

**Validation of SCALE4.4a-PC for
High Enriched Uranium Systems**

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1.0 Introduction

The SCALE4.4a KENO code [Reference 1] has been validated for enriched uranium systems using several different methods [References 2 through 5]. The objective of this evaluation is to establish that the CSAS25, CSAS26, and CSAS2X sequences will conservatively predict the multiplication factor (k_{eff}) of High Enriched Uranium (HEU) systems. In order to demonstrate the applicability of the SCALE4.4a KENO code for HEU systems, several critical experiments [References 6 through 53] using a variety of material forms were modeled with the SCALE4.4a KENO code and run on a desktop PC. The critical experiments were segregated into various groups based on the uranium system, and the results were evaluated using various statistical methods. Validations are performed using both KENO Va and KENO VI.

2.0 Methodology

2.1 Experiment Selection

Table 1 provides a summary of the critical experiments that were modeled. The critical experiments selected were chosen for analysis because they consist of HEU systems and are documented in sufficient detail to develop an accurate analytical model. Each critical experiment report provides comprehensive data on the materials of construction, dimensions, fissionable material, and experimental uncertainties.

The HEU experiments were selected and categorized into four distinct groups. These groupings consisted of:

- Group 1: All experiments (161) used in this validation,
- Group 2: Experiments (81) with $\text{ALCF} \leq 10^2$ eV, data sets 1-82, and
- Group 3: Experiments (56) with $\text{ALCF} > 10^2$ eV and $\leq 10^5$ eV, data sets 83-138, and
- Group 4: Experiments (24) with $\text{ALCF} > 10^5$ eV, data sets 139-162.

The experimental and calculated results were then compared based on a review of the k_{eff} distribution, enrichment (wt%²³⁵U), average lethargy causing fission (ALCF), the hydrogen-to-fissile atom ratio (H/X), and the fissile material density (g²³⁵U/l).

2.2 SCALE4.4a Models

Each critical experiment was modeled exactly as described in References 6 and 53. All criticality calculations were run to convergence, which typically required 600 generations and 1000 neutrons per generation for a total of 600,000 histories. Default values were used for all other parameters. All calculations were performed using the SCALE4.4a KENO Va Code with the 44-Group Standard Cross Section Library [Reference 1]. Appendix A contains the input decks for each critical experiment modeled. All dimensional and material information is identical to that reported in References 6 and 53. C5TOC6 is then executed to generate the initial KENO VI cases. Each case is then reviewed and further edited by the analyst (incorporate evaluator specific traits) and then executed for the validation.

2.3 Methodology for Statistical Evaluation of Results

The results of the SCALE4.4a KENO calculations were compared with the experimental results of the critical experiments through the use of various statistical analyses. The multiplication factor for each critical experiment is equal to unity; therefore, an accurate prediction of the multiplication factor using

SCALE4.4a KENO must be equivalent to unity also. The KENO program uses a Monte Carlo probability-based method, and as a result of this method, the calculated multiplication factors of an infinite number of critical experiments should provide a normal distribution about a mean multiplication factor of unity. However, it is known that biases exist in the SCALE4.4a program that lead to over-estimation of the multiplication factor for specific groups of fissile systems. Therefore, the objective of the statistical evaluation is to determine whether or not the results for each Group are normally distributed about unity (KENO predicts accurately for the Group) with an acceptable deviation (KENO predicts precisely for the Group). If KENO does not provide an accurate prediction, further evaluations are provided to determine whether or not a bias exists. The methods used to calculate the SCALE4.4a KENO Va bias and bias uncertainty is outlined in **References 54 and 55**.

2.3.1 Accuracy measures: Comparison of the Means

The calculated multiplication factors and the experimental multiplication factors represent two populations having the means μ_1 and μ_2 and the variances σ_1 and σ_2 . The objective of this comparison is to determine whether or not the means of the experimental and calculated data are statistically equivalent, and if they are not, whether or not there is an identifiable bias. A two-tailed t-test for the difference between two means [**Reference 55**] is used to test the hypothesis that the means of the two data sets are equal, or $\mu_1 = \mu_2$. The alternative hypothesis is $\mu_1 \neq \mu_2$, or the mean of the two populations are not equal, and that a bias exists in the calculated data. The t-value is calculated using Equation 1:

$$t = \frac{\mu_1 - \mu_2 - \delta}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}}, \quad (\text{Equation 1})$$

where:

- μ_1 is the mean of the standard data set,
- μ_2 is the mean of the data set to be tested,
- δ is the null hypothesis constant (0 here for the hypothesis of $\mu_1 = \mu_2$),
- σ_1 is the standard deviation of the standard data set,
- σ_2 is the standard deviation of the data set to be tested,
- n_1 is the number of observation in the standard data set, and
- n_2 is the number of observations in the data set to be tested.

2.3.2 Accuracy Measures: Determination Of Method Bias

The bias is defined as:

$$\text{Bias} = \bar{k}_{calc} - \bar{k}_{exp}, \quad (\text{Equation 2})$$

where k_{exp} and k_{calc} are the mean of the experimental and calculated (KENO) k_{eff} values, respectively.

2.3.3 Precision Measures: Determination Of Calculational Variance and Standard Deviation

The variance, S^2 , of the calculated KENO k_{eff} is defined as:

$$S^2 = \frac{\sum (\overline{k_{calc}} - k_i)^2}{n - 1}, \quad (\text{Equation 3})$$

where k_i is the calculated k_{eff} for the i^{th} critical experiment and n is the total number of experiments.

The standard deviation, σ_{calc} , of the KENO-calculated k_{eff} is the positive square root of the variance, S^2 . Note that this is *not* the KENO-calculated standard deviation, $\sigma_{KENO-calc}$, presented in **Table 3**, which is an average value of the calculated k_{eff} uncertainties.

2.3.4 Precision Measures: Determination Of Experimental Variance and Standard Deviation

The variance of the experimental k_{eff} is generally ignored, since the uncertainty associated with the measured k_{eff} (the known standard) is typically very small. Values reported for various experiments range from 0.0004 to 0.0019. Since the experimental uncertainties are usually reported as standard deviations, the experimental variance, S_o , is simply the average standard deviation of the group of experiments, $\overline{\sigma_{exp}}$, squared:

$$S_o^2 = (\overline{\sigma_{exp}})^2. \quad (\text{Equation 4})$$

2.3.5 Precision Measures: Determination Of Bias Uncertainty

According to **Reference 55**, the variance associated with the bias is given by the following equation:

$$V_B = \frac{S^2}{n} + S_o^2, \quad (\text{Equation 5})$$

where S^2 is the calculated k_{eff} variance (Equation 3), and S_o^2 is the experimental k_{eff} variance (Equation 4).

For conservatism, an additional term is added to Equation 5 to incorporate the effect of the individual uncertainties of the KENO-calculated k_{eff} value for each critical experiment model. The variance of the KENO-calculated uncertainty, S_u^2 , is defined as:

$$S_u^2 = \frac{\sum (\sigma_{calc,i})^2}{n}, \quad (\text{Equation 6})$$

where, $\sigma_{calc,i}$ is the uncertainty associated with the KENO results for experiment i , and n is the number of experiments. This equation is the square-weighted average of the individual KENO uncertainties. The standard deviation of the KENO-calculated uncertainties is the square root of the variance, S_u^2 .

Incorporating Equation 6 into Equation 5, the final equation for the variance associated with the KENO-calculated k_{eff} bias is:

$$V = \frac{(S^2 + S_u^2)}{n} + S_o^2. \quad (\text{Equation 7})$$

The standard deviation of the bias value is then simply the square root of the variance:

$$U = \kappa\sqrt{V}, \quad (\text{Equation 8})$$

where, κ is the 95/95 one-sided tolerance factor that is applied to the bias uncertainty for the number of critical experiments [Reference 54].

2.4 Methodology for Determination Applicable Limits

With the determination of the KENO bias and bias uncertainty associated with each Group of experiments, it is possible to calculate the Upper Subcritical Limits and the maximum allowable or biased KENO k_{eff} to maintain subcriticality for each system type.

2.4.1 Practical application: Calculation of an Upper Subcritical k_{eff} Limit

Starting at a multiplication factor of 1 (critical), the biases and uncertainties are subtracted, and the resulting number is the Upper Subcritical Limit for the system. At a 95% confidence level:

$$\text{Upper Subcritical Limit} = 1 + \text{bias} - U, \quad (\text{Equation 9})$$

where the *bias* and *U* are substituted from **Equations 2** and **8**, respectively. Values determined using this method are provided in **Table 3**. For systems with a positive bias, the second term of **Equation 9**, *bias*, is omitted.

In practice, the calculated system is considered to be subcritical if the following condition is met:

$$KENO_{\text{-calc-}k_{\text{eff}}} + \kappa(\sigma_{\text{KENO-calc}}) < \text{Upper Subcritical Limit}, \quad (\text{Equation 10})$$

where the system is subcritical at a 95% confidence level. A bounding κ factor of 1.645 is historically applied to the corresponding $\sigma_{\text{KENO-calc}}$ uncertainty for the calculation. This κ factor is different from that used in **Equation 8** for determination of the bias uncertainty.

2.4.2 Practical application: Calculation of the biased KENO Multiplication Factor

Alternatively starting with the calculated $KENO_{\text{-calc-}k_{\text{eff}}}$, a biased k_{eff} can be calculated:

$$\text{Biased } KENO\text{-}k_{\text{eff}} = KENO_{\text{-calc-}k_{\text{eff}}} + \kappa(\sigma_{\text{KENO-calc}}) - \text{bias} + U. \quad (\text{Equation 11})$$

And the system is considered to be subcritical if the following condition is met:

$$\text{Biased } KENO\text{-}k_{\text{eff}} < 1. \quad (\text{Equation 12})$$

In the case where the bias is positive (KENO consistently over-estimates k_{eff}), the bias term is omitted for conservatism.

3.0 Calculation Results

Table 2 presents the multiplication factor (k_{eff}), standard deviation (σ), and average lethargy causing fission (ALCF) calculated for each critical experiment modeled using the SCALE4.4a code with the 44 group cross-section library. **Table 3** provides the results of the statistical evaluations from different groupings of critical experiment data sets. The Upper Limit Subcritical k_{eff} for each group was calculated using the mean KENO-calculated uncertainty for the Group. In practice, it is preferable to use the actual

KENO-calculated standard deviation for the calculation being performed. However, it is conservative to use the mean KENO-calculated uncertainty to establish the bias for the group and then use the actual KENO-calculated standard deviation for the calculation to ensure a margin below the established limit.

4.0 Discussion

In order to validate the SCALE4.4a code for use with high enriched uranium systems, it is necessary to determine if KENO predicts the multiplication factor in an accurate and precise manner throughout the range of fission energies of interest. To evaluate the accuracy of the code, the mean of each Group of experiments was compared to the mean of the experimental results. A t-test was performed for each Group to determine whether or not the average result of a KENO calculation (the mean calculated k_{eff} for each Group) is statistically the same as the experimental result (unity). Passing the t-test affirms that the KENO code predicts multiplication factors accurately for the Group being tested, without bias. Failure of the t-test indicates that the mean KENO k_{eff} is statistically different from the experimental mean, and that a bias exists in the data. Groups that failed the t-test were further evaluated for bias and uncertainty, and these parameters applied to provide an upper limit subcritical multiplication factor for the Group.

Each Group of KENO-calculated k_{eff} s are also graphed against key system parameters (Enrichment {wtg%²³⁵U}, Energy of the Average Lethargy Causing Fission {ALCF}, Hydrogen-to-Fissile Atom Ratio {H/²³⁵U}, and fissile material density {g ²³⁵U/cc}) to identify trends within the data that may indicate inaccurate cross-sections or instabilities in the code. The normality of residuals is also tested using the Anderson-Darling method. The null hypothesis of a normality test is that there is no significant departure from normality. When the probability level, ρ is greater than 0.05, it fails to reject the null hypothesis and thus the assumption holds. Histogram, skewness and kurtosis plots are also provided for each group.

4.1 Comparison of the Means

The t-statistic for each Group evaluated against the experimental data is provided in **Table 3**. A two-tailed test at the 95% confidence limit was performed. All Groupings of the data were found to have statistically different means, and therefore, the mean KENO-calculated k_{eff} is biased.

4.2 Comparison of Uncertainty

In order to benchmark the performance of the code, the uncertainty associated with the KENO-calculated k_{eff} , must take into account the uncertainty associated with the critical experiment, since it is inherently a part of the result. The experimental uncertainty impacting the modeling of the experiment stems from material and geometric tolerances, rather than measurement of the experimental k_{eff} . Unfortunately, this type of uncertainty is not well evaluated or documented. Therefore, an average uncertainty of 0.0011 was assigned to those experiments that did not report an uncertainty value.

The bias uncertainty associated with Groups 1 through 4 are 0.0022, 0.0024, 0.0027, and 0.0037, respectively, at a 95% confidence level. For Groups 3 and 4, the uncertainty is higher than the bias. This fact leads to the conclusion that there is no detectable bias (either positive or negative) in the data, since application of the uncertainty obscures it. The uncertainty is lower than the bias for Groups 1 and 2 suggesting that there is a detectable bias in this data. However, as indicated in **Table 3** the bias is positive for all data groups.

4.3 Comparison of System Behavior as a Function of the System Attributes

For hydrogen moderated ^{235}U systems, the fission energy is proportional to the degree of moderation. Variations in the bias over the data range for the fissile density ($\text{g}^{235}\text{U}/\text{cc}$), energy of the average lethargy causing fission (ALCF) and the hydrogen-to-fissile atomic ratio ($\text{H}/^{235}\text{U}$) should be similar. However, differences will be evident due to statistical variations in the experimental and calculated results.

4.3.1 Oxide and Solution Systems

Dry (non-hydrogenous moderated) UO_2 systems at any enrichment are fast (neutronic) systems. The results of the critical experiments documented elsewhere, as well as the results of the critical experiments modeled here; show that the typical average lethargy causing fission in a fast system ranges from 10^4 to 10^6 eV. Fast critical UO_2 systems enriched to less than 15wt% are not feasible due to the large quantity of material required. However, a few LEU fast critical systems (metal) have been performed ranging in enrichment from 10 – 15wt%. The neutronic attributes of these fast metal experiments are very similar to the fast metal experiments with enrichments ranging from 93 - 97wt%. Several of these types of experiments are evaluated in this validation. The only major difference between the experiments at these different enrichments is the fact that more material is required for the lower enriched systems to achieve criticality. Various analytical methods have shown that an infinite UO_2 mass system has sufficient ^{235}U density to achieve criticality for enrichments near 7.0 wt %. However, without moderation, the system is fast. A few low-enriched (<5wt%) metal critical experiments have been performed; however, these systems also required moderation (water) to achieve critical configurations and therefore were driven by intermediate and thermal energy neutrons.

As moderator is introduced to the system, the neutronics of the system changes. A fast system becomes an under-moderated intermediate system. The typical average lethargy causing fission in an intermediate system ranges from 10^0 to 10^4 eV. Very few low enriched intermediate critical experiments have been performed. These systems are difficult to construct and maintain due to the under-moderated configurations. However, a few intermediate experiments have been completed using mixtures of low-enriched metals and fissile solutions. Several of these types of experiments are evaluated in this validation.

With additional moderation the intermediate system becomes a thermal system. The typical average lethargy causing fission in a thermal system ranges from 10^{-2} to 10^0 eV. The large majority of critical experiments are thermal. These systems are easily constructed at all enrichments. For a low enriched UO_2 system approximately 5.0wt% water is required to change the neutronics of the system from fast to thermal. Little difference is observed for enrichments less than 5.0wt% and those ranging from 5 to 10wt%. However, for enrichments ranging from 90 to 97wt%, a large amount of water, approximately 90wt%, is necessary to change the neutronics of a fast system to an intermediate, and finally a thermal, system.

Given that the mechanics of hydrogen moderated critical systems are the same regardless of enrichment, analytical computer codes predicting the k_{eff} of enriched systems should perform equally well at all enrichments. Since the SCALE4.4a KENO Code has been validated as performing accurately over a large range of enrichments with a variety of moderators and moderation levels, it is reasonable that it should also perform accurately in the remaining ranges. The results of these calculations demonstrate that the SCALE4.4a KENO Code is accurate in the high enrichment range. These results also demonstrate that the level of accuracy is the same as the accuracy of the KENO Code at other enrichment ranges [Reference 56].

4.3.2 Metal Systems

Metal systems are typically fast due to experimental configurations involving single and arrays of units at high densities with little or no moderation. Several experiments display similar attributes when the fissile media is further diluted with non-fissile metals. A few metal (fast) experiments exist at 10wt% however the majority of these experiments are highly enriched. Several of these types of experiments are evaluated in this validation.

4.4 Comparison of the k_{eff} Distributions

The KENO-calculated, unbiased k_{eff} was plotted for Groups 1 through 4 using a histogram to demonstrate the relative distributions about the mean value, as shown in **Figures 1** through **4**, respectively. If the CSAS25 sequence performs accurately without systemic errors, then the k_{eff} results will be normally distributed about a mean k_{eff} . This is expected since KENO is a Monte Carlo probability-based program. Also, a k_{eff} of unity is expected since the experiments were reported as being critical. As shown in the histograms, the distribution appears to be normal, with a slight positive bias indicating that the CSAS25 sequence contains a systemic conservative bias.

The normality of residuals, using the Anderson-Darling method, indicated that the probability level ρ is greater than 0.05 for **Groups 2** through **4**. Therefore, the test fails to reject the null hypothesis and thus the assumption, normal data, holds. The null hypothesis of a normality test is that there is no significant departure from normality. Since the probability level ρ is greater than 0.05, it fails to reject the null hypothesis and thus the assumption holds. Histogram, skewness and kurtosis plots are also provided for each group in **Figures 1** through **3** for **Groups 2** through **4**, respectively.

4.5 Bias Trends with Enrichment

Figure 5 shows the KENO-calculated, unbiased k_{eff} plotted as a function of the system enrichment. The enrichments of the selected benchmarks ranged from 62.40 to 97.68 wt% ^{235}U . Based on this plot, there appears to be no distinct or observable bias in the k_{eff} as a function of enrichment. Based on this, the proposed enrichment range for the validation can be extended from 97.68 wt% to 100.00 wt%.

4.6 Bias Trends with Average Lethargy Causing Fission (ALCF)

Figure 6 shows the KENO-calculated unbiased k_{eff} plotted as a function of the energy of the average lethargy causing fission (ALCF). The ALCF plots use a logarithmic scale to distinguish between the different neutron energy ranges. Based on this plot, there appears to be no distinct or observable bias in the k_{eff} as a function of the ALCF. Considering all experiments presented in this validation, the ALCF covers a range of energies from 0.0291eV to 914,000eV, spanning the thermal, intermediate, and fast fission groups.

4.7 Bias Trends with Hydrogen-to-Fissile Atom Ratio (H/X)

Figure 7 shows the KENO-calculated unbiased k_{eff} plotted as a function of the hydrogen-to-fissile atom ratio (H/X, where X is ^{235}U). Considering all experiments, the H/X covers a range from 0 to 1,836. This spans the under-moderated (less than 200), optimum (200 to 300), and over-moderated (greater than 300) regions. The H/X plots use a logarithmic scale to distinguish the different ranges of H/X values for the experiments. Overall, there appears to be no distinct or observable bias in the k_{eff} as a function of the hydrogen-to-fissile atom ratio.

4.8 Fissile Density ($\text{g }^{235}\text{U/cc}$)

Figure 8 shows the KENO-calculated unbiased k_{eff} plotted as a function of the fissile material density for all experiments. Considering all experiments, the fissile density covers a range from 0.014 to 18.36 g $^{235}\text{U/cc}$. The plot of the fissile density is similar to the plot of the ALCF. Overall, there appears to be no distinct or observable bias in the k_{eff} as a function of the fissile density.

4.9 KENO VI and KENO Va Comparison

Figure 9 shows the KENO VI-calculated unbiased k_{eff} plotted as a function of the KENO Va-calculated unbiased k_{eff} . The KENO VI results appear to be slightly higher for k_{eff} results less than 1.00 and slightly lower for k_{eff} results greater than 1.00. However, these observed k_{eff} differences are less than 0.0025. The results of both code versions statistically give essentially the same result. The KENO VI results are further provided in Table 2. The statistical results (bias and bias uncertainty) are further provided in Table 3.

5.0 Conclusions

The SCALE4.4a KENO Code provides precise results (slight positive bias for Groups 1 through 4) using the 44-Group Standard Cross Section Library for high enrichments with a variety of material forms, geometry, neutron energy, water-to-fuel ratio, density and ALCF. The precision of the code varies somewhat depending upon the fissile system being analyzed, as demonstrated by the results of the statistical evaluations. For the Group 1 (all experiments) at a 95% confidence level, the bias uncertainty of the KENO results is ± 0.0022 . The overall bias (Group 1) associated with the KENO results is +0.0031.

Additionally, the results of the parametric studies indicate that there appears to be no distinct or observable trends with the energy of the average lethargy causing fission, the moderator-to-fissile atom ratio, fissile density or enrichment. The recommended application of the KENO-calculated standard deviation, uncertainty, and Upper Subcritical Limits will prevent a critical system from being mistakenly evaluated as subcritical. The Group 1 data is normally distributed about a mean k_{eff} value of 1.0030 such that a one-sided 95% confidence level can be used to establish the Upper Limit k_{eff} . Based on this validation, the Upper Limit k_{eff} for Group 1 (All Data) is 0.9969 (includes the bias and bias uncertainty at a 95% confidence level). This value does not include an arbitrary administrative margin.

Many of the critical experiments available for code validation do not document experimental uncertainties that may impact the modeling of the system; therefore, it is difficult to assess whether poor results are due to faulty code performance or simply poor modeling of the experiment due to lack of proper information.

The overall (Group 1) Upper Subcritical Limit is 0.9969. However, an Upper Subcritical Limit of 0.9966 should be used for Groups 2 and 3 for ALCF values to 10^5eV . An Upper Subcritical Limit of 0.9958 must be used (Group 4) for ALCF values greater than 10^5eV . For all cases, including both KENO VI and KENO Va, an Upper Subcritical Limit of 0.9958 is bounding for ALCF values ranging from less than 10^2eV to greater than 10^5eV .

Based on these results, an administrative upper subcritical limit of 0.95 is overly restrictive. An administrative upper subcritical limit of 0.97 is justified based on this validation. This provides an arbitrary administrative margin of 3%. With a 3% margin the Upper Subcritical Limit is 0.9658. However, with a 5% margin the Upper Subcritical Limit is 0.9458. Values provided in Table 3 implement the Upper Subcritical Limit with a 5% margin. As applied to analyses, since the bias is

positive in all cases and neglected, limiting the $k_{\text{eff}} + 2\sigma$ to less than or equal to 0.9458 (5% administrative margin) meets the intended requirements of this validation.

6.0 Area of Applicability

An essential portion of a code validation effort is to define the area of applicability for the code. The area of applicability defines the types of materials, options, and range of parameter values that were used or were bounded by the validation. This study has demonstrated that Scale 4.4a/KENO V.a with the ENDF/B-V 44 group cross-sectional data is accurate for use in evaluating the multiplication factor for high enriched uranium (60.0-100.0 wt%), moderated, reflected and unreflected systems or configurations. The H/²³⁵U values used in the benchmark experiments varied from 0 to 1,836. The fissile density (g ²³⁵U/cc) ranges from 0.014 to 18.36. The average lethargy causing fission (ALCF) ranges from 0.0291eV to 914,000eV. This defines the range of applicability for the enrichment, H/²³⁵U, ALCF, and fissile density of this validation.

The MULTIREGION and INFHOM cross-sectional modeling options were used in the benchmark modeling. This validation specifically covers uranium systems (homogeneous and heterogeneous) moderated by hydrogen (water- or poly-bound hydrogen) with carbon, nitrogen, fluorine and oxygen also present as a portion of the uranium compound. This validation further covers various moderator and reflector materials such as water, carbon, concrete, paraffin, plexiglas, aluminum, natural uranium and polyethylene. The basic geometry package consisting of cuboid, cylinder, sphere and hemisphere were used in modeling the benchmark critical experiments. Several other materials including boron, chlorine, gadolinium, stainless steel, and carbon steel were also used in modeling the benchmark experiments.

If the parameters of a fissile system or configuration being evaluated are outside of the boundaries or limits of this evaluation, then an additional margin of subcriticality determined from an alternate code or specific experimental benchmark will be used to ensure that the system remains subcritical.

7.0 References

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- 9) HEU-COMP-THERM-011, *Critical and Subcritical Experiments with Four Clusters of Square-Pitched 21x21 Lattices of Highly Enriched (~80% ²³⁵U) Stainless-Steel-Clad Fuel Rods*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 10) HEU-COMP-THERM-012, *Critical and Subcritical Experiments with Four Clusters of Square-Pitched 18x18 Lattices of Highly Enriched (~80% ²³⁵U) Stainless-Steel-Clad Fuel Rods of Two Types*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 11) HEU-COMP-THERM-013, *Critical and Subcritical Experiments with Nine Clusters of Square-Pitched 14x14 Lattices of Highly Enriched (~80% ²³⁵U) Stainless-Steel-Clad Fuel Rods*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 12) HEU-COMP-THERM-014, *Critical and Subcritical Experiments with Nine Clusters of Square-Pitched 10x10 Lattices of Highly Enriched (~80% ²³⁵U) Stainless-Steel-Clad Fuel Rods*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 13) HEU-MET-FAST-001, *Bare, Highly Enriched Uranium Sphere (Godiva)*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 14) HEU-MET-FAST-003, *Reflected Oralloid Spherical Assemblies*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 15) HEU-MET-FAST-004, *Water-Reflected, Highly Enriched Uranium Sphere*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 16) HEU-MET-FAST-007, *Uranium Metal Slabs Moderated with Polyethylene, Plexiglas, and Teflon*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 17) HEU-MET-FAST-018, *Bare Spherical Assembly of ²³⁵U(90%)*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 18) HEU-MET-FAST-019, *Graphite-Reflected Spherical Assembly of ²³⁵U(90%)*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 19) HEU-MET-FAST-020, *Polyethylene-Reflected Spherical Assembly of ²³⁵U(90%)*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 20) HEU-MET-FAST-023, *Tinkertoy: Unmoderated Uranium Metal (93.2) Arrays with Cylinders of 10.5 kg Mass*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 21) HEU-MET-FAST-026, *Tinkertoy 2: Bare and Paraffin Reflected Uranium Metal (93.2) Arrays with 15, 20, and 25 kg Cylinders*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 22) HEU-MET-FAST-027, *Spherical Assembly of ²³⁵U(90%) with a 3.25-cm Lead Reflector*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 23) HEU-MET-FAST-031, *Spherical Assembly of ²³⁵U(90%) with Central Area of Polyethylene and 17.45-cm Polyethylene Reflector*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 24) HEU-MET-FAST-034, *Three Heterogeneous Cylinders of Highly Enriched Uranium with Polyethylene and Titanium, Aluminum, or Steel*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 25) HEU-MET-FAST-041, *²³⁵U(94%) Spheres Surrounded by Beryllium or Graphite Reflectors*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 26) HEU-MET-MIXED-001, *Heterogeneous Cylinder of Highly Enriched Uranium, Polyethylene, and Titanium with Polyethylene Reflector*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 27) HEU-MET-MIXED-002, *Spherical Assembly of ²³⁵U(90%) with Central Area of Polyethylene and 12.85-cm Polyethylene Reflector*, (NEA/NSC/DOC/(95)03/II), (September 2002).

- 28) HEU-MET-MIXED-003, *Spherical Assembly of ^{235}U (90%) with Central Area of Polyethylene and 15.85-cm Polyethylene Reflector*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 29) HEU-MET-MIXED-006, *Two Heterogeneous Cylinders of Highly Enriched Uranium with Polyethylene*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 30) HEU-SOL-THERM-002, *Concrete Reflected Cylinders of Highly Enriched Solutions of Uranyl Nitrate*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 31) HEU-SOL-THERM-003, *Plexiglas Reflected Cylinders of Highly Enriched Solutions of Uranyl Nitrate*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 32) HEU-SOL-THERM-004, *Reflected Uranyl-Fluoride Solutions in Heavy Water*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 33) HEU-SOL-THERM-005, *Aqueous Solutions of ^{235}U Poisoned with Pyrex Glass* (NEA/NSC/DOC/(95)03/II), (September 2002).
- 34) HEU-SOL-THERM-006, *Experiments with Boron-Poisoned Highly Enriched Uranyl Nitrate Solution*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 35) HEU-SOL-THERM-007, *Concrete Reflected Arrays Highly Enriched Solutions of Uranyl Nitrate*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 36) HEU-SOL-THERM-008, *Plexiglas Reflected Arrays Highly Enriched Solutions of Uranyl Nitrate*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 37) HEU-SOL-THERM-009, *Water-Reflected 6.4 Liter Spheres of Enriched Uranium Oxfluoride Solutions*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 38) HEU-SOL-THERM-010, *Water-Reflected 9.7 Liter Spheres of Enriched Uranium Oxfluoride Solutions*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 39) HEU-SOL-THERM-011, *Water-Reflected 17 Liter Spheres of Enriched Uranium Oxfluoride Solutions*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 40) HEU-SOL-THERM-012, *Water-Reflected 91 Liter Sphere of Enriched Uranium Oxfluoride Solution*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 41) HEU-SOL-THERM-014, *Uranium Nitrate Solution (70 gU/l) with Gadolinium*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 42) HEU-SOL-THERM-015, *Uranium Nitrate Solution (100 gU/l) with Gadolinium*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 43) HEU-SOL-THERM-020, *Unreflected Cylinders of Uranyl-Fluoride Solutions in Heavy Water*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 44) HEU-SOL-THERM-021, *Bare and Hydrogenous Reflected Arrays of Highly Enriched Solution of Uranyl Nitrate*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 45) HEU-SOL-THERM-025, *Uranium Nitrate Solutions with Gadolinium*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 46) HEU-SOL-THERM-027, *Uranium (89% ^{235}U) Nitrate Solution with Central Boron Carbide or Cadmium Absorber Rod*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 47) HEU-SOL-THERM-028, *Uranium (89% ^{235}U) Nitrate Solutions with Central Boron Carbide Absorber Rod*, (NEA/NSC/DOC/(95)03/II), (September 2002).

- 48) HEU-SOL-THERM-030, *Uranium (89% ²³⁵U) Nitrate Solutions with Cluster of Several Boron Carbide Absorber Rods*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 49) HEU-SOL-THERM-032, *A 48-Inch-Diameter Unreflected Sphere of ²³⁵U Nitrate Solution*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 50) HEU-SOL-THERM-033, *Highly Enriched Uranyl Nitrate in Annular Tanks with Concrete: Four Nested Tanks*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 51) HEU-SOL-THERM-035, *Boron Carbide Absorber Rods in Uranium (89% ²³⁵U) Nitrate Solutions*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 52) HEU-SOL-THERM-036, *Square-Pitched Lattices of Boron Carbide Absorber Rods in Uranium (89% ²³⁵U) Nitrate Solution*, (NEA/NSC/DOC/(95)03/II), (September 2002).
- 53) HEU-SOL-THERM-037, *Hexagonally Pitched Lattices of Boron Carbide Absorber Rods in Uranium Nitrate Solution*, (NEA/NSC/DOC/(95)03/II), (September 2002).
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Table 1 Summary of Critical Experiments Modeled

| Case ID | Case Number | H/ ²³⁵ U Atom Ratio | g ²³⁵ U/cc | Material | Geometry | Moderator | Reflector | Enrichment |
|---------------|-------------|--------------------------------|-----------------------|-----------------|-----------|-----------|-------------------------------------|------------|
| Heust-032-001 | 1 | 1836.68 | 0.01411 | Uranyl Nitrate | Spherical | Water/NO3 | Aluminum/Steel | 93.21 |
| Heust-002-009 | 2 | 458.76 | 0.05558 | Uranyl Nitrate | Cylinder | Water/NO3 | Concrete/Aluminum | 93.17 |
| Heust-012-001 | 3 | 1272.25 | 0.02047 | Uranyl Fluoride | Spherical | Water/HF | Water/Aluminum | 93.18 |
| Heust-037-005 | 4 | 463.05 | 0.05469 | Uranyl Nitrate | Cylinder | Water/NO3 | Water | 89.08 |
| Heust-028-001 | 5 | 374.56 | 0.06770 | Uranyl Nitrate | Cylinder | Water/NO3 | Water | 89.08 |
| Heust-014-002 | 6 | 418.13 | 0.06064 | Uranyl Nitrate | Cylinder | Water/NO3 | Water/Steel | 89.04 |
| Heust-035-005 | 7 | 378.60 | 0.06670 | Uranyl Nitrate | Cylinder | Water/NO3 | Water/Steel | 89.08 |
| Heust-035-001 | 8 | 766.63 | 0.03341 | Uranyl Nitrate | Cylinder | Water/NO3 | Water/Steel | 89.08 |
| Heust-007-009 | 9 | 336.62 | 0.07520 | Uranyl Nitrate | Cylinder | Water/NO3 | Concrete/Aluminum/Stainless Steel | 93.17 |
| Heust-037-002 | 10 | 684.46 | 0.03732 | Uranyl Nitrate | Cylinder | Water/NO3 | Water | 89.08 |
| Heust-011-001 | 11 | 523.41 | 0.04940 | Uranyl Fluoride | Spherical | Water/HF | Water/Aluminum | 93.20 |
| Heumt-006-012 | 12 | 0.00 | 0.72167 | U-Al Metal | Cuboid | Aluminum | Water | 93.17 |
| Heust-025-006 | 13 | 586.11 | 0.04336 | Uranyl Nitrate | Cylinder | Water/NO3 | Water | 89.04 |
| Heust-008-007 | 14 | 453.75 | 0.05620 | Uranyl Nitrate | Cylinder | Water/NO3 | Plexiglass/Aluminum/Stainless Steel | 93.17 |
| Heust-002-010 | 15 | 458.76 | 0.05558 | Uranyl Nitrate | Cylinder | Water/NO3 | Concrete/Aluminum | 93.17 |

Table 1 Summary of Critical Experiments Modeled

| Case ID | Case Number | H/ ²³⁵ U Atom Ratio | g ²³⁵ U/cc | Material | Geometry | Moderator | Reflector | Enrichment |
|---------------|-------------|--------------------------------|-----------------------|-----------------|-----------|-----------|-----------------------------------|------------|
| Heust-003-001 | 16 | 453.75 | 0.05620 | Uranyl Nitrate | Cylinder | Water/NO3 | Plexiglass/Stainless Steel | 93.17 |
| Heumt-006-005 | 17 | 0.00 | 0.72167 | U-Al Metal | Cuboid | Aluminum | Water | 93.17 |
| Heust-028-008 | 18 | 374.56 | 0.06770 | Uranyl Nitrate | Cylinder | Water/NO3 | Water | 89.08 |
| Heumt-006-016 | 19 | 0.00 | 0.72167 | U-Al Metal | Cuboid | Aluminum | Water | 93.17 |
| Heust-007-010 | 20 | 325.16 | 0.07779 | Uranyl Nitrate | Cylinder | Water/NO3 | Concrete/Aluminum/Stainless Steel | 93.17 |
| Heust-037-009 | 21 | 339.68 | 0.07393 | Uranyl Nitrate | Cylinder | Water/NO3 | Water | 89.08 |
| Heust-010-003 | 22 | 245.70 | 0.10190 | Uranyl Fluoride | Spherical | Water/HF | Water/Aluminum | 93.13 |
| Heust-036-002 | 23 | 302.47 | 0.08263 | Uranyl Nitrate | Cuboid | Water/NO3 | Steel | 89.14 |
| Heumt-006-018 | 24 | 0.00 | 0.72167 | U-Al Metal | Cuboid | Aluminum | Water | 93.17 |
| Heust-015-003 | 25 | 278.39 | 0.08948 | Uranyl Nitrate | Cylinder | Water/NO3 | Water/Steel | 89.04 |
| Heumt-006-010 | 26 | 0.00 | 0.72167 | U-Al Metal | Cuboid | Aluminum | Water | 93.17 |
| Heust-027-001 | 27 | 203.61 | 0.12115 | Uranyl Nitrate | Cylinder | Water/NO3 | None | 89.08 |
| Heust-027-005 | 28 | 203.61 | 0.12115 | Uranyl Nitrate | Cylinder | Water/NO3 | None | 89.08 |
| Heust-002-012 | 29 | 183.79 | 0.13452 | Uranyl Nitrate | Cylinder | Water/NO3 | Concrete/Aluminum | 93.17 |
| Heust-002-011 | 30 | 183.79 | 0.13452 | Uranyl Nitrate | Cylinder | Water/NO3 | Concrete/Aluminum | 93.17 |

Table 1 Summary of Critical Experiments Modeled

| Case ID | Case Number | H/ ²³⁵ U Atom Ratio | g ²³⁵ U/cc | Material | Geometry | Moderator | Reflector | Enrichment |
|---------------|-------------|--------------------------------|-----------------------|-----------------|----------|--|--------------------------|------------|
| Heuct-010-021 | 31 | 0.00 | 1.49407 | Uranium Dioxide | Cylinder | Beryllium/Borated Uranyl Nitrate/Water | Water | 62.40 |
| Heuct-010-010 | 32 | 0.00 | 1.49410 | Uranium Dioxide | Cylinder | Beryllium/Water | Water | 62.40 |
| Heuct-014-002 | 33 | 0.00 | 1.03792 | Uranium Dioxide | Cylinder | Aluminum/Silicon Oxides | Water | 79.38 |
| Heuct-010-017 | 34 | 0.00 | 1.49407 | Uranium Dioxide | Cylinder | Beryllium/Boric Acid/Water | Water | 62.40 |
| Heuct-010-015 | 35 | 0.00 | 1.49407 | Uranium Dioxide | Cylinder | Beryllium/Water | Water | 62.40 |
| Heuct-010-008 | 36 | 0.00 | 1.49407 | Uranium Dioxide | Cylinder | Beryllium/Water | Water | 62.40 |
| Heuct-014-001 | 37 | 0.00 | 1.03792 | Uranium Dioxide | Cylinder | Aluminum/Silicon Oxides | Water | 79.38 |
| Heust-020-003 | 38 | 847.40 | 0.03010 | Uranyl Fluoride | Cylinder | D2O/Water/HF | D2O/Water/Steel/Aluminum | 93.65 |
| Heuct-010-005 | 39 | 0.00 | 1.49407 | Uranium Dioxide | Cylinder | Beryllium/Water | Water | 62.40 |
| Heuct-010-006 | 40 | 0.00 | 1.49407 | Uranium Dioxide | Cylinder | Beryllium/Water | Water | 62.40 |
| Heust-030-004 | 41 | 91.14 | 0.25745 | Uranyl Nitrate | Cylinder | Water/NO3 | Water | 89.08 |
| Heust-025-017 | 42 | 62.68 | 0.35010 | Uranyl Nitrate | Cylinder | Water/NO3 | Water | 89.04 |
| Heust-025-016 | 43 | 61.85 | 0.35616 | Uranyl Nitrate | Cylinder | Water/NO3 | Water | 89.04 |
| Heuct-010-004 | 44 | 0.00 | 1.49407 | Uranium Dioxide | Cylinder | Beryllium/Water | Water | 62.40 |

Table 1 Summary of Critical Experiments Modeled

| Case ID | Case Number | H/ ²³⁵ U Atom Ratio | g ²³⁵ U/cc | Material | Geometry | Moderator | Reflector | Enrichment |
|---------------|-------------|--------------------------------|-----------------------|----------------|----------|-----------|--|------------|
| Heust-008-014 | 45 | 68.75 | 0.33164 | Uranyl Nitrate | Cylinder | Water/NO3 | Plexiglass/Aluminum/ Stainless Steel | 93.17 |
| Heust-021-006 | 46 | 58.78 | 0.38429 | Uranyl Nitrate | Cylinder | Water/NO3 | Paraffin | 92.60 |
| heust-005-015 | 47 | 80.26 | 0.28947 | Uranyl Nitrate | Cylinder | Water/NO3 | None | 87.40 |
| Heust-003-011 | 48 | 70.94 | 0.32175 | Uranyl Nitrate | Cylinder | Water/NO3 | Plexiglass/Aluminum | 93.17 |
| Heust-005-008 | 49 | 80.26 | 0.28947 | Uranyl Nitrate | Cylinder | Water/NO3 | Water | 87.40 |
| Heust-008-008 | 50 | 80.26 | 0.28947 | Uranyl Nitrate | Cylinder | Water/NO3 | Water | 87.40 |
| Heust-002-003 | 51 | 73.50 | 0.31191 | Uranyl Nitrate | Cylinder | Water/NO3 | Concrete/Stainless Steel | 93.17 |
| Heust-003-018 | 52 | 70.94 | 0.32175 | Uranyl Nitrate | Cylinder | Water/NO3 | Plexiglass/Aluminum | 93.17 |
| Heust-007-008 | 53 | 66.78 | 0.33925 | Uranyl Nitrate | Cylinder | Water/NO3 | Concrete/Aluminum/St ainless Steel | 93.17 |
| Heust-007-006 | 54 | 67.50 | 0.33576 | Uranyl Nitrate | Cylinder | Water/NO3 | Concrete/Aluminum/St ainless Steel | 93.17 |
| Heust-021-018 | 55 | 58.78 | 0.38429 | Uranyl Nitrate | Cylinder | Water/NO3 | top (paraffin), bottom (paraffin) | 92.60 |
| Heust-033-003 | 56 | 68.10 | 0.33317 | Uranyl Nitrate | Annular | Water/NO3 | Concrete | 93.22 |
| Heust-021-023 | 57 | 58.78 | 0.38429 | Uranyl Nitrate | Cylinder | Water/NO3 | top (plexiglass), bottom (plexiglass) | 92.60 |

Table 1 Summary of Critical Experiments Modeled

| Case ID | Case Number | H/ ²³⁵ U Atom Ratio | g ²³⁵ U/cc | Material | Geometry | Moderator | Reflector | Enrichment |
|---------------|-------------|--------------------------------|-----------------------|-----------------|-----------|-------------------------|-------------------------------|------------|
| Heust-033-008 | 58 | 68.10 | 0.33317 | Uranyl Nitrate | Annular | Water/NO3 | Concrete | 93.22 |
| Heuct-013-002 | 59 | 0.00 | 1.03792 | Uranium Dioxide | Cylinder | Aluminum/Silicon Oxides | Water | 79.38 |
| Heust-006-022 | 60 | 84.54 | 0.27481 | Uranyl Nitrate | Cylinder | Water/NO3 | Borated Water | 93.06 |
| Heust-009-002 | 61 | 47.23 | 0.50603 | Uranyl Fluoride | Spherical | Water/HF | Water/Aluminum | 93.19 |
| Heuct-010-003 | 62 | 0.00 | 1.49407 | Uranium Dioxide | Cylinder | Beryllium/Water | Water | 62.40 |
| Heucm-001-002 | 63 | 0.00 | 1.74728 | Uranium Dioxide | Cylinder | Oxygen | Water/Plexiglass/Polyethylene | 93.15 |
| Heust-006-014 | 64 | 84.98 | 0.27452 | Uranyl Nitrate | Cylinder | Water/NO3 | Nickel | 93.06 |
| Heust-006-021 | 65 | 84.24 | 0.27360 | Uranyl Nitrate | Cylinder | Water/NO3 | Nickel/Borated Water | 93.06 |
| Heuct-013-001 | 66 | 0.00 | 1.03792 | Uranium Dioxide | Cylinder | Aluminum/Silicon Oxides | Water | 79.38 |
| Heuct-011-002 | 67 | 0.00 | 1.03792 | Uranium Dioxide | Cylinder | Aluminum/Silicon Oxides | Water | 79.38 |
| Heuct-012-001 | 68 | 0.00 | 1.03792 | Uranium Dioxide | Cylinder | Aluminum/Silicon Oxides | Water | 79.48 |
| Heuct-011-001 | 69 | 0.00 | 1.03792 | Uranium Dioxide | Cylinder | Aluminum/Silicon Oxides | Water | 79.38 |
| Heust-004-004 | 70 | 134.90 | 0.18499 | Uranyl Fluoride | Spherical | D2O/Water/HF | D2O/Water/Steel | 93.65 |

Table 1 Summary of Critical Experiments Modeled

| Case ID | Case Number | H/ ²³⁵ U Atom Ratio | g ²³⁵ U/cc | Material | Geometry | Moderator | Reflector | Enrichment |
|---------------|-------------|--------------------------------|-----------------------|-----------------|-----------|----------------|-------------------------------|------------|
| Heust-020-001 | 71 | 227.70 | 0.10940 | Uranyl Fluoride | Cylinder | D2O/Water/HF | D2O/Water/Steel/Aluminum | 93.65 |
| Heust-004-003 | 72 | 80.96 | 0.30200 | Uranyl Fluoride | Spherical | D2O/Water/HF | D2O/Water/Steel | 93.65 |
| Heumt-003-005 | 73 | 0.00 | 17.69982 | U-Metal | Cuboid | None | Water | 94.52 |
| Heust-004-002 | 74 | 53.54 | 0.44298 | Uranyl Fluoride | Spherical | D2O/Water/HF | D2O/Water/Steel | 93.65 |
| Heust-004-001 | 75 | 34.10 | 0.67902 | Uranyl Fluoride | Spherical | D2O/Water/HF | D2O/Water/Steel | 93.65 |
| Heucm-001-018 | 76 | 34.10 | 0.67902 | Uranyl Fluoride | Spherical | D2O/Water/HF | D2O/Water/Steel | 93.65 |
| Heucm-001-017 | 77 | 0.00 | 4.49781 | Uranium Dioxide | Cylinder | Oxygen | Water/Plexiglass/Polyethylene | 93.15 |
| Heucm-001-015 | 78 | 0.00 | 4.49781 | Uranium Dioxide | Cylinder | Oxygen | Water/Plexiglass/Polyethylene | 93.15 |
| Heucm-001-016 | 79 | 0.00 | 4.49781 | Uranium Dioxide | Cylinder | Oxygen | Water/Plexiglass/Polyethylene | 93.15 |
| Heumf-007-043 | 80 | 0.00 | 4.49781 | Uranium Dioxide | Cylinder | Oxygen | Water/Plexiglass/Polyethylene | 93.15 |
| Heucm-001-019 | 81 | 0.00 | 17.18152 | U-Metal | Cuboid | None | Polyethylene | 93.15 |
| Heuci-004-001 | 82 | 0.00 | 4.49781 | Uranium Dioxide | Cylinder | Oxygen | Water/Plexiglass/Polyethylene | 93.15 |
| Heucm-001-013 | 83 | 0.45 | 0.09763 | Uranium Dioxide | Cuboid | Graphite/Water | None | 92.28 |

Table 1 Summary of Critical Experiments Modeled

| Case ID | Case Number | H/ ²³⁵ U Atom Ratio | g ²³⁵ U/cc | Material | Geometry | Moderator | Reflector | Enrichment |
|---------------|-------------|--------------------------------|-----------------------|-----------------|----------|-----------|---------------------------------|------------|
| Heucm-001-011 | 84 | 0.00 | 4.49781 | Uranium Dioxide | Cylinder | Oxygen | Water/Plexiglass/Polyethylene | 93.15 |
| Heucm-001-012 | 85 | 0.00 | 4.49781 | Uranium Dioxide | Cylinder | Oxygen | Water/Plexiglass/Polyethylene | 93.15 |
| Heumf-007-042 | 86 | 0.00 | 17.18338 | U-Metal | Cuboid | None | Polyethylene | 93.15 |
| Heumf-007-041 | 87 | 0.00 | 17.21505 | U-Metal | Cuboid | None | Polyethylene | 93.15 |
| Heucm-001-009 | 88 | 0.00 | 4.49781 | Uranium Dioxide | Cylinder | Oxygen | Water/Plexiglass/Polyethylene | 93.15 |
| Heumf-007-018 | 89 | 0.00 | 17.23368 | U-Metal | Cuboid | None | Polyethylene | 93.15 |
| Heucm-001-010 | 90 | 0.00 | 4.49781 | Uranium Dioxide | Cylinder | Oxygen | Water/Plexiglass/Polyethylene | 93.15 |
| Heumf-007-017 | 91 | 0.00 | 17.23554 | U-Metal | Cuboid | None | Polyethylene | 93.15 |
| Heucm-001-027 | 92 | 1.56 | 5.41384 | Uranium Dioxide | Cylinder | Alcohol | Alcohol/Plexiglass/Polyethylene | 93.15 |
| Heucm-001-026 | 93 | 1.56 | 5.41384 | Uranium Dioxide | Cylinder | Alcohol | Alcohol/Plexiglass/Polyethylene | 93.15 |
| Heucm-001-025 | 94 | 1.56 | 5.41384 | Uranium Dioxide | Cylinder | Alcohol | Alcohol/Plexiglass/Polyethylene | 93.15 |
| Heucm-001-023 | 95 | 1.56 | 5.41384 | Uranium Dioxide | Cylinder | Alcohol | Alcohol/Plexiglass/Polyethylene | 93.15 |

Table 1 Summary of Critical Experiments Modeled

| Case ID | Case Number | H/ ²³⁵ U Atom Ratio | g ²³⁵ U/cc | Material | Geometry | Moderator | Reflector | Enrichment |
|---------------|-------------|--------------------------------|-----------------------|-----------------|----------|-----------|---------------------------------|------------|
| Heucm-001-024 | 96 | 1.56 | 5.41384 | Uranium Dioxide | Cylinder | Alcohol | Alcohol/Plexiglass/Polyethylene | 93.15 |
| Heucm-001-029 | 97 | 1.56 | 5.41384 | Uranium Dioxide | Cylinder | Alcohol | Alcohol/Plexiglass/Polyethylene | 93.15 |
| Heucm-001-028 | 98 | 1.56 | 5.41384 | Uranium Dioxide | Cylinder | Alcohol | Alcohol/Plexiglass/Polyethylene | 93.15 |
| Heucm-001-022 | 99 | 1.56 | 5.41384 | Uranium Dioxide | Cylinder | Alcohol | Alcohol/Plexiglass/Polyethylene | 93.15 |
| Heucm-001-021 | 100 | 1.56 | 5.41384 | Uranium Dioxide | Cylinder | Alcohol | Alcohol/Plexiglass/Polyethylene | 93.15 |
| Heucm-001-020 | 101 | 1.56 | 5.41384 | Uranium Dioxide | Cylinder | Alcohol | Alcohol/Plexiglass/Polyethylene | 93.15 |
| Heucm-001-008 | 102 | 0.00 | 4.49781 | Uranium Dioxide | Cylinder | Oxygen | Water/Plexiglass/Polyethylene | 93.15 |
| Heumm-002-001 | 103 | 0.00 | 16.52425 | U-Metal | Sphere | None | Polyethylene | 90.00 |
| Heumm-003-001 | 104 | 0.00 | 16.52425 | U-Metal | Sphere | None | Polyethylene | 90.00 |
| Heucm-001-005 | 105 | 0.00 | 4.49781 | Uranium Dioxide | Cylinder | Oxygen | Water/Plexiglass/Polyethylene | 93.15 |
| Heumf-007-031 | 106 | 0.00 | 17.37061 | U-Metal | Cuboid | None | Plexiglass | 93.15 |
| Heumf-007-039 | 107 | 0.00 | 17.24859 | U-Metal | Cuboid | None | Polyethylene | 93.15 |

Table 1 Summary of Critical Experiments Modeled

| Case ID | Case Number | H/ ²³⁵ U Atom Ratio | g ²³⁵ U/cc | Material | Geometry | Moderator | Reflector | Enrichment |
|---------------|-------------|--------------------------------|-----------------------|-----------------|---------------|----------------------|-------------------------------|------------|
| Heumf-007-040 | 108 | 0.00 | 17.28957 | U-Metal | Cuboid | None | Polyethylene | 93.15 |
| Heucm-001-007 | 109 | 0.00 | 4.49781 | Uranium Dioxide | Cylinder | Oxygen | Water/Plexiglass/Polyethylene | 93.15 |
| Heumf-007-038 | 110 | 0.00 | 17.17034 | U-Metal | Cuboid | None | Polyethylene | 93.15 |
| Heucm-001-006 | 111 | 0.00 | 4.49781 | Uranium Dioxide | Cylinder | Oxygen | Water/Plexiglass/Polyethylene | 93.15 |
| Heumf-007-037 | 112 | 0.00 | 17.18897 | U-Metal | Cuboid | None | Polyethylene | 93.15 |
| Heumm-001-001 | 113 | 0.00 | 17.83457 | U-Metal | Cylinder/Slab | None | Titanium/Polyethylene | 95.98 |
| Heumf-007-013 | 114 | 0.00 | 17.20853 | U-Metal | Cuboid | None | Polyethylene | 93.15 |
| Heumf-007-016 | 115 | 0.00 | 17.28212 | U-Metal | Cuboid | None | Polyethylene | 93.15 |
| Heumf-007-015 | 116 | 0.00 | 17.28957 | U-Metal | Cuboid | None | Polyethylene | 93.15 |
| Heumf-007-014 | 117 | 0.00 | 17.17872 | U-Metal | Cuboid | None | Polyethylene | 93.15 |
| Heumf-007-036 | 118 | 0.00 | 17.34639 | U-Metal | Cuboid | None | Polyethylene | 93.15 |
| Heumf-023-020 | 119 | 0.00 | 17.48432 | U-Metal | Cylinder | None | Polyethylene | 93.20 |
| Heumf-007-011 | 120 | 0.00 | 17.20853 | U-Metal | Cuboid | None | Polyethylene | 93.15 |
| Heumf-031 | 121 | 0.00 | 17.83087 | U-Metal | Cylinder | Carbon/Iron/Tungsten | Polyethylene | 95.96 |
| Heumf-007-035 | 122 | 0.00 | 17.11072 | U-Metal | Cuboid | None | Polyethylene | 93.15 |

Table 1 Summary of Critical Experiments Modeled

| Case ID | Case Number | H/ ²³⁵ U Atom Ratio | g ²³⁵ U/cc | Material | Geometry | Moderator | Reflector | Enrichment |
|---------------|-------------|--------------------------------|-----------------------|----------|----------|----------------------|---------------------------------|------------|
| Heumf-026-004 | 123 | 0.00 | 17.48432 | U-Metal | Cylinder | None | Paraffin | 93.20 |
| Heumf-034-003 | 124 | 0.00 | 17.83087 | U-Metal | Cylinder | Carbon/Iron/Tungsten | Titanium/Polyethylene /Aluminum | 95.96 |
| Heumf-034-001 | 125 | 0.00 | 17.60018 | U-Metal | Cuboid | None | Water | 94.01 |
| Heumf-034-002 | 126 | 0.00 | 17.83087 | U-Metal | Cylinder | Carbon/Iron/Tungsten | Titanium/Polyethylene /Aluminum | 95.96 |
| Heumf-026-006 | 127 | 0.00 | 17.48432 | U-Metal | Cylinder | None | Paraffin | 93.20 |
| Heumf-007-030 | 128 | 0.00 | 17.37806 | U-Metal | Cuboid | None | Plexiglass | 93.15 |
| Heumt-003-001 | 129 | 0.00 | 17.60018 | U-Metal | Cuboid | None | Water | 94.01 |
| Heumf-007-026 | 130 | 0.00 | 17.27374 | U-Metal | Cuboid | None | Polyethylene | 93.15 |
| Heumf-007-010 | 131 | 0.00 | 17.24113 | U-Metal | Cuboid | None | Polyethylene | 93.15 |
| Heumf-007-025 | 132 | 0.00 | 17.28212 | U-Metal | Cuboid | None | Polyethylene | 93.15 |
| Heumf-026-003 | 133 | 0.00 | 17.48432 | U-Metal | Cylinder | None | Paraffin | 93.20 |
| Heumf-004-002 | 134 | 0.00 | 18.35603 | U-Metal | Sphere | None | Water | 97.68 |
| Heumf-004-001 | 135 | 0.00 | 18.35603 | U-Metal | Sphere | None | Water, Plexiglass | 97.68 |
| Heumf-007-024 | 136 | 0.00 | 0.44400 | U-Metal | Cylinder | Iron/Nickel/Chromium | Carbon Steel | 93.18 |
| Heumf-007-023 | 137 | 0.00 | 17.27933 | U-Metal | Cuboid | None | Polyethylene | 93.15 |

Table 1 Summary of Critical Experiments Modeled

| Case ID | Case Number | H/ ²³⁵ U Atom Ratio | g ²³⁵ U/cc | Material | Geometry | Moderator | Reflector | Enrichment |
|---------------|-------------|--------------------------------|-----------------------|----------|----------|----------------------|------------------|------------|
| Heumf-007-006 | 138 | 0.00 | 17.31752 | U-Metal | Cuboid | None | Polyethylene | 93.15 |
| Heumf-007-022 | 139 | 0.00 | 17.30541 | U-Metal | Cuboid | None | Polyethylene | 93.15 |
| Heumf-007-009 | 140 | 0.00 | 17.27001 | U-Metal | Cuboid | None | Polyethylene | 93.15 |
| Heumf-007-008 | 141 | 0.00 | 17.27839 | U-Metal | Cuboid | None | Polyethylene | 93.15 |
| Heumf-007-005 | 142 | 0.00 | 17.26442 | U-Metal | Cuboid | None | Polyethylene | 93.15 |
| Heumf-007-003 | 143 | 0.00 | 17.26256 | U-Metal | Cuboid | None | Polyethylene | 93.15 |
| Heumf-020 | 144 | 0.00 | 17.29423 | U-Metal | Cuboid | None | Plexiglass | 93.15 |
| Heumf-007-002 | 145 | 0.00 | 16.58525 | U-Metal | Sphere | Carbon/Iron/Tungsten | Polyethylene | 89.65 |
| Heumf-003-004 | 146 | 0.00 | 17.53125 | U-Metal | Sphere | None | Tungsten Carbide | 93.50 |
| Heumf-041 | 147 | 0.00 | 17.37150 | U-Metal | Cuboid | None | Beryllum | 93.90 |
| Heumf-003-003 | 148 | 0.00 | 17.53125 | U-Metal | Sphere | None | Tungsten Carbide | 93.50 |
| Heumf-003-002 | 149 | 0.00 | 17.53125 | U-Metal | Sphere | None | Tungsten Carbide | 93.50 |
| Heumf-007-034 | 150 | 0.00 | 17.13215 | U-Metal | Cuboid | None | Teflon | 93.15 |
| Heumf-003-001 | 151 | 0.00 | 17.53125 | U-Metal | Sphere | None | Tungsten Carbide | 93.50 |
| Heumf-007-033 | 152 | 0.00 | 17.17779 | U-Metal | Cuboid | None | Teflon | 93.15 |
| Heumf-007-032 | 153 | 0.00 | 17.17779 | U-Metal | Cuboid | None | Teflon | 93.15 |

Table 1 Summary of Critical Experiments Modeled

| Case ID | Case Number | H/²³⁵U Atom Ratio | g²³⁵U/cc | Material | Geometry | Moderator | Reflector | Enrichment |
|----------------|--------------------|-------------------------------------|----------------------------|-----------------|-----------------|----------------------|------------------|-------------------|
| Heumf-019 | 154 | 0.00 | 16.54912 | U-Metal | Sphere | Carbon/Iron/Tungsten | Graphite | 89.60 |
| Heumf-027 | 155 | 0.00 | 16.29293 | U-Metal | Sphere | Carbon/Iron/Tungsten | Lead/Iron | 89.47 |
| Heumf-023-016 | 156 | 0.00 | 17.48430 | U-Metal | Cylinder | None | Polyethylene | 93.20 |
| Heumf-018 | 157 | 0.00 | 16.33423 | U-Metal | Sphere | Carbon/Iron/Tungsten | None | 89.65 |
| Heumf-026-001 | 158 | 0.00 | 17.48432 | U-Metal | Cylinder | None | None | 93.20 |
| Heumf-001-001 | 159 | 0.00 | 17.65883 | U-Metal | Sphere | None | None | 93.90 |
| Heumf-007-019 | 160 | 0.00 | 17.31845 | U-Metal | Cuboid | None | None | 93.15 |
| Heumf-007-001 | 161 | 0.00 | 17.21598 | U-Metal | Cuboid | None | None | 93.15 |

Table 2 Experimental and Calculation Results

| Case ID | Case Number | Kexp | Sigexp | K5calc | Sig5calc | K6calc | Sig6calc | ALCF, eV |
|---------------|-------------|--------|--------|--------|----------|--------|----------|----------|
| Heust-032-001 | 1 | 1.0000 | 0.0004 | 0.9994 | 0.0008 | 0.9979 | 0.0009 | 2.91E-02 |
| Heust-002-009 | 2 | 1.0000 | 0.0004 | 1.0081 | 0.0017 | 1.0077 | 0.0018 | 3.05E-02 |
| Heust-012-001 | 3 | 1.0000 | 0.0004 | 1.0047 | 0.0009 | 1.0018 | 0.0010 | 3.08E-02 |
| Heust-037-005 | 4 | 1.0000 | 0.0004 | 1.0092 | 0.0012 | 1.0046 | 0.0011 | 3.16E-02 |
| Heust-028-001 | 5 | 1.0000 | 0.0004 | 1.0019 | 0.0017 | 1.0014 | 0.0021 | 3.28E-02 |
| Heust-014-002 | 6 | 1.0000 | 0.0004 | 1.0149 | 0.0014 | 1.0157 | 0.0014 | 3.31E-02 |
| Heust-035-005 | 7 | 1.0000 | 0.0004 | 1.0066 | 0.0013 | 1.0096 | 0.0012 | 3.45E-02 |
| Heust-035-001 | 8 | 1.0000 | 0.0004 | 1.0045 | 0.0013 | 1.0014 | 0.0011 | 3.52E-02 |
| Heust-007-009 | 9 | 1.0000 | 0.0004 | 1.0085 | 0.0013 | 1.0080 | 0.0013 | 3.61E-02 |
| Heust-037-002 | 10 | 1.0000 | 0.0004 | 1.0061 | 0.0011 | 1.0044 | 0.0013 | 3.71E-02 |
| Heust-011-001 | 11 | 1.0000 | 0.0004 | 1.0075 | 0.0012 | 1.0049 | 0.0013 | 3.79E-02 |
| Heumt-006-012 | 12 | 1.0000 | 0.0004 | 1.0054 | 0.0016 | 1.0049 | 0.0014 | 4.00E-02 |
| Heust-025-006 | 13 | 1.0000 | 0.0004 | 1.0107 | 0.0009 | 1.0120 | 0.0009 | 4.07E-02 |
| Heust-008-007 | 14 | 1.0000 | 0.0004 | 1.0003 | 0.0014 | 0.9986 | 0.0014 | 4.13E-02 |

Table 2 Experimental and Calculation Results

| Case ID | Case Number | Kexp | Sigexp | K5calc | Sig5calc | K6calc | Sig6calc | ALCF, eV |
|---------------|-------------|--------|--------|--------|----------|--------|----------|----------|
| Heust-002-010 | 15 | 1.0000 | 0.0004 | 1.0079 | 0.0013 | 1.0089 | 0.0014 | 4.19E-02 |
| Heust-003-001 | 16 | 1.0000 | 0.0004 | 1.0070 | 0.0014 | 1.0008 | 0.0014 | 4.19E-02 |
| Heumt-006-005 | 17 | 1.0000 | 0.0004 | 1.0023 | 0.0015 | 1.0048 | 0.0016 | 4.34E-02 |
| Heust-028-008 | 18 | 1.0000 | 0.0004 | 1.0010 | 0.0014 | 0.9992 | 0.0015 | 4.56E-02 |
| Heumt-006-016 | 19 | 1.0000 | 0.0004 | 1.0030 | 0.0014 | 1.0008 | 0.0017 | 4.73E-02 |
| Heust-007-010 | 20 | 1.0000 | 0.0004 | 1.0142 | 0.0013 | 1.0162 | 0.0011 | 5.06E-02 |
| Heust-037-009 | 21 | 1.0000 | 0.0004 | 1.0057 | 0.0013 | 1.0057 | 0.0015 | 5.20E-02 |
| Heust-010-003 | 22 | 1.0000 | 0.0004 | 1.0023 | 0.0016 | 1.0012 | 0.0015 | 5.33E-02 |
| Heust-036-002 | 23 | 1.0000 | 0.0004 | 1.0006 | 0.0015 | 0.9966 | 0.0015 | 5.56E-02 |
| Heumt-006-018 | 24 | 1.0000 | 0.0004 | 1.0036 | 0.0018 | 1.0031 | 0.0016 | 6.04E-02 |
| Heust-015-003 | 25 | 1.0000 | 0.0004 | 1.0124 | 0.0013 | 1.0128 | 0.0013 | 6.04E-02 |
| Heumt-006-010 | 26 | 1.0000 | 0.0004 | 1.0040 | 0.0015 | 1.0040 | 0.0016 | 6.28E-02 |
| Heust-027-001 | 27 | 1.0000 | 0.0004 | 0.9983 | 0.0019 | 0.9999 | 0.0016 | 7.18E-02 |
| Heust-027-005 | 28 | 1.0000 | 0.0004 | 0.9946 | 0.0014 | 0.9989 | 0.0014 | 7.33E-02 |
| Heust-002-012 | 29 | 1.0000 | 0.0004 | 1.0113 | 0.0014 | 1.0082 | 0.0013 | 7.52E-02 |

Table 2 Experimental and Calculation Results

| Case ID | Case Number | Kexp | Sigexp | K5calc | Sig5calc | K6calc | Sig6calc | ALCF, eV |
|---------------|-------------|--------|--------|--------|----------|--------|----------|----------|
| Heust-002-011 | 30 | 1.0000 | 0.0004 | 1.0041 | 0.0015 | 1.0034 | 0.0015 | 7.69E-02 |
| Heuct-010-021 | 31 | 1.0000 | 0.0004 | 1.0059 | 0.0012 | 1.0040 | 0.0013 | 9.09E-02 |
| Heuct-010-010 | 32 | 1.0000 | 0.0004 | 1.0009 | 0.0011 | 1.0019 | 0.0011 | 9.57E-02 |
| Heuct-014-002 | 33 | 1.0000 | 0.0004 | 1.0028 | 0.0013 | 1.0000 | 0.0013 | 9.61E-02 |
| Heuct-010-017 | 34 | 1.0000 | 0.0004 | 1.0056 | 0.0013 | 1.0042 | 0.0012 | 9.69E-02 |
| Heuct-010-015 | 35 | 1.0000 | 0.0004 | 1.0027 | 0.0011 | 1.0031 | 0.0012 | 9.96E-02 |
| Heuct-010-008 | 36 | 1.0000 | 0.0004 | 1.0025 | 0.0012 | 1.0029 | 0.0012 | 1.09E-01 |
| Heuct-014-001 | 37 | 1.0000 | 0.0004 | 1.0001 | 0.0013 | 1.0036 | 0.0012 | 1.16E-01 |
| Heust-020-003 | 38 | 1.0000 | 0.0004 | 1.0098 | 0.0016 | 1.0083 | 0.0017 | 1.32E-01 |
| Heuct-010-005 | 39 | 1.0000 | 0.0004 | 0.9968 | 0.0011 | 0.9963 | 0.0012 | 1.37E-01 |
| Heuct-010-006 | 40 | 1.0000 | 0.0004 | 0.9947 | 0.0013 | 0.9965 | 0.0012 | 1.38E-01 |
| Heust-030-004 | 41 | 1.0000 | 0.0004 | 1.0028 | 0.0015 | 1.0016 | 0.0015 | 1.56E-01 |
| Heust-025-017 | 42 | 1.0000 | 0.0004 | 1.0057 | 0.0010 | 1.0062 | 0.0010 | 1.67E-01 |
| Heust-025-016 | 43 | 1.0000 | 0.0004 | 1.0148 | 0.0010 | 1.0134 | 0.0010 | 1.79E-01 |
| Heuct-010-004 | 44 | 1.0000 | 0.0004 | 0.9964 | 0.0013 | 0.9958 | 0.0014 | 1.90E-01 |

Table 2 Experimental and Calculation Results

| Case ID | Case Number | Kexp | Sigexp | K5calc | Sig5calc | K6calc | Sig6calc | ALCF, eV |
|---------------|-------------|--------|--------|--------|----------|--------|----------|----------|
| Heust-008-014 | 45 | 1.0000 | 0.0004 | 1.0000 | 0.0017 | 1.0005 | 0.0014 | 2.06E-01 |
| Heust-021-006 | 46 | 1.0000 | 0.0004 | 1.0132 | 0.0015 | 1.0138 | 0.0014 | 2.15E-01 |
| Heust-005-015 | 47 | 1.0000 | 0.0004 | 0.9984 | 0.0014 | 0.9985 | 0.0014 | 2.23E-01 |
| Heust-003-011 | 48 | 1.0000 | 0.0004 | 1.0024 | 0.0017 | 1.0012 | 0.0014 | 2.28E-01 |
| Heust-005-008 | 49 | 1.0000 | 0.0004 | 1.0039 | 0.0012 | 1.0031 | 0.0013 | 2.33E-01 |
| Heust-008-008 | 50 | 1.0000 | 0.0004 | 1.0004 | 0.0016 | 0.9998 | 0.0015 | 2.40E-01 |
| Heust-002-003 | 51 | 1.0000 | 0.0004 | 1.0020 | 0.0017 | 1.0029 | 0.0017 | 2.48E-01 |
| Heust-003-018 | 52 | 1.0000 | 0.0004 | 0.9990 | 0.0016 | 1.0003 | 0.0014 | 2.54E-01 |
| Heust-007-008 | 53 | 1.0000 | 0.0004 | 1.0046 | 0.0015 | 1.0040 | 0.0015 | 2.66E-01 |
| Heust-007-006 | 54 | 1.0000 | 0.0004 | 1.0065 | 0.0014 | 1.0059 | 0.0016 | 2.70E-01 |
| Heust-021-018 | 55 | 1.0000 | 0.0004 | 1.0030 | 0.0015 | 1.0061 | 0.0016 | 2.79E-01 |
| Heust-033-003 | 56 | 1.0000 | 0.0004 | 1.0033 | 0.0013 | 1.0020 | 0.0013 | 2.90E-01 |
| Heust-021-023 | 57 | 1.0000 | 0.0004 | 0.9989 | 0.0014 | 1.0014 | 0.0014 | 2.98E-01 |
| Heust-033-008 | 58 | 1.0000 | 0.0004 | 1.0029 | 0.0013 | 1.0041 | 0.0014 | 3.07E-01 |
| Heuct-013-002 | 59 | 1.0000 | 0.0004 | 0.9993 | 0.0012 | 1.0004 | 0.0011 | 3.12E-01 |

Table 2 Experimental and Calculation Results

| Case ID | Case Number | Kexp | Sigexp | K5calc | Sig5calc | K6calc | Sig6calc | ALCF, eV |
|---------------|-------------|--------|--------|--------|----------|--------|----------|----------|
| Heust-006-022 | 60 | 1.0000 | 0.0004 | 1.0037 | 0.0012 | 1.0024 | 0.0011 | 3.14E-01 |
| Heust-009-002 | 61 | 1.0000 | 0.0004 | 1.0046 | 0.0014 | 1.0045 | 0.0014 | 3.18E-01 |
| Heuct-010-003 | 62 | 1.0000 | 0.0004 | 0.9947 | 0.0015 | 0.9912 | 0.0014 | 3.24E-01 |
| Heucm-001-002 | 63 | 1.0000 | 0.0004 | 1.0102 | 0.0014 | 1.0111 | 0.0013 | 3.56E-01 |
| Heust-006-014 | 64 | 1.0000 | 0.0004 | 1.0048 | 0.0010 | 1.0029 | 0.0012 | 3.58E-01 |
| Heust-006-021 | 65 | 1.0000 | 0.0004 | 1.0040 | 0.0008 | 1.0043 | 0.0009 | 4.44E-01 |
| Heuct-013-001 | 66 | 1.0000 | 0.0004 | 0.9995 | 0.0014 | 0.9994 | 0.0012 | 4.49E-01 |
| Heuct-011-002 | 67 | 1.0000 | 0.0004 | 0.9976 | 0.0012 | 0.9954 | 0.0011 | 5.39E-01 |
| Heuct-012-001 | 68 | 1.0000 | 0.0004 | 0.9957 | 0.0015 | 0.9963 | 0.0014 | 5.94E-01 |
| Heuct-011-001 | 69 | 1.0000 | 0.0004 | 0.9972 | 0.0012 | 0.9972 | 0.0012 | 7.04E-01 |
| Heust-004-004 | 70 | 1.0000 | 0.0004 | 1.0027 | 0.0017 | 1.0044 | 0.0016 | 1.09E+00 |
| Heust-020-001 | 71 | 1.0000 | 0.0004 | 1.0065 | 0.0020 | 1.0037 | 0.0019 | 1.35E+00 |
| Heust-004-003 | 72 | 1.0000 | 0.0004 | 1.0017 | 0.0015 | 1.0015 | 0.0016 | 2.68E+00 |
| Heumt-003-005 | 73 | 1.0000 | 0.0004 | 0.9943 | 0.0017 | 0.9917 | 0.0015 | 2.73E+00 |
| Heust-004-002 | 74 | 1.0000 | 0.0004 | 1.0000 | 0.0017 | 1.0015 | 0.0017 | 5.59E+00 |

Table 2 Experimental and Calculation Results

| Case ID | Case Number | Kexp | Sigexp | K5calc | Sig5calc | K6calc | Sig6calc | ALCF, eV |
|----------------|--------------------|-------------|---------------|---------------|-----------------|---------------|-----------------|-----------------|
| Heust-004-001 | 75 | 1.0000 | 0.0004 | 1.0049 | 0.0016 | 1.0013 | 0.0016 | 1.30E+01 |
| Heucm-001-018 | 76 | 1.0000 | 0.0004 | 1.0072 | 0.0016 | 1.0079 | 0.0014 | 2.35E+01 |
| Heucm-001-017 | 77 | 1.0000 | 0.0004 | 1.0022 | 0.0010 | 1.0019 | 0.0010 | 2.50E+01 |
| Heucm-001-015 | 78 | 1.0000 | 0.0004 | 1.0129 | 0.0011 | 1.0129 | 0.0012 | 2.88E+01 |
| Heucm-001-016 | 79 | 1.0000 | 0.0004 | 1.0024 | 0.0011 | 1.0051 | 0.0010 | 2.92E+01 |
| Heumf-007-043 | 80 | 1.0000 | 0.0004 | 1.0081 | 0.0017 | 1.0073 | 0.0017 | 3.32E+01 |
| Heucm-001-019 | 81 | 1.0000 | 0.0004 | 1.0061 | 0.0014 | 1.0075 | 0.0017 | 5.81E+01 |
| Heuci-004-001 | 82 | 1.0000 | 0.0004 | 1.0138 | 0.0004 | 1.0141 | 0.0004 | 1.45E+02 |
| Heucm-001-013 | 83 | 1.0000 | 0.0004 | 1.0061 | 0.0011 | 1.0081 | 0.0010 | 2.32E+02 |
| Heucm-001-011 | 84 | 1.0000 | 0.0004 | 1.0074 | 0.0013 | 1.0085 | 0.0012 | 2.58E+02 |
| Heucm-001-012 | 85 | 1.0000 | 0.0004 | 1.0050 | 0.0012 | 1.0011 | 0.0011 | 2.59E+02 |
| Heumf-007-042 | 86 | 1.0000 | 0.0004 | 1.0066 | 0.0011 | 1.0037 | 0.0013 | 2.91E+02 |
| Heumf-007-041 | 87 | 1.0000 | 0.0004 | 1.0044 | 0.0015 | 1.0035 | 0.0014 | 3.05E+02 |
| Heucm-001-009 | 88 | 1.0000 | 0.0004 | 1.0061 | 0.0012 | 1.0042 | 0.0012 | 3.46E+02 |
| Heumf-007-018 | 89 | 1.0000 | 0.0004 | 0.9972 | 0.0014 | 0.9959 | 0.0013 | 3.47E+02 |

Table 2 Experimental and Calculation Results

| Case ID | Case Number | Kexp | Sigexp | K5calc | Sig5calc | K6calc | Sig6calc | ALCF, eV |
|---------------|-------------|--------|--------|--------|----------|--------|----------|----------|
| Heucm-001-010 | 90 | 1.0000 | 0.0004 | 0.9996 | 0.0012 | 1.0004 | 0.0012 | 3.50E+02 |
| Heumf-007-017 | 91 | 1.0000 | 0.0004 | 0.9943 | 0.0014 | 0.9959 | 0.0013 | 3.72E+02 |
| Heucm-001-027 | 92 | 1.0000 | 0.0004 | 1.0066 | 0.0012 | 1.0063 | 0.0012 | 3.83E+02 |
| Heucm-001-026 | 93 | 1.0000 | 0.0004 | 1.0049 | 0.0012 | 1.0052 | 0.0012 | 4.01E+02 |
| Heucm-001-025 | 94 | 1.0000 | 0.0004 | 1.0021 | 0.0014 | 1.0025 | 0.0012 | 4.42E+02 |
| Heucm-001-023 | 95 | 1.0000 | 0.0004 | 1.0131 | 0.0011 | 1.0107 | 0.0013 | 4.54E+02 |
| Heucm-001-024 | 96 | 1.0000 | 0.0004 | 1.0056 | 0.0011 | 1.0080 | 0.0013 | 4.54E+02 |
| Heucm-001-029 | 97 | 1.0000 | 0.0004 | 1.0096 | 0.0013 | 1.0064 | 0.0012 | 4.64E+02 |
| Heucm-001-028 | 98 | 1.0000 | 0.0004 | 1.0089 | 0.0012 | 1.0112 | 0.0012 | 4.82E+02 |
| Heucm-001-022 | 99 | 1.0000 | 0.0004 | 1.0059 | 0.0011 | 1.0046 | 0.0011 | 5.28E+02 |
| Heucm-001-021 | 100 | 1.0000 | 0.0004 | 1.0067 | 0.0011 | 1.0077 | 0.0010 | 5.35E+02 |
| Heucm-001-020 | 101 | 1.0000 | 0.0004 | 1.0122 | 0.0011 | 1.0100 | 0.0012 | 5.39E+02 |
| Heucm-001-008 | 102 | 1.0000 | 0.0004 | 1.0017 | 0.0012 | 1.0017 | 0.0013 | 5.54E+02 |
| Heumm-002-001 | 103 | 1.0000 | 0.0004 | 1.0096 | 0.0011 | 1.0108 | 0.0012 | 1.18E+03 |
| Heumm-003-001 | 104 | 1.0000 | 0.0004 | 1.0107 | 0.0012 | 1.0084 | 0.0012 | 1.18E+03 |

Table 2 Experimental and Calculation Results

| Case ID | Case Number | Kexp | Sigexp | K5calc | Sig5calc | K6calc | Sig6calc | ALCF, eV |
|---------------|-------------|--------|--------|--------|----------|--------|----------|----------|
| Heucm-001-005 | 105 | 1.0000 | 0.0004 | 1.0084 | 0.0011 | 1.0082 | 0.0011 | 1.54E+03 |
| Heumf-007-031 | 106 | 1.0000 | 0.0004 | 1.0002 | 0.0015 | 1.0011 | 0.0014 | 1.61E+03 |
| Heumf-007-039 | 107 | 1.0000 | 0.0004 | 1.0041 | 0.0011 | 1.0019 | 0.0013 | 1.70E+03 |
| Heumf-007-040 | 108 | 1.0000 | 0.0004 | 1.0066 | 0.0012 | 1.0071 | 0.0014 | 1.70E+03 |
| Heucm-001-007 | 109 | 1.0000 | 0.0004 | 1.0092 | 0.0012 | 1.0073 | 0.0011 | 1.72E+03 |
| Heumf-007-038 | 110 | 1.0000 | 0.0004 | 1.0016 | 0.0011 | 1.0008 | 0.0012 | 1.74E+03 |
| Heucm-001-006 | 111 | 1.0000 | 0.0004 | 1.0035 | 0.0010 | 1.0024 | 0.0010 | 1.82E+03 |
| Heumf-007-037 | 112 | 1.0000 | 0.0004 | 1.0032 | 0.0012 | 1.0032 | 0.0011 | 1.90E+03 |
| Heumm-001-001 | 113 | 1.0000 | 0.0004 | 1.0053 | 0.0012 | 1.0050 | 0.0012 | 2.26E+03 |
| Heumf-007-013 | 114 | 1.0000 | 0.0004 | 0.9972 | 0.0014 | 0.9997 | 0.0012 | 2.54E+03 |
| Heumf-007-016 | 115 | 1.0000 | 0.0004 | 0.9947 | 0.0014 | 0.9954 | 0.0014 | 2.82E+03 |
| Heumf-007-015 | 116 | 1.0000 | 0.0004 | 0.9949 | 0.0013 | 0.9925 | 0.0012 | 2.83E+03 |
| Heumf-007-014 | 117 | 1.0000 | 0.0004 | 0.9974 | 0.0013 | 0.9953 | 0.0013 | 3.70E+03 |
| Heumf-007-036 | 118 | 1.0000 | 0.0004 | 1.0049 | 0.0011 | 1.0046 | 0.0013 | 3.90E+03 |
| Heumf-023-020 | 119 | 1.0000 | 0.0004 | 1.0036 | 0.0013 | 1.0020 | 0.0012 | 5.14E+03 |

Table 2 Experimental and Calculation Results

| Case ID | Case Number | Kexp | Sigexp | K5calc | Sig5calc | K6calc | Sig6calc | ALCF, eV |
|---------------|-------------|--------|--------|--------|----------|--------|----------|----------|
| Heumf-007-011 | 120 | 1.0000 | 0.0004 | 0.9931 | 0.0012 | 0.9955 | 0.0015 | 5.53E+03 |
| Heumf-031 | 121 | 1.0000 | 0.0004 | 1.0018 | 0.0012 | 1.0045 | 0.0012 | 6.81E+03 |
| Heumf-007-035 | 122 | 1.0000 | 0.0004 | 0.9971 | 0.0012 | 0.9964 | 0.0012 | 7.53E+03 |
| Heumf-026-004 | 123 | 1.0000 | 0.0004 | 1.0013 | 0.0012 | 1.0033 | 0.0011 | 1.08E+04 |
| Heumf-034-003 | 124 | 1.0000 | 0.0004 | 1.0006 | 0.0011 | 1.0003 | 0.0013 | 1.51E+04 |
| Heumf-034-001 | 125 | 1.0000 | 0.0004 | 0.9963 | 0.0012 | 0.9966 | 0.0012 | 1.58E+04 |
| Heumf-034-002 | 126 | 1.0000 | 0.0004 | 0.9937 | 0.0012 | 0.9940 | 0.0013 | 1.62E+04 |
| Heumf-026-006 | 127 | 1.0000 | 0.0004 | 0.9999 | 0.0011 | 1.0029 | 0.0011 | 1.65E+04 |
| Heumf-007-030 | 128 | 1.0000 | 0.0004 | 0.9942 | 0.0013 | 0.9946 | 0.0013 | 1.75E+04 |
| Heumt-003-001 | 129 | 1.0000 | 0.0004 | 1.0009 | 0.0013 | 1.0013 | 0.0012 | 1.83E+04 |
| Heumf-007-026 | 130 | 1.0000 | 0.0004 | 0.9943 | 0.0014 | 0.9934 | 0.0013 | 2.50E+04 |
| Heumf-007-010 | 131 | 1.0000 | 0.0004 | 0.9970 | 0.0012 | 0.9934 | 0.0013 | 2.64E+04 |
| Heumf-007-025 | 132 | 1.0000 | 0.0004 | 0.9940 | 0.0012 | 0.9970 | 0.0013 | 2.66E+04 |
| Heumf-026-003 | 133 | 1.0000 | 0.0004 | 1.0036 | 0.0012 | 1.0037 | 0.0011 | 3.06E+04 |
| Heumf-004-002 | 134 | 1.0000 | 0.0004 | 0.9972 | 0.0013 | 1.0002 | 0.0011 | 3.10E+04 |

Table 2 Experimental and Calculation Results

| Case ID | Case Number | Kexp | Sigexp | K5calc | Sig5calc | K6calc | Sig6calc | ALCF, eV |
|---------------|-------------|--------|--------|--------|----------|--------|----------|----------|
| Heumf-004-001 | 135 | 1.0000 | 0.0004 | 0.9988 | 0.0011 | 0.9954 | 0.0011 | 3.12E+04 |
| Heumf-007-024 | 136 | 1.0000 | 0.0004 | 0.9975 | 0.0011 | 0.9959 | 0.0012 | 5.84E+04 |
| Heumf-007-023 | 137 | 1.0000 | 0.0004 | 0.9975 | 0.0014 | 0.9969 | 0.0013 | 6.25E+04 |
| Heumf-007-006 | 138 | 1.0000 | 0.0004 | 1.0011 | 0.0015 | 1.0035 | 0.0012 | 1.61E+05 |
| Heumf-007-022 | 139 | 1.0000 | 0.0004 | 0.9979 | 0.0012 | 0.9961 | 0.0013 | 1.80E+05 |
| Heumf-007-009 | 140 | 1.0000 | 0.0004 | 0.9965 | 0.0013 | 1.0004 | 0.0013 | 1.82E+05 |
| Heumf-007-008 | 141 | 1.0000 | 0.0004 | 0.9960 | 0.0012 | 0.9946 | 0.0012 | 2.06E+05 |
| Heumf-007-005 | 142 | 1.0000 | 0.0004 | 0.9965 | 0.0013 | 0.9949 | 0.0012 | 2.54E+05 |
| Heumf-007-003 | 143 | 1.0000 | 0.0004 | 0.9964 | 0.0014 | 0.9994 | 0.0012 | 3.76E+05 |
| Heumf-020 | 144 | 1.0000 | 0.0004 | 1.0016 | 0.0013 | 1.0001 | 0.0013 | 4.82E+05 |
| Heumf-007-002 | 145 | 1.0000 | 0.0004 | 0.9962 | 0.0012 | 0.9969 | 0.0010 | 4.98E+05 |
| Heumf-003-004 | 146 | 1.0000 | 0.0004 | 1.0135 | 0.0011 | 1.0143 | 0.0012 | 5.60E+05 |
| Heumf-041 | 147 | 1.0000 | 0.0004 | 1.0066 | 0.0012 | 1.0065 | 0.0011 | 5.65E+05 |
| Heumf-003-003 | 148 | 1.0000 | 0.0004 | 1.0088 | 0.0010 | 1.0083 | 0.0011 | 5.75E+05 |
| Heumf-003-002 | 149 | 1.0000 | 0.0004 | 1.0045 | 0.0011 | 1.0048 | 0.0011 | 6.23E+05 |

Table 2 Experimental and Calculation Results

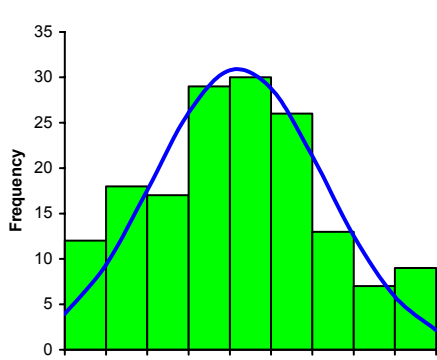
| Case ID | Case Number | Kexp | Sigexp | K5calc | Sig5calc | K6calc | Sig6calc | ALCF, eV |
|---------------|-------------|--------|--------|--------|----------|--------|----------|----------|
| Heumf-007-034 | 150 | 1.0000 | 0.0004 | 1.0105 | 0.0013 | 1.0099 | 0.0012 | 6.59E+05 |
| Heumf-003-001 | 151 | 1.0000 | 0.0004 | 1.0063 | 0.0011 | 1.0048 | 0.0011 | 6.82E+05 |
| Heumf-007-033 | 152 | 1.0000 | 0.0004 | 1.0064 | 0.0013 | 1.0082 | 0.0013 | 7.23E+05 |
| Heumf-007-032 | 153 | 1.0000 | 0.0004 | 1.0005 | 0.0012 | 0.9991 | 0.0011 | 7.97E+05 |
| Heumf-019 | 154 | 1.0000 | 0.0004 | 1.0061 | 0.0010 | 1.0047 | 0.0012 | 8.16E+05 |
| Heumf-027 | 155 | 1.0000 | 0.0004 | 1.0131 | 0.0012 | 1.0131 | 0.0012 | 8.55E+05 |
| Heumf-023-016 | 156 | 1.0000 | 0.0004 | 1.0019 | 0.0012 | 0.9999 | 0.0013 | 8.85E+05 |
| Heumf-018 | 157 | 1.0000 | 0.0004 | 0.9987 | 0.0012 | 1.0019 | 0.0011 | 8.89E+05 |
| Heumf-026-001 | 158 | 1.0000 | 0.0004 | 1.0021 | 0.0013 | 1.0031 | 0.0011 | 8.99E+05 |
| Heumf-001-001 | 159 | 1.0000 | 0.0004 | 1.0014 | 0.0011 | 0.9999 | 0.0011 | 9.05E+05 |
| Heumf-007-019 | 160 | 1.0000 | 0.0004 | 0.9962 | 0.0012 | 0.9971 | 0.0013 | 9.08E+05 |
| Heumf-007-001 | 161 | 1.0000 | 0.0004 | 0.9960 | 0.0011 | 0.9937 | 0.0012 | 9.14E+05 |

Table 3 Summary of Analysis Results

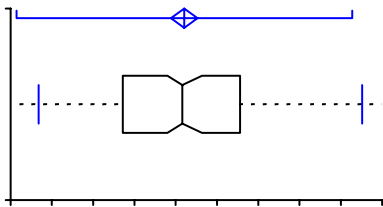
| | K5Group 1 All Data | K5Group 2 ALCF $\leq 10^2$ eV | K5Group 3 10^2 eV < ALCF $\leq 10^5$ eV | K5Group 4 ALCF > 10^5 eV | K6Group 1 All Data | K6Group 2 ALCF $\leq 10^2$ eV | K6Group 3 10^2 eV < ALCF $\leq 10^5$ eV | K6Group 4 ALCF > 10^5 eV |
|--|-------------------------------|---|---|---|-------------------------------|---|---|---|
| Number of Experiments | 161 | 81 | 56 | 24 | 161 | 81 | 56 | 24 |
| Mean Experimental k_{eff} | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| Mean Calculated k_{eff} | 1.0030 | 1.0037 | 1.0024 | 1.0023 | 1.0028 | 1.0033 | 1.0022 | 1.0023 |
| Experimental k_{eff} variance | 1.6000E-07 | 1.6000E-07 | 1.6000E-07 | 1.6000E-07 | 1.6000E-07 | 1.6000E-07 | 1.6000E-07 | 1.6000E-07 |
| Calculated k_{eff} variance | 2.6907E-05 | 2.3170E-05 | 3.0155E-05 | 3.1154E-05 | 2.6907E-05 | 2.3170E-05 | 3.0155E-05 | 3.1154E-05 |
| $\sigma_{KENO-calc}$ mean | 0.0013 | 0.0014 | 0.0012 | 0.0012 | 0.0013 | 0.0014 | 0.0012 | 0.0012 |
| t-value | -2543 | -1876 | -1365 | -879 | | | | |
| t-critical 1 tail (95%) | 1.8610 | 1.9620 | 2.0380 | 2.3090 | | | | |
| t-critical 2 tail (95%) | 1.9674 | 1.9750 | 1.9750 | 1.9818 | | | | |
| t-test 2 tail pass/fail | Fail | Fail | Fail | Fail | | | | |
| Method Bias | +0.0030 | +0.0037 | +0.0024 | +0.0023 | +0.0030 | +0.0037 | +0.0024 | +0.0023 |
| Uncertainty (U) {1 tail (95%)} | 0.0022 | 0.0024 | 0.0027 | 0.0037 | 0.0022 | 0.0024 | 0.0027 | 0.0037 |
| Total Uncertainty $\kappa(\sigma_{KENO-calc}) + (U)$ | 0.0031 | 0.0033 | 0.0034 | 0.0042 | 0.0030 | 0.0033 | 0.0034 | 0.0042 |
| Upper Limit k_{eff} | 0.9469 | 0.9467 | 0.9466 | 0.9458 | 0.9470 | 0.9467 | 0.9466 | 0.9458 |

Notes; Positive biases were neglected in the determination of the k_{eff} limits and the mean KENO-calculated standard deviation (σ) was used to determine the Upper Limit.

| | | |
|---------------------|--|-------------|
| Test | Continuous summary descriptives | |
| | Group 1 | |
| | Kcalc | |
| Performed by | RDMontgomery | Date |
| | | 7 July 2004 |

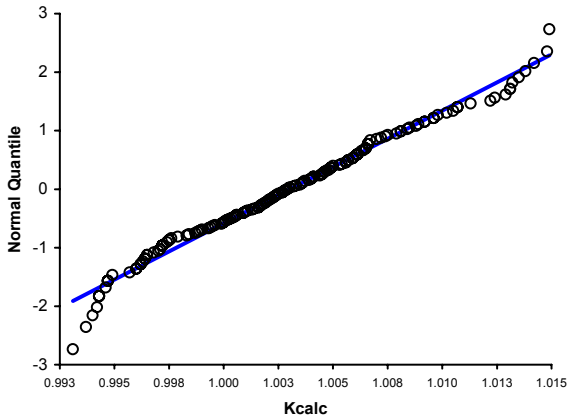


| | |
|-----------------|--------------------|
| n | 161 |
| Mean | 1.00302 |
| 95% CI | 1.00222 to 1.00383 |
| Variance | 0.000027 |
| SD | 0.005187 |
| SE | 0.000409 |
| CV | 1% |



| | |
|-----------------|--------------------|
| Median | 1.00290 |
| 96.0% CI | 1.00200 to 1.00410 |
| Range | 0.0218 |
| IQR | 0.0071 |

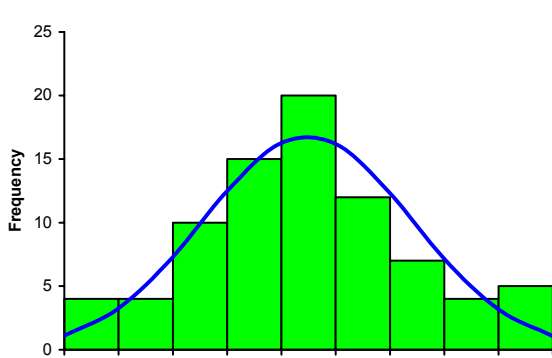
| Percentile | |
|-------------------|---------|
| 2.5th | 0.99421 |
| 25th | 0.99930 |
| 50th | 1.00290 |
| 75th | 1.00640 |
| 97.5th | 1.01379 |



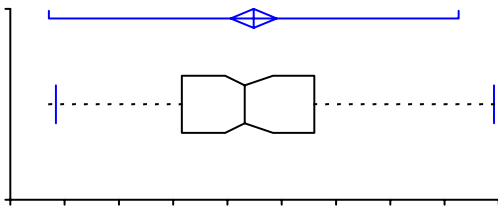
| | Coefficient | p |
|-------------------------|--------------------|----------|
| Anderson-Darling | 0.4951 | 0.2146 |
| Skewness | 0.1862 | 0.3228 |
| Kurtosis | -0.5371 | 0.0741 |

Figure 1, Group 1 Histogram, Skewness and Kurtosis.

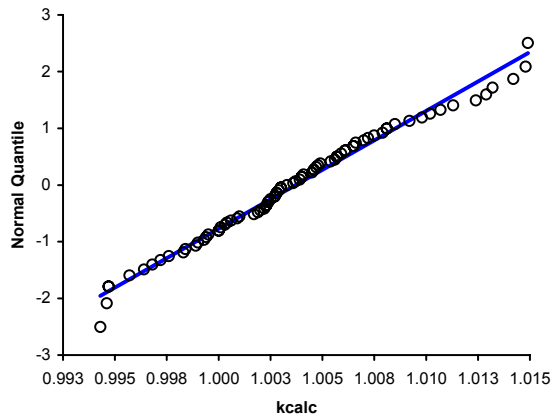
| | |
|---------------------|--|
| Test | Continuous summary descriptives |
| | Group 2 |
| | kcalc |
| Performed by | RDMontgomery |
| Date | 10 September 2003 |



| | |
|-----------------|--------------------|
| n | 81 |
| Mean | 1.00371 |
| 95% CI | 1.00264 to 1.00477 |
| Variance | 0.000023 |
| SD | 0.004814 |
| SE | 0.000535 |
| CV | 0% |



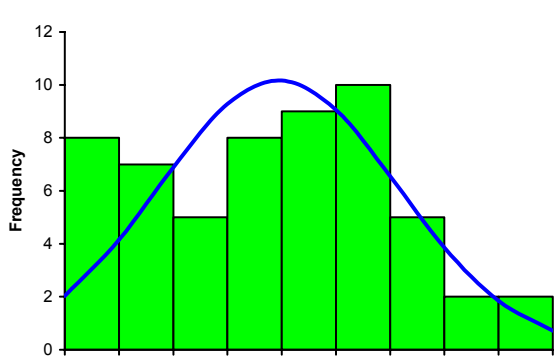
| | |
|-------------------|--------------------|
| Median | 1.00330 |
| 95.5% CI | 1.00240 to 1.00460 |
| Range | 0.0206 |
| IQR | 0.0061 |
| Percentile | |
| 2.5th | 0.99461 |
| 25th | 1.00040 |
| 50th | 1.00330 |
| 75th | 1.00650 |
| 97.5th | 1.01477 |



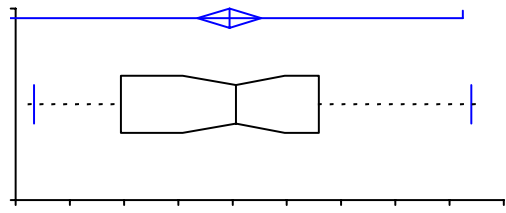
| | Coefficient | p |
|-------------------------|--------------------|----------|
| Anderson-Darling | 0.3513 | 0.4696 |
| Skewness | 0.2746 | 0.2927 |
| Kurtosis | -0.0750 | 0.9661 |

Figure 2, Group 2 Histogram, Skewness and Kurtosis.

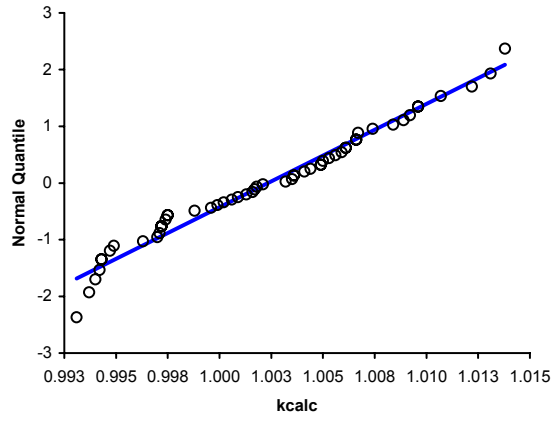
| | |
|---------------------|--|
| Test | Continuous summary descriptives |
| Group 3 | kcalc |
| Performed by | RDMontgomery |
| Date | 10 September 2003 |



| | |
|-----------------|--------------------|
| n | 56 |
| Mean | 1.00235 |
| 95% CI | 1.00088 to 1.00382 |
| Variance | 0.000030 |
| SD | 0.005491 |
| SE | 0.000734 |
| CV | 1% |



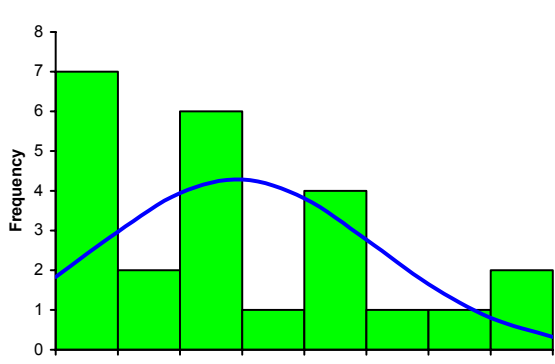
| | |
|-------------------|--------------------|
| Median | 1.00265 |
| 95.6% CI | 1.00020 to 1.00490 |
| Range | 0.0207 |
| IQR | 0.0091 |
| Percentile | |
| 2.5th | 0.99336 |
| 25th | 0.99735 |
| 50th | 1.00265 |
| 75th | 1.00648 |
| 97.5th | 1.01350 |



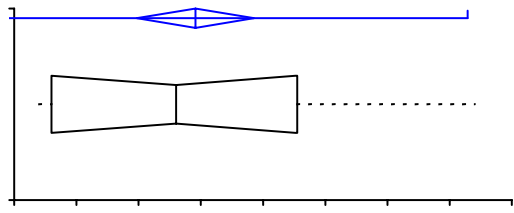
| | Coefficient | p |
|-------------------------|--------------------|----------|
| Anderson-Darling | 0.5075 | 0.2000 |
| Skewness | 0.0838 | 0.7834 |
| Kurtosis | -0.8797 | 0.0391 |

Figure 3, Group 3 Histogram, Skewness and Kurtosis.

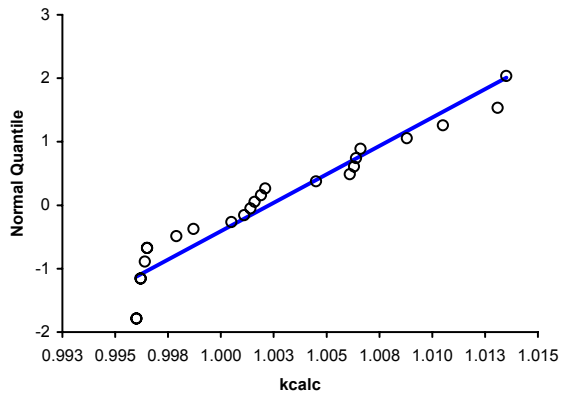
| | | |
|---------------------|--|-------------------|
| Test | Continuous summary descriptives | |
| | Group 4 | |
| | kcalc | |
| Performed by | RDMontgomery | Date |
| | | 10 September 2003 |



| | |
|-----------------|--------------------|
| n | 24 |
| Mean | 1.00228 |
| 95% CI | 0.99993 to 1.00464 |
| Variance | 0.000031 |
| SD | 0.005582 |
| SE | 0.001139 |
| CV | 1% |



| | |
|-------------------|--------------------|
| Median | 1.00150 |
| 97.7% CI | 0.99650 to 1.00630 |
| Range | 0.0175 |
| IQR | 0.0099 |
| Percentile | |
| 2.5th | - |
| 25th | 0.99650 |
| 50th | 1.00150 |
| 75th | 1.00638 |
| 97.5th | - |



| | Coefficient | p |
|-------------------------|--------------------|----------|
| Anderson-Darling | 0.7342 | 0.0557 |
| Skewness | 0.5767 | 0.2084 |
| Kurtosis | -0.7094 | 0.4126 |

Figure 4, Group 4 Histogram, Skewness and Kurtosis.

SCALE 4.4a Validation of KENO V.a for HEU Systems

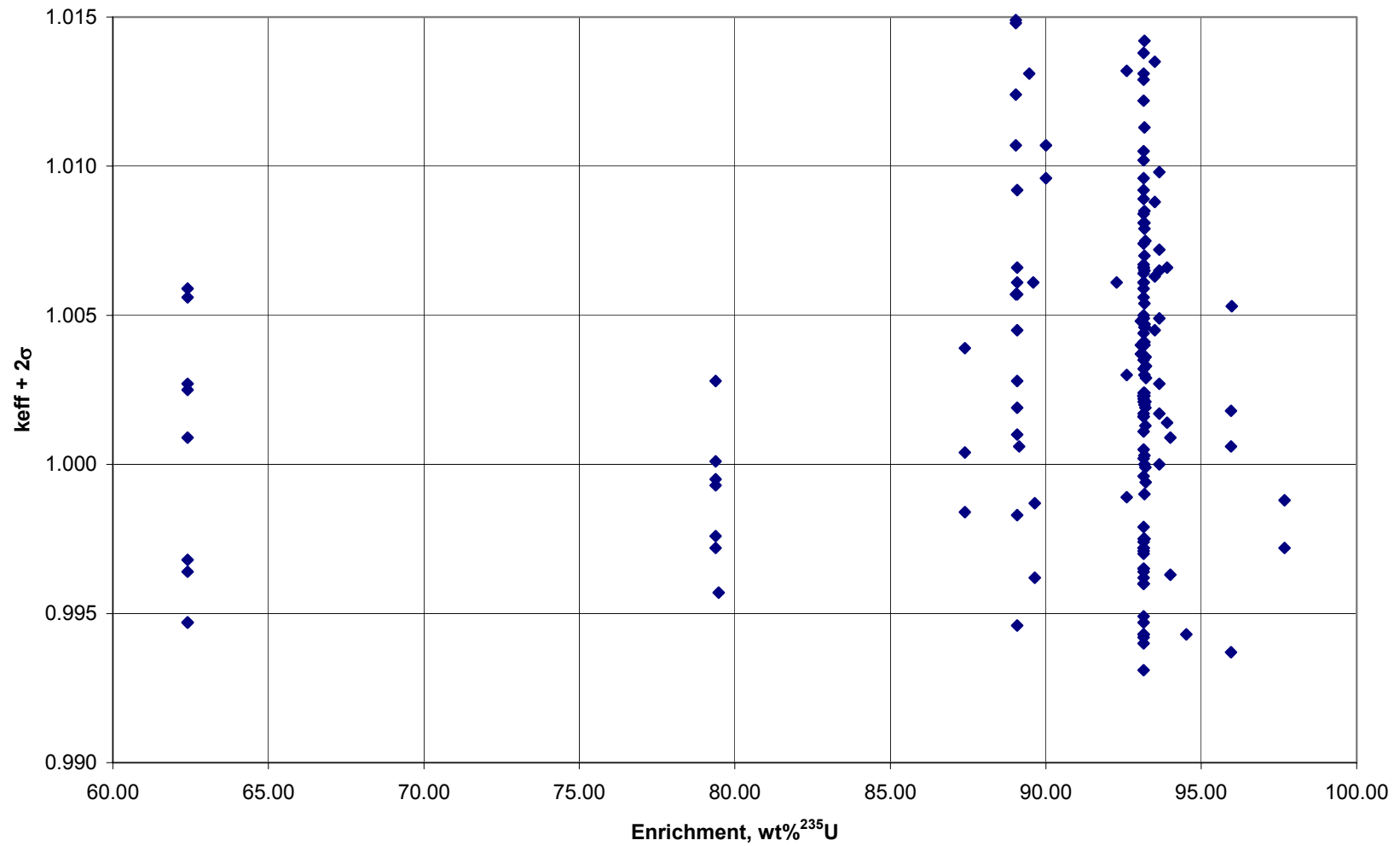


Figure 5, Plot of k_{eff} with the Enrichment (wt% ²³⁵U).

SCALE 4.4a Validation of KENO V.a for HEU Systems

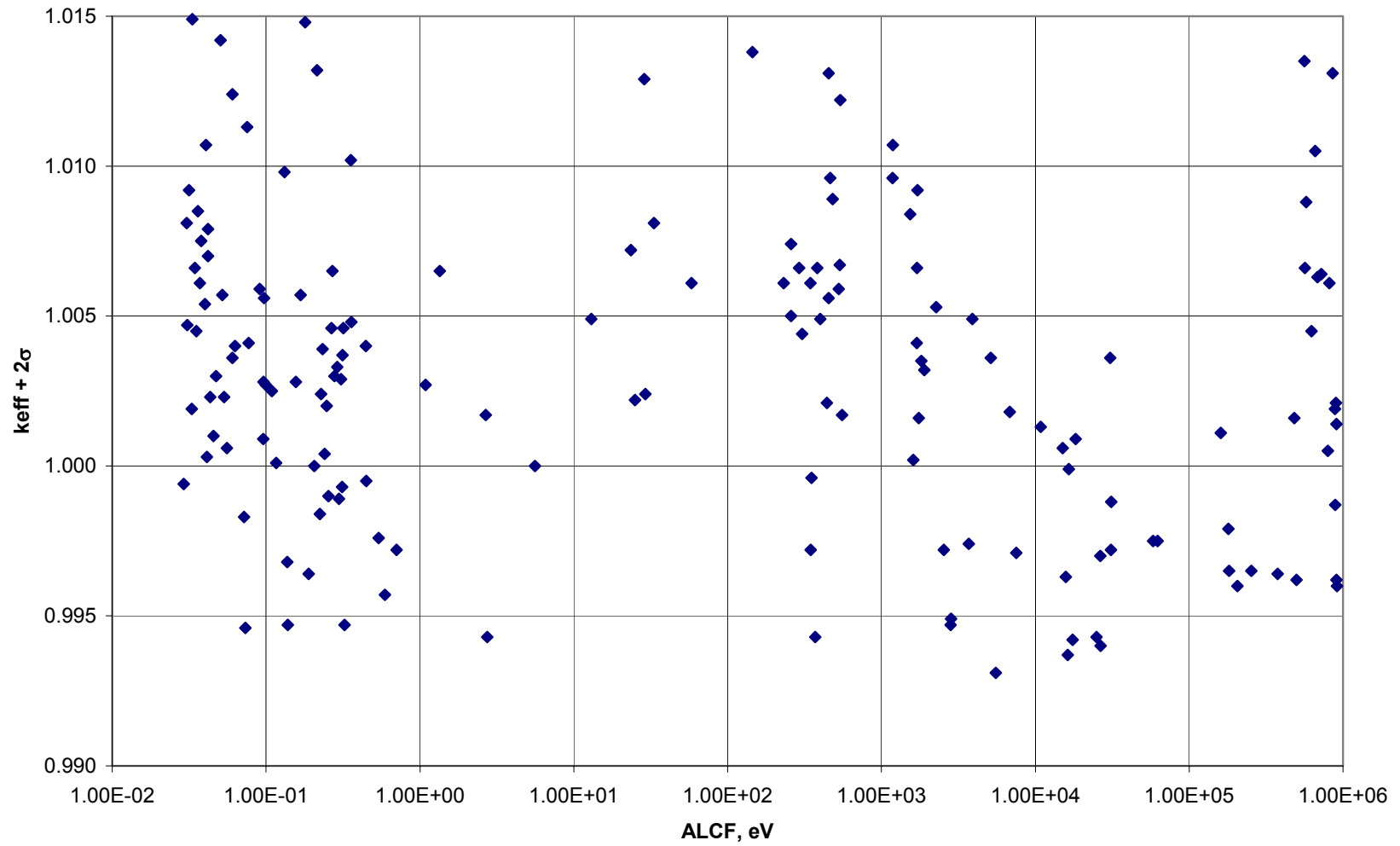


Figure 6, Plot of k_{eff} with the Energy of the Average Lethargy Causing Fission (ALCF).

SCALE 4.4a Validation of KENO V.a for HEU Systems

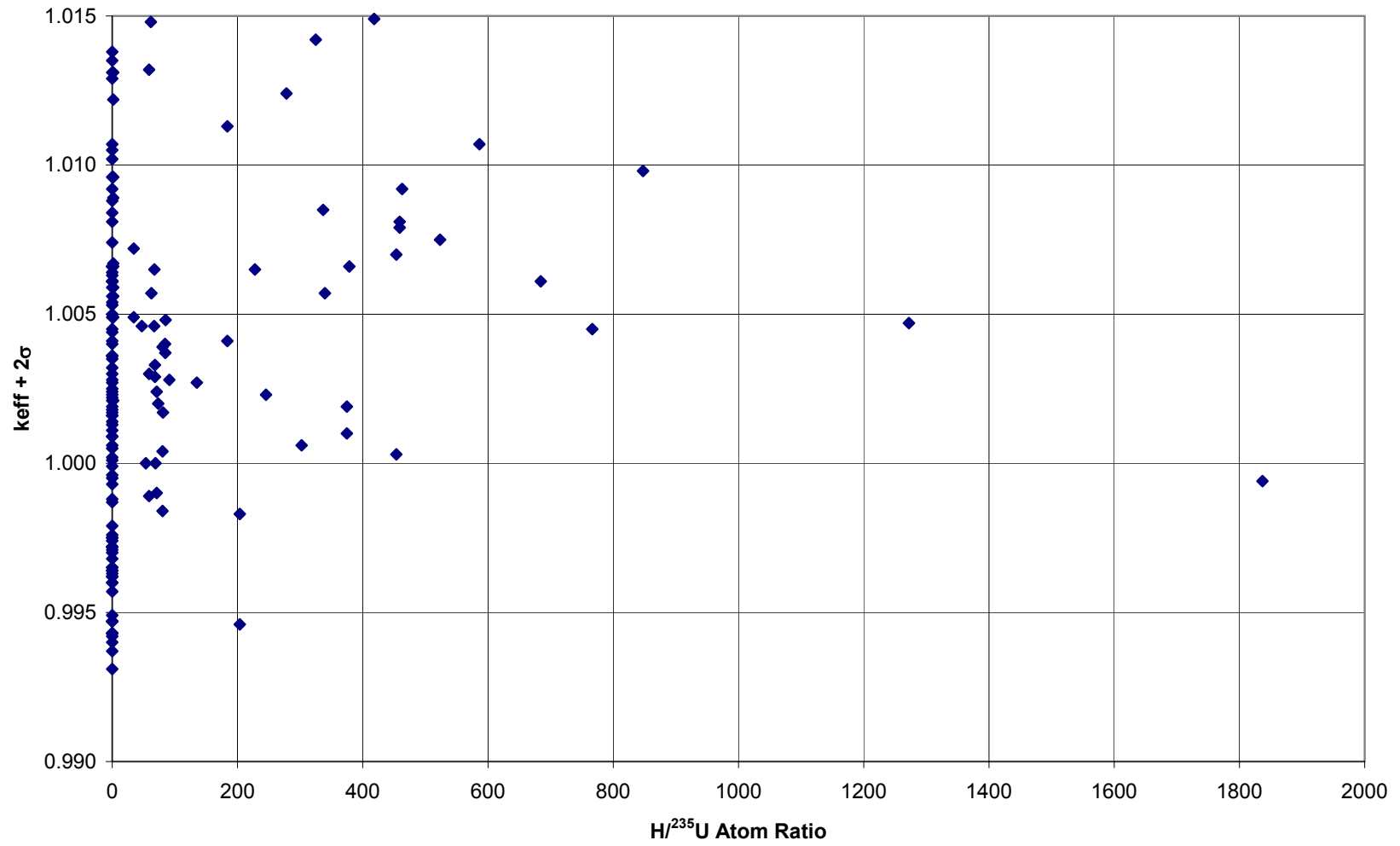


Figure 7, Plot of the k_{eff} with the Moderator-to-Fissile atom ratio (H/²³⁵U).

SCALE 4.4a Validation of KENO V.a for HEU Systems

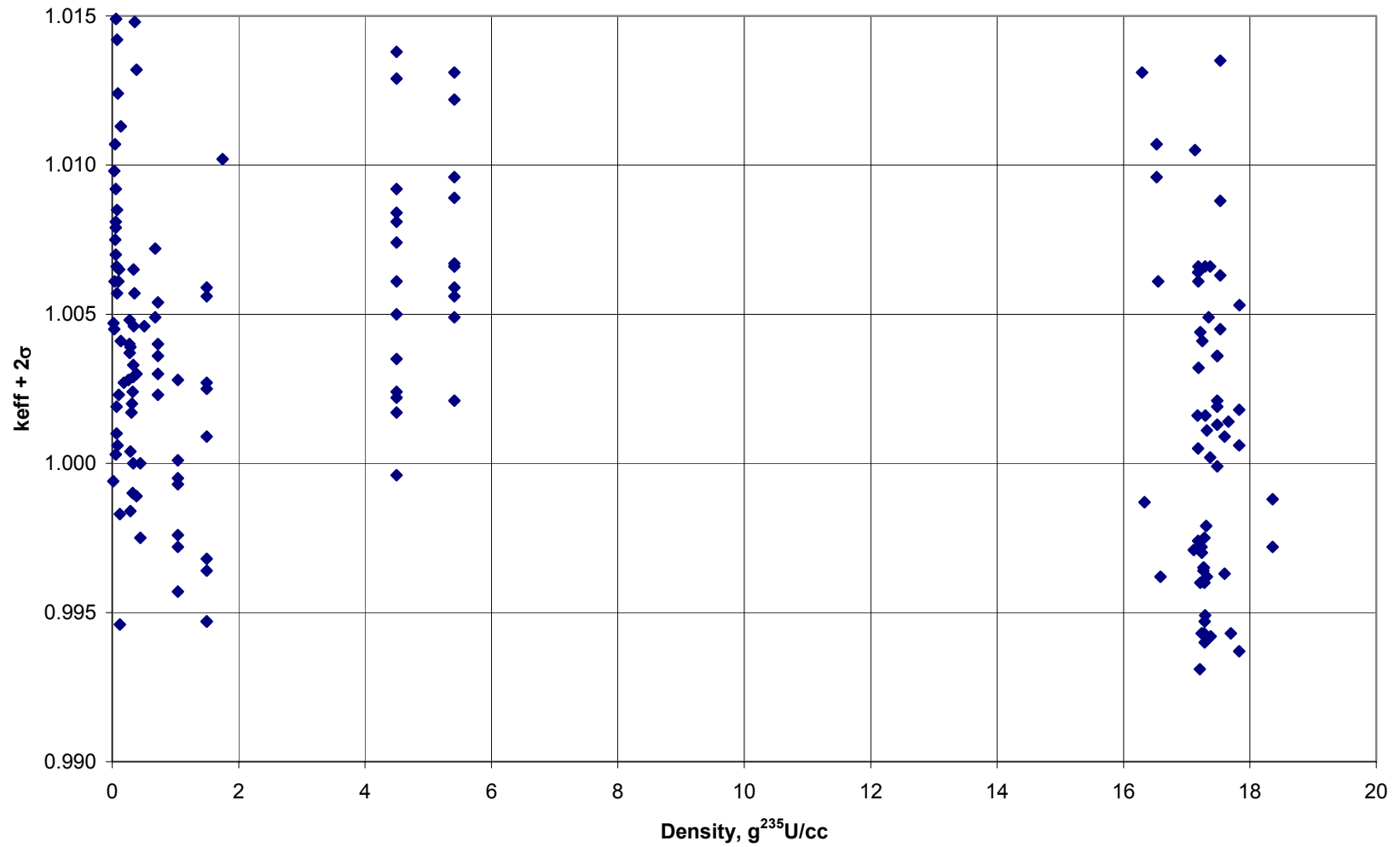


Figure 8, Plot of k_{eff} with the Fissile Density ($g^{235}U/cc$)

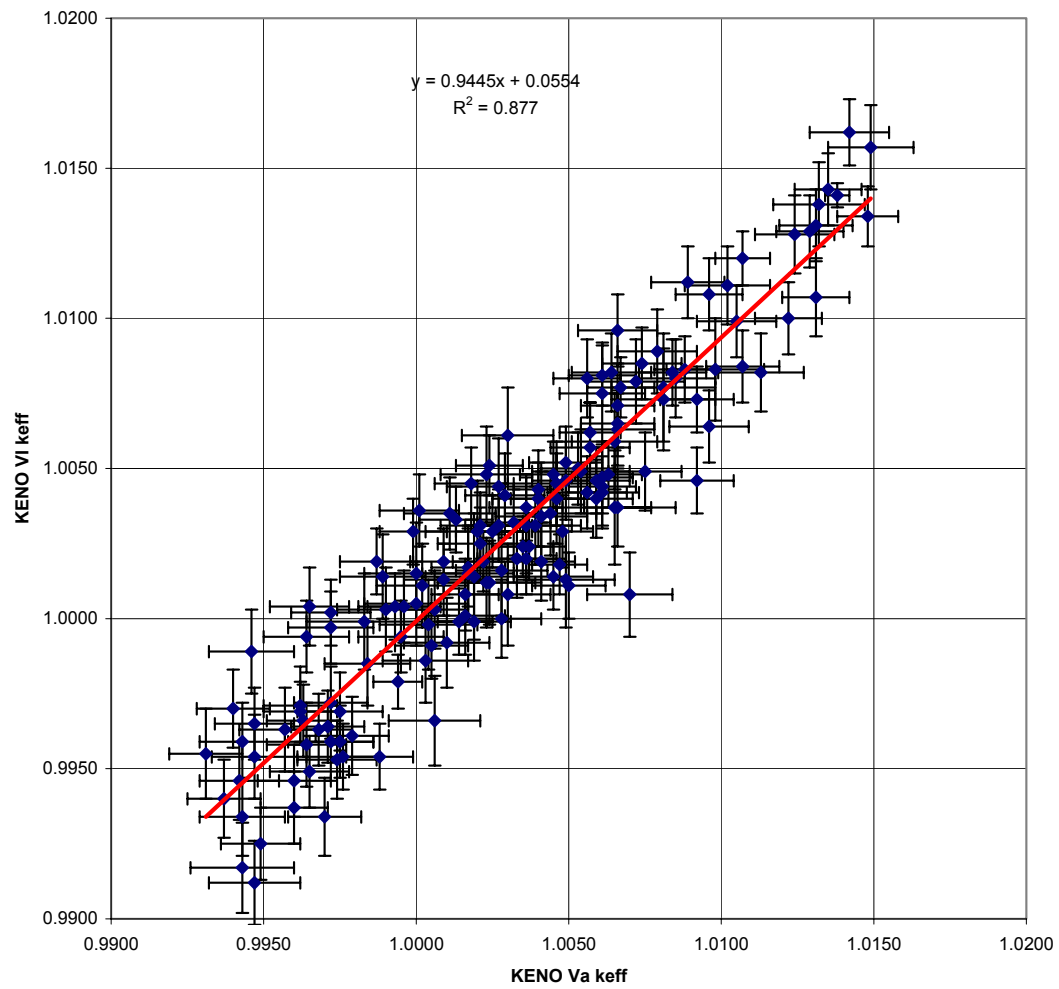


Figure 9, Plot of KENO VI k_{eff} with the KENO Va k_{eff}

APPENDIX A

SCALE INPUT CASES FOR DATA SETS 1 THROUGH 161 CRITICAL EXPERIMENTS

(This information available in electronic media only)