results agree well with the measurements. The Root-Mean-Squares (RMS) are all within one percent. Table 5.1 summarizes the mean ( $\overline{\mathrm{x}}$ ), standard deviation (S), and RMS for each case.

The standard deviations from these cases were tested for poolability with the Bartlett's test (Reference 20). Table 5.2 summarizes the parameters. The test confirms that the samples are poolable. Table 5.3 provides the pooled mean $(\bar{x})$, standard deviation (S), as well as the K*S value for the $95 / 95$ tolerance limit.

The tolerance limit ( $\overline{\mathrm{x}}-\mathrm{K}_{95 / 95} \mathrm{~S}$ ) was calculated by subtracting the mean from the $\mathrm{K}_{95 / 95} \mathrm{~S}_{\text {pooled }}$. Since the sample mean was very small and positive, it was assumed zero. The resulting tolerance limit was 1.608\%. For conservatism, the 95/95 tolerance limit for pin power reconstruction, $\mathrm{K}_{95 / 95} \mathrm{~S}$ (pin), was set to $2.00 \%$.

## Figure 5.1

## Pin Power Distribution Comparison

## B\&W Core 01

| Measured | ---- | 1.018 | 1.011 | 0.987 | 0.981 | 0.997 | 0.966 | 0.945 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| SIM-3 |  | 1.037 | 1.003 | 0.989 | 0.985 | 0.982 | 0.963 | 0.943 |
| Diff (\%) | ---- | 1.83 | -0.80 | 0.20 | 0.41 | -1.53 | -0.31 | -0.21 |
|  |  | 1.019 | 1.067 | 1.012 | 1.009 | 1.058 | 0.999 | 0.945 |
|  |  | 1.030 | 1.068 | 1.014 | 1.011 | 1.050 | 0.984 | 0.947 |
|  |  | 1.07 | 0.09 | 0.20 | 0.20 | -0.76 | -1.52 | 0.21 |
|  |  |  | - | 1.081 | 1.090 | ---- | 1.032 | 0.953 |
|  |  |  | ---- | 1.083 | 1.085 | ---- | 1.040 | 0.952 |
|  |  |  | ---- | 0.18 | -0.46 | ---- | 0.77 | -0.11 |
|  |  |  |  | 1.054 | 1.104 | 1.086 | 0.989 | 0.945 |
|  |  |  |  | 1.060 | 1.105 | 1.087 | 0.990 | 0.946 |
|  |  |  |  | 0.57 | 0.09 | 0.09 | 0.10 | 0.11 |
|  |  |  |  |  | ---- | 1.059 | 0.965 | 0.934 |
|  |  |  |  |  | ---- | 1.057 | 0.962 | 0.934 |
|  |  |  |  |  | ---- | -0.19 | -0.31 | 0.00 |
| AVG. (\%) |  | 0.012 |  |  |  | 0.988 | 0.938 | 0.923 |
|  |  |  |  |  |  | 0.983 | 0.942 | 0.924 |
| RMS (\%) |  | 0.631 |  |  |  | -0.51 | 0.42 | 0.11 |
| S.D. (\%) |  | 0.641 |  |  |  |  | 0.925 | 0.914 |
|  |  |  |  |  |  |  | 0.927 | 0.914 |
|  |  |  |  |  |  |  | 0.22 | 0.00 |
|  |  |  |  |  |  |  |  | 0.903 |
|  |  |  |  |  |  |  |  | 0.905 |
|  |  |  |  |  |  |  |  | 0.22 |

## Figure 5.2

## Pin Power Distribution Comparison

## B\&W Core 12

| Measured SIM-3 <br> Diff (\%) |  | $\begin{array}{r} 1.075 \\ 1.095 \\ 1.83 \end{array}$ | 1.041 1.033 -0.77 | 1.006 1.012 0.59 | 1.019 0.999 -2.00 | 1.000 0.987 -1.32 | 0.960 0.956 -0.42 | 0.923 0.920 -0.33 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 1.067 | 1.125 | 1.044 | 1.034 | 1.075 | 0.987 | 0.927 |
|  |  | 1.073 | 1.123 | 1.040 | 1.028 | 1.079 | 0.979 | 0.923 |
|  |  | 0.56 | -0.18 | -0.38 | -0.58 | 0.37 | -0.82 | -0.43 |
|  |  |  | ---- | 1.114 | 1.118 | --- | 1.034 | 0.942 |
|  |  |  | ---- | 1.127 | 1.119 | ---- | 1.052 | 0.924 |
|  |  |  | ---- | 1.15 | 0.09 | ---- | 1.71 | -1.95 |
|  |  |  |  | 1.083 | 1.137 | 1.102 | 0.979 | 0.908 |
|  |  |  |  | 1.078 | 1.138 | 1.108 | 0.977 | 0.913 |
|  |  |  |  | -0.46 | 0.09 | 0:54 | -0.20 | 0.55 |
|  |  |  |  |  | ---- | 1.071 | 0.939 | 0.895 |
|  |  |  |  |  | ---- | 1.067 | 0.938 | 0.896 |
|  |  |  |  |  | ---- | -0.37 | -0.11 | 0.11 |
| AVG (\%) |  | -0.048 |  |  |  | 0.958 | 0.900 | 0.883 |
|  |  |  |  |  |  | 0.965 | 0.911 | 0.879 |
| RMS (\%) |  | 0.872 |  |  |  | 0.73 | 1.21 | -0.46 |
| S.D. (\%) |  | 0.885 |  |  |  |  | 0.884 | 0.856 |
|  |  |  |  |  |  |  | 0.885 | 0.860 |
|  |  |  |  |  |  |  | 0.11 | 0.47 |
|  |  |  |  |  |  |  |  | 0.845 |
|  |  |  |  |  |  |  |  | 0.838 |
|  |  |  |  |  |  |  |  | -0.84 |

Figure 5.3

## Pin Power Distribution Comparison

## B\&W Core 18

| Measured SIM-3 <br> Diff (\%) |  | 1.205 1.217 0.99 | 1.033 1.035 0.19 | 0.997 1.002 0.50 | $\begin{array}{r} 0.977 \\ 0.988 \\ 1.11 \end{array}$ | $\begin{array}{r} 0.959 \\ 0.970 \\ 1.13 \end{array}$ | 0.941 0.948 0.74 | 0.909 0.922 1.41 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 1.076 | 1.021 | 1.012 | 1.010 | 0.982 | 0.946 | 0.912 |
|  |  | 1.082 | 1.033 | 1.028 | 1.014 | 0.983 | 0.951 | 0.920 |
|  |  | 0.55 | 1.16 | 1.56 | 0.39 | 0.10 | 0.53 | 0.87 |
|  |  |  | 1.065 | 1.228 | 1.203 | 1.043 | 0.957 | 0.928 |
|  |  |  | 1.079 | 1.211 | 1.197 | 1.038 | 0.958 | 0.919 |
|  |  |  | 1.30 | -1.40 | -0.50 | -0.48 | 0.10 | -0.98 |
|  |  |  |  | ---- | ---- | 1.183 | 0.974 | 0.924 |
|  |  |  |  | ---- | ---- | 1.168 | 0.966 | 0.913 |
|  |  |  |  | ---- | ---- | -1.28 | -0.83 | -1.20 |
|  |  |  |  |  | ---- | 1.170 | 0.970 | 0.909 |
|  |  |  |  |  | ---- | 1.154 | 0.953 | 0.901 |
|  |  |  |  |  | ---- | -1.39 | -1.78 | -0.89 |
| AVG. (\%) |  | 0.048 |  |  |  | 0.995 | 0.924 | 0.886 |
|  |  |  |  |  |  | 0.999 | 0.922 | 0.883 |
| RMS (\%) |  | 0.925 |  |  |  | 0.40 | -0.22 | -0.34 |
| S.D. (\%) |  | 0.939 |  |  |  |  | 0.893 | 0.866 |
|  |  |  |  |  |  |  | 0.890 | 0.862 |
|  |  |  |  |  |  |  | -0.34 | -0.46 |
|  |  |  |  |  |  |  |  | 0.833 |
|  |  |  |  |  |  |  |  | 0.838 |
|  |  |  |  |  |  |  |  | 0.60 |

Table 5.1

## SIMULATE-3 Pin Power Distribution

## Benchmark Results

| CASE | $\frac{\bar{x}(\%)}{}$ | S (\%) | RMS $(\%)$ | $\frac{N}{2}$ |
| :--- | :---: | :---: | :---: | :---: |
| Core 01 | 0.012 | 0.641 | 0.631 | 32 |
| Core 12 | -0.048 | 0.885 | 0.872 | 32 |
| Core 18 | 0.048 | 0.939 | 0.925 | 32 |

## Table 5.2

Bartlett's Test Results for Pin Power Distributions

| b-value | 4.773 |
| :--- | :--- |
| Degrees-of-Freedom | 2 |
| $\chi_{0.05}^{2}$ | 5.991 |
| Conclusion | Poolable |
| $S_{\text {pooled }}(\%)$ | 0.832 |

Table 5.3
Pooled Statistics for SIMULATE-3

## Pin Power Distribution

Benchmark Results
$\frac{\bar{x}(\%)}{0.004}$
$\underline{S}_{\text {pooled_(\%) }}$
0.832
N

96 $\quad$| $\underline{K}_{95 / 95}$ |
| :--- |
| 1.933 |

$\underline{K}_{95 / 95} \underline{S}_{\text {POOLED_( }}(\%)$
1.608

For conservatism, the tolerance limit is set to $2.00 \%$

### 5.2 CALCULATION OF PIN PEAKING FACTOR UNCERTAINTIES

The 95/95 tolerance limits for Planar Radial Peaking Factor $\left(F_{X Y}\right)$, One-Pin Peaking Factor ( $F_{Q}$ ), and the Integrated Radial Peaking Factor ( $F_{R}, F_{\Delta B}$ ) can be calculated by using:

$$
\begin{gathered}
\mathrm{K}_{95 / 95} \mathrm{~S}(\text { combined })=\left(\left(\mathrm{K}_{95 / 95} \mathrm{~S}(\text { assembly })\right)^{2}+\left(\mathrm{K}_{95 / 95} \mathrm{~S}(\mathrm{pin})\right)^{2}\right)^{1 / 2} .5 \mathrm{E}^{1 / 2.1)}
\end{gathered}
$$

where,

| $K_{95 / 95} S$ (assembly) | are the $95 / 95$ tolerance limits for <br> assembly power peaking. From Section |
| :--- | :--- |
|  | 4.7 .3, the $95 / 95$ tolerance limits for |

$\mathrm{K}_{95 / 95} \mathrm{~S}(\mathrm{pin}) \quad$ is the $95 / 95$ tolerance limit for the pin power reconstitution. From Section 5.1, this uncertainty component is $2 \%$.

Table 5.4 summarizes the calculation of the tolerance limits for $F_{X Y}, F_{Q}$, and $F_{R}\left(F_{\Delta B}\right)$ of $5.20 \%, 4.62 \%$, and $3.89 \%$, respectively.

The tolerance limits are applied to the SIMULATE-3 calculated peaking factors at all power levels and for all rodded and unrodded cases using:

Adjusted Peaking Factor $=(S I M U L A T E-3$ results $)$ * (1 + Tolerance Limit/100)
(Eq. 5.2.2)

## Table 5.4

## Calculation of Peaking Factor Tolerance Limits

|  | $\underset{\substack{\mathrm{K}_{9 / 95} \mathrm{~S}(\text { Assembly }) \\(\%)}}{ }$ | $\begin{gathered} \mathrm{K}_{95 / 95} \mathrm{~S}(\operatorname{Pin}) \\ (\%) \\ \hline \end{gathered}$ | $\frac{\mathrm{K}_{95 / 95} \mathrm{~S} \text { (Combined) }}{(\%)}$ |
| :---: | :---: | :---: | :---: |
| $F_{X Y}$ | 4.780 | 2.000 | 5.20 |
| $\mathrm{F}_{\mathrm{Q}}$ | 4.170 | 2.000 | 4.62 |
| $\mathrm{F}_{\mathrm{R}}$ | 3.340 | 2.000 | 3.89 |

## SECTION 6

## CONCLUSIONS

Southern California Edison Company (SCE) has performed extensive benchmarking using the CASMO-3/SIMULATE-3 methodology. This effort consisted of comparisons of calculated physics parameters to measurements from both Pressurized Water Reactors (PWR) and Critical Experiments. The results were used to determine a set of 95/95 (probability/confidence) tolerance limits for application in the calculation of key PWR physics parameters. This effort has also successfully demonstrated SCE's ability to use the CASMO-3/SIMULATE-3 computer program package.

Based on the analyses and results contained in this report, SCE concludes that the CASMO-3/SIMULATE-3 methodology applies to all steady-state PWR reactor physics calculations. The accuracy of this methodology is sufficient for use in licensing applications, PWR reload physics analysis, safety analysis inputs, startup predictions, core physics databooks, and, reactor protection system and monitoring system setpoint updates.

## SECTION 7

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[^0]:    * Level of significance $(\alpha)=0.05$

