
RESPONSE TO REQUEST FOR ADDITIONAL INFORMATION

07/08/2013

US-APWR Design Certification

Mitsubishi Heavy Industries

Docket No. 52-021

RAI NO.: NO. 490-3732 REVISION 0
SRP SECTION: 03.08.01 – Concrete Containment
APPLICATION SECTION: 3.8.1
DATE OF RAI ISSUE: 11/23/2009

QUESTION NO. 03.08.01-09:

In its response for Part (a) of Question 3.8.1-9, MHI states that thermal forces and moments are reduced according to the concrete cracking depth during the post-processing of the global FE model analysis results. The reduction is based on redistribution of section forces and moments that occurs from the concrete cracking.

For Part (b) of the question MHI explains that the depth of concrete cracking is calculated by determining the neutral axis of the cross-section of the member, along with consideration of strain compatibility among the concrete, liner, tendons, and steel reinforcement. A summary description of the stress verification methodology is presented in this response, including simplified examples to demonstrate the methodology.

The staff finds that MHI's response does not clearly indicate how thermal forces and moments are reduced according to the concrete cracking depth. In MHI's response, a notation, σ_c1 , is used to denote the extreme fiber stress of the concrete; however, in the example given at the end, an additional notation, σ_c2 , is introduced without any explanation. MHI is requested to clarify this confusion. Also, MHI is requested to provide a calculation example that is taken from the US-APWR design, and that will have numerical results clearly showing the amount of reduction in forces and moments and the concrete cracking depth.

ANSWER:

This response replaces the previous response submitted via MHI letter UAP-HF-10033 dated February 4, 2010 (ML100430768).

Due to changes in the US-APWR prestressed concrete containment vessel (PCCV) analysis and design approach, the variable, σ_c2 , is no longer applicable. As before, the reduction is based on redistribution of section forces and moments that occurs from the concrete cracking. Concrete is considered to crack when the section is subject to tension and the neutral axis is shifted.

The following example is provided to show how concrete cracking in the PCCV cylindrical section is considered. The stress across a concrete section is calculated as an un-cracked

section initially and then the stress due to concrete cracking is calculated to adjust the concrete section given the effects of the cracked concrete behavior.

The example presented herein is an example of a PCCV concrete section when subjected to a thermal gradient with reinforcement provided on both faces and concrete cracking is considered.

Given:	b	$= 12''$	t	$= 42''$
	$A' s$	$= 2 \text{ in}^2$	ΔT	$= 100^\circ\text{F Linear}$
	A_s	$= 2 \text{ in}^2$	E_c	$= 3 \times 10^6 \text{ psi}$
	n	$= 10$	α	$= 6.0 \times 10^{-6} \text{ (for concrete and steel)}$

Nomenclatures:

α is coefficient of thermal expansion ($^\circ\text{F}^{-1}$)

$A' s$ is inside steel area (in^2)

A_s is outside steel area (in^2)

t is concrete section height (in.)

ΔT is thermal gradient ($^\circ\text{F}$)

E_c is modulus of elasticity for concrete (psi)

E_s is modulus of elasticity for steel ($30 \times 10^6 \text{ psi}$)

f_s is tension reinforcing Steel Stress (psi)

$f' s$ is compression reinforcing Steel Stress (psi)

n is modular ratio of reinforcing and concrete (E_s/E_c)

σ_c is uncracked concrete stress (psi)

$\sigma' c$ is cracked concrete stress (psi)

Assumptions:

- The coefficient of thermal expansions for the reinforcing steel and concrete are equal to each other.
- Free axial expansion.

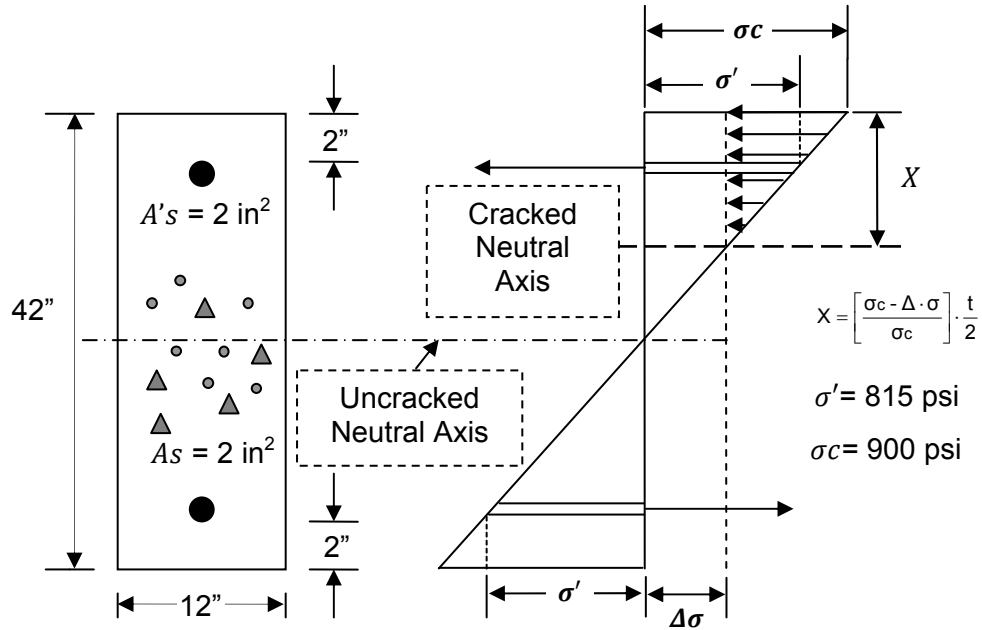


Figure 1 Section View and Stresses

Uncracked concrete stress, σ_c :

$$\sigma_c = \frac{1}{2} \alpha E_c \Delta T = 900 \text{ psi}$$

Cracked concrete stress at rebar location, σ' :

$$\sigma' = \sigma_c \left(\frac{\frac{t}{2} - 2''}{\frac{t}{2}} \right)$$

$$\sigma' = 900 \left(\frac{(21-2)}{21} \right) = 814.3 \text{ psi, use } \sigma' = 815 \text{ psi}$$

Force Equilibrium to Solve for Change in Stress, $\Delta\sigma$:

Reinforcing Tension – Initial Concrete Compression Force + Concrete Compression Reduction = 0

$$Asfs - \frac{\sigma_c}{2} \left(\frac{t}{2} \right) b + \frac{\Delta\sigma b}{2} \left[\frac{t}{2} + \frac{t}{2} \left(\frac{\sigma_c - \Delta\sigma}{\sigma_c} \right) \right] = 0$$

The term $Asfs$ is adjusted due to stress shift where reinforcing steel stress in tension is subtracted by the amount of reinforcing steel stress in compression and is calculated as follows:

$$Asfs = As(fs - f's) = [As(\sigma' + \Delta\sigma)n - As(\sigma' - \Delta\sigma)(n-1)]$$

Therefore, the change in stress, $\Delta\sigma$ is calculated as shown below.

$$2.0(815 + \Delta\sigma)10 - 2.0(815 - \Delta\sigma)(10 - 1) - \frac{900}{2}(21)(12) + \Delta\sigma\left(\frac{12}{2}\right)\left[21 + 21\left(\frac{900 - \Delta\sigma}{900}\right)\right] = 0$$

$$\Delta\sigma = 511.9 \text{ psi, use } \Delta\sigma = 512 \text{ psi}$$

The tension and compression reinforcement along with the concrete compression stress are adjusted with the $\Delta\sigma$ value calculated previously to account for concrete cracking condition. The tension and compression reinforcement and concrete compression stress are adjusted as follows:

Adjusted Tension Reinforcing Steel Stress, f_s

$$f_s = (\sigma' + \Delta\sigma)n$$

$$f_s = (815 + 512)10 = 13,270 \text{ psi}$$

Adjusted Compression Reinforcing Steel Stress, f'_s

$$f'_s = (\sigma' - \Delta\sigma)(n - 1)$$

$$f'_s = (815 - 512)(10-1) = 2,727 \text{ psi}$$

Adjusted Compression Concrete Stress, f_c

$$f_c = (\sigma_c - \Delta\sigma)$$

$$f_c = (900 - 512) = 388 \text{ psi}$$

The addition of compression reinforcing has increased the stress in the tensile reinforcing from 12,860 psi to 13,270 psi due to the compression reinforcing expanding from the applied thermal gradient. If the gradient is applied over a long period of time, the concrete section will creep in the compressive zone, relieving concrete stress, but increasing the compression reinforcing steel stress. The tensile reinforcing stress can be calculated by adjusting the outside reinforcing modular ratio, n .

$$f'_s = 2727 \frac{(2n - 1)}{(n - 1)} = 2727 \frac{(19)}{9} = 5,757 \text{ psi}$$

Due to the effects of concrete cracking have on the cross section, the neutral axis is shifted to reflect such conditions. The cracked neutral axis is therefore calculated as follows.

Cracked Neutral Axis, X

$$X = \left(\frac{\sigma_c - \Delta\sigma}{\sigma_c}\right) \frac{t}{2} = \left(\frac{388}{900}\right) 21 = 9.05 \text{ in.}$$

Impact on DCD

There is no impact on the DCD.

Impact on R-COLA

There is no impact on the R-COLA.

Impact on PRA

There is no impact on the PRA.

Impact on Technical/Topical Report

There is no impact on the Technical/Topical Report.

This completes MHI's response to the NRC's question.