

Calculation No: CDQ000020080014

Attachment A18-3

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TAILWATER HEADS
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Calculation No: CDQ000020080014

Attachment A18-6

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Tailwater Heads

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Calculation No: CDQ000020080014

Attachment A18-13

Tailwater Heads $6.0.$ Proto = 29,0486'

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Attachment A18-17

TAILWATER HEADS
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Tailwater Heads

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HORE AMERICAN SOCIETY OF CIVIL ENGINEERS **3. FREE EARTH-SUPPORT AMERICAN SOCIETY OF CIVIL ENGINEERS**

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3. Free earth support analyses which compensate for toe fixity by included and the second of the second of the misleading; fixed earth Founded November 5. 1852 ing a bending moment reduction factor are liable to be misieading; uxed early and the suitable of product of practical design and the support methods should always be used. TRANSACTIONS

4. Design analyses should be suitable for practical design use. In view of soil properties, design computations should not depend on arithmetical accu-
soil properties, design computations should not depend on arithmetical accu-
Paper No. 2677 vol. 119, 1154 racy to several decimal places.

RATING CURVES FOR FLOW OVER DRUM GATES

BY JOSEPH N. BRADLEY,¹ A. M. ASCE

WITu DISCUSSION *BY* MESSRS. GUIDO Wyss; **SAM** SHtULITS; Bon BUEHLER; F. B. *CAMPBJELL AND* A. A. **MCCOOL;** *AND* JOSEPH *N.* BRADLEY

SYNOPSIS
With water becoming more valuable in the western states each year, there is
an increasing demand for better methods of measurement and additional
rating structures. This condition applies not only to the requireme me_t main canals and laterals of irrigation works but also to the regulation a
measurement of flow at dams. In fact, the need has reached the point
which operators are desirous of metering the flow at nearly all control devi
in

clude spillways, with or without gates; outlet works for dams using gates or station as well as that of a regulating device. Examples of such structures in-
clude spillways, with or without gates; outlet works for dams using gates or
valves; and canal regulating structures using gates. With the acc valves; and canal regulating structures using gates. With the accumulat
of information from hydraulic model studies made by the Bureau of Reclan
tion (USBR), United States Department of the Interior, it is now possible
pre

of a spillway.

Nors.—Published, essentially as printed here, in February, 1953, as *Proceedings-Separate No. 169*,

Positions and titles given are those in effect when the paper or discussion was received for publication. ¹ Hydr. Engr., Bureau of Reclamation, U.S. Dept. of the Interior, Denver, Colo.

DRUM GATES **⁴⁰⁵**

sec-ft, is questionable. Measurement of the flow over the drum gates, which is sec-ft, is questionable. Measurement of the flow over the drum gates, which is
now possible, would have afforded a continuous record and one that would be
as accurate for floods as for normal flows. for floods

CHARACTERISTICS OF **THE** *DitRUM* **GATE**

a curved upstream As a measuring device, the drum gate resembles a sharp-crested weir with As a measuring device, the drum gate resembles a sharp-crested weir with a curved upstream face over the greater part of its travel. With an adequate positioning indicator, the drum gate can serve as a very estimated to th positioning indicator, the drum gate can serve as a very satisfactory metering

When the drum gate simulates a sharp-crested weir-that is, when a line the horizontal, as in Fig. 2(a), four principal factors are involved. These factors
are H, the total hoad above the kind in the contractors are involved. These factors drawn tangent to the downstream lip of the gate makes a positive angle with are H , the total head above line drawn tangent to the the radius of the gate or an equivalent radius, should the curvature of the

gate involve a parabola; and C_q , the coefficient of discharge in $Q = C_q L H^{\dagger}$, which Q is the discharge in second-feet, and L is the length of the gate.
The depth of second-feet, and L is the length of the gate.

installations Find approach was not included as a variable because drum-gate.
studied were for medium and it is in a variable because drum-gate installations studied were for medium and high dams at which approach effect
were negligible. When the approach doubt were negligible. When the approach depth, measured below the high point of the gate, is equal to or greater than \pm . of the gate, is equal to or greater than twice the head on the gate, it has been
shown' that a further increase in approach dead, it has been shown's that a further increase in approach depth produces very little increase in the coefficient of discharge. Most drum-gate installations satisfy this condition, especially when the gate is in a spiral during the sati adequate approach depth condition, especially when the gate is in a raised position. Therefore, with adequate approach depth the four variables H , θ , r , and C_q completely define the flow over this type of gate for positive angles of θ adequate approach depth the four variables H , θ , r , and C_g completely defined the flow over this type of gate for position.

For negative values of θ , Fig. 2(b), the downstream lip of the gate no longer controls the flow. Rather, the control point shifts upstream to the vicinity of the high point of the gate for each setting as illustrated in Fig. 2(c), and
flow conditions gradually approach those of the free crest (as the gate is
lowered). Although other factors enter the problem, the similitude lowered). Although other factors enter the problem, the similitude also holds

of Reclamation, U. S. Dept. of the Interior, Denver, Colo., 1948. IDENTIFY CODE CALLY AND PERMISSION Bureau

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INTRODUCTION

The drum gate is a type of gate that floats in a chamber and is buoyed into
position by regulating the water level in that chamber. A medium-sized gate
of this type is shown in Fig. 1. To use drum gates as metering device

rating a drum gate consists of the over-all dimensions of the gate and overflow
crest, the information contained in this paper, and the coefficient of discharge

Flo. I.--DRuM **GATE. 100** FT By 16 FT. **AT** IlooVEw DA.% (AMIZo.A-NEvAOA)

for any appreciable head on the spillway with the gate in the completely lowered
position. Should the coefficient data be lacking, the coefficient of discharge
for the designed head can be estimated for nearly any overflow

charge and (2) in time of flood, the gaging station may be out of order but the gate calibration is as accurate as usual. The flood that passed over Grand Coulee Dam (Washington) in 1948 is an example. The river gage, in the pier of a bridge downstream, was in error because of a drawdown in the water surface, adjacent to the pier, at the higher flows. Current-meter measurements were also attempted during the flood, but the swiftness of the current and other difficulties rendered these only partially successful. As a result, the discharge at the peak of. the flood, which was finally estimated as 638,000

Monography Sections for Irregular Overfall Spillway Sections, "by J. N. Bradley, Engineering"
 Monography Sections, Denverally Reclamation, U.S. Denver. Colo., March, 1952.

VRUM GATES **0**

Bazin, in his classical experiments, studied inclined sharp-crested weirs.⁴ The angle of the weir was varied in increments from 14° to 90° with the horizontal, and each weir was 3.7 ft high (vertical dimension). The head on the crest of the weirs ranged from 0.32 ft to 1.48 ft. The results, presented in Fig. 4, $s_{\text{now } \theta}$ plotted ngainst the Bazin coefficient, C_b (in the formula, $Q = C_b L \hat{h}$ $\sqrt{2 g h}$, in which h does not include the velocity head of approach (h_a) . The

FIG. 3.-EXAMPLES OF DRUM-GATE CROSS SECTION

angle θ is also plotted with respect to C_{ϵ} (in the expression, $Q = C_{\epsilon} L H^{\dagger}$) in which H is the total head. This latter expression will be used throughout

By reference to Fig. 4 it can be observed (1) that the coefficient, C_q , varies only slightly with the observed head on the weir, (2) that there is a rather

⁴ 'Recent Experiments on the Flow of Water over Weirs," by H. Bazin, Annales des Ponts et Chaussée.
October, 1888. (Translation by Arthur Marichal and John C. Trautwine, Jr., Proceedings, Engineers

SOURCES OF INFORMATION

The data for this drum-gate study were obtained from hydraulic models of various sizes and scales. The experiments were performed over a period of about eighteen years. The spillway drum gates tested, the principal dimensions of each, the model scale, the laboratory where the tests were conducted, and other information are given in Table **1.** Gates for the first three dams

TABLE 1.-PRINCIPAL DIMENSIONS OF DRUM GATES TESTED

.= Gate down. **I** Refers to the **shape** of the spillway cross section.

listed in the table-Grand Coulee Dam (Waslhington), Bhakra Dam (India), and Shasta Dam (California)—are identical except for the length and number. The models of each were tested at different times by different personnel. The results of the tests are nearly identical, which fact indicates the consistency possible in this type of test. Although identical gates are of value in indicating the consistency of results, test results on dissimilar gates are desirable because they can give assurance that all factors involved in the establishment of similitude have been considered. The study includes only eleven gates (Table 1), but the dimensions of these vary over a fairly wide range, and the consistency indicated in compiling the results was quite satisfactory.

Cross sections of representative examples of the spillway overflow sections and drum.gates listed in. Table **I** are shown in Fig. 3. For Hoover Dam, Shape 4-M3 is shown. The data relating the coefficient, C_q , to the head for the model drum gates tested are tabulated in Table 2.

RESULTS OF BAZIN ON STRAIGHT INCLINED WEIRS

The straight inclined weir is comparable to a drum gate, having infinite radius, thus the results of Bazin serve as an introduction to this study.

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DRUM GATES

DRUM GATES

TABLE 2.-DRUM-GATE COEFFICIENTS"

TABLE 2.9 -(Continued)

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sharp reversal in the curve when the angle θ approaches 28°, and (3) that the coefficient of discharge is a maximum at this angle. As the angle θ is increased from 28° to 90°, contraction of the jet gradually reduces the coefficient to approximately 3.33, which occurs when the weir is vertical. As θ is decreased from 28° to 0° the coefficient is gradually reduced—either by approach conditions, friction, or both-to that for a broad-crested weir, which may be some value between 2.8 and 3.1. As the principal difference between the drum gate and the straight inclined weir lies in the curvature of the gate, the trends for the two should be similar.

An inconsistency exists in Fig. 4-namely, the coefficient of discharge for a vertical sharp-crested weir should approximate 3.33, but Fig. 4 shows that Bazin obtained 3.45. This conclusion is supported by the fact that the USBR, Ernest W. Schoder, M.ASCE, and Kenneth B. Turner,⁵ and others have not

⁴"Precise Weir Measurements," by Ernest W. Schoder and Kenneth B. Turner, Transactions, ASCE, Vol. 93, 1929, p. 999.

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and values are not so important for the case at hand as is the significance at hand as is the significance ϵ $\frac{1}{2}$ the trend. actual values are not so important for the case at hand as is the significance

The method for combining results from the eleven drum gates tested The method for combining results from the eleven drum gates tested The method for combining results from the electron critical separately
(Table 2) consisted of first plotting the coefficient of discharge data separately

for each gate as illustrated by the sheet for the Shasta Dam gate (Fig. 5). With the coefficient of discharge as the abscissa and H/r as the ordinate, each curve in Fig. 5 represents a different gate angle θ , which the tangent to the downstre lip of the gate makes with the horizontal. In all cases, H is the

total head, including the velocity head of approach, measured above the hig
point of the gate, and r is the radius of the gate. In Fig. 5, C_q is based on the
relationship $Q = C L H$. For positive velocies of 8, the best wa point of the gate, and r is the radius of the gate. In Fig. 5, C_a is based on the the set relationship, $Q = C_q L H^1$. For positive values of θ , the head was measure above the lip of the gate, whereas for negative angles it was observed above the lip of the gate, whereas for negative angles it was observed abo

Included a sillustrated in Fig. 2.

head is illustrated in Fig. 2.

Upon completion of a similar set of curves for each gate tested, the eleven

of a similar set of curves for each gate tested, the eleven From the various gates showed good general agreement; and the curves in Fig. 6 constitute the general experimental information needed for the discharge coefficients in Fig. 6 constitute the general experimental information The results from the various gates showed good general agreement; and the curves in Fig. 6 constitute the general experimental information needed for determining the discharge coefficients for gates in raised or partly raised positions. The supporting points are not shown in Fig. 6, but the indi information for each gate is listed in Table 2.

ANALYSIS OF TEST RESULTS

ANALYSIS OF TEST RESULTS
The curves in Fig. 6 show a tendency toward reversal, similar to that _{the curve}
6 bibited by $e = 26$ hibited by the Bazin curve in Fig. 4, but the points of inflection vary fre $\theta = 20^{\circ}$ to $\theta = 30^{\circ}$, depending on the value of H/r . Fig. 4 showed the efficients to vary only slightly with the head. but in this case efficients to vary only slightly with the head, but in this case the coefficients definitely vary with the head. definitely vary with the head.
A metter of significance is the reversel of the (H/r) -order which occurs

29° (Fig. 6). The coefficient of discharge has but one value, 3.88, when θ
29° (Fig. 6). The coefficient of discharge has but one value, 3.88, when θ matter of significance is the reversal of the (H/r) -order which occurs ig. 6). The coefficient of discharge has but one value, 3.88, when θ proximates 29°; thus it is insensitive to both the radius and the head on proximates 25, thus, it is insensitive to both the radius and the nead on
gate for this angle. The curve for $H/r = 0$ approximates a drum gate
infinite radius and was obtained from the data of Bazin (Fig. 4) by any infinite radius and was obtained from the data of Bazin (Fig. 4) by applying a uniform adjustment.

As stated previously, similitude is valid for small negative angles of θ , as and As stated previously, similitude is valid for small negative angles of the as for positive angles up to 90°; thus, the curves in Fig. 6 are sh and recommended for use down to $\theta = -15^{\circ}$. As the gate is lowered bey this this angle, the curves double back and converge, finally terminating in the free flow coefficient.

free flow coefficient.
The discharge coefficients in the region between $\theta = -15^{\circ}$ and the generalistic down are determined by graphical interpolation. Interpolation completely down are determined by graphical interpolation. Interpolation is $\frac{\text{acconv}}{160}$ accomplished by plotting head-discharge curves for several gate angles between plotted for the free crest. This information is then cross-plotted to obtain values in the transition zone. The method will be explained in the example that follows. It will be discovered that negative angles greater than operator's standpoint, as a change in gate position has little effect on the dis-(with the exception of the free crest) are not particularly important from an

It. must be assumed that the coefficient of discharge is known for at least one value of the head on the free crest (gate completely down) for the partic- ~ 1 ular spillway under consideration. With the coefficient known for one or more heads, the complete coefficient curve for the free crest can be plotted by consulting Fig. 7, in which H_o and C_o are the designed head and

 $\label{eq:2.1} \frac{d}{dt} \sum_{i=1}^N \frac{d}{dt} \left(\frac{d}{dt} \right) \left(\frac{d}{dt} \right) \left(\frac{d}{dt} \right) \left(\frac{d}{dt} \right)$

illustrated in Table 3, and the head-cocificient curve for free for free flow (gate down), and for free flow (gate down), and the head-cocificient curve for free flow (gate down), and the set of the set of the set of the s

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and $C_0 = 3.48$ is constructed by arbitrarily assuming several values of H/H_0 . and reading the corresponding values of C/C, from Fig. 7. The method is illustrated in Table 3, and the head-coefficient curve for free flow (gate down), obtained in this manner, is shown in Fig. 10.

Fig. 9.-SPILLWAY CREST DETAIL, BLACK CANTON DAM IN IDANO

for the designed head, respectively. This chart was reproduced from a previous publication 2 and represents a curve well supported by tests of some fifty α supported by tests of some fifth α

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From the plan and second of the lower in
 $\begin{array}{c}\n\text{From the plan and second or second in}\n\hline\n\text{flown in}\n\hline\n\text{Gayon} \quad \text{Diversion} \quad \text{Dam (Idaho), shown in}\n\end{array}$ Figs. 8 and 9, assume that it becomes neces-0.3 cator is calibrated to show the elevation of 0.2 the high point of the gate, and the gate has a 0.5 and the gate of the gate position indicated to show the elevation of o . . . long. The coeflicient of discharge for the free o.3 the high point of the gate, and the gate has a c. **3.48 for the case of 21.0** ft. The gate is 64 ft. constant radius of 21.0 ft. The gate is 64 ft **Fig. 7.3. Fla. 7.4. Fla. Fla.** $\frac{10}{10.7}$ **10. 100K 10 one one outlined of** 14.5 ft. Flow cress is $\frac{G}{C_g}$ consulting for $\frac{G}{T}$ for $\frac{14.5 \text{ ft}}{14.5 \text{ ft}}$ by consulting Fig. 7. The free-flow of discharge known and $\frac{1}{T}$

coefficient of Curve for Canyon Cultum Canyon. The coefficient of discharge knot
Example for Black Canyon Designed Band from a few at the designed head, the entire flow coefficient curve can be established by consulting Fig. ... The real flow coefficient curve for Black Canyon Dam spillway (for which $H_o = 14.5$ ft

DRUM GATES

DRUM GATES $B_{\rm eff}$ considering the spinlar values in rating of the spinlar values in raised positions, μ

Before considering the rating of the spillway with gates in raised positions, it is necessary to construct a diagram such as that shown in Fig. 11 to relate. gate elevation to the angle θ for the Black Canyon Dam gate. The tabulation in Fig. 11 shows the angle θ for corresponding elevations of the downstream lip

of the gate at intervals of 2 ft.

Beginning with the maximum positive angle of the gate, which is 34.883° , the computations may be begun by choosing $\begin{array}{ccc} \hline \text{16} & \text{...} \\ \hline \end{array}$ a representative number of reservoir ele- $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ vations as indicated in Col. 2, Table 4. 12 vation and the high point of the gate vation and the high point of the gate (which is the downstream lip in this case) constitutes the total head on the gate, and values of head are recorded in Col. 3. the radius of the gate, which is 21.0 ft.

Entering the curves in Fig. 6 with the values in Col. 4, Table 4, for $\theta =$ $+34.883$ °, the discharge coefficients, listed in Col. 5 of the set of computations designated "A." are obtained. The remainder 3.0 3.4 3.8 of the procedure outlined in Cols. 6 and **2.6 3.0 3.4 3.8 of the procedure outlined in Cols. 6 and Coefficient**, C_q **7.** Table 4, consists of computing the dis-FIG. 10.-HEAD-COEFFICIENT CURVE, charge for one gate from the expression, BLACK CANYON DAM, IN IDAHO $Q = C_a L H¹$. A similar procedure of

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computation is repeated for other positive angles of θ as in sets B , C, and D
Table 4.

Table 4.
As the angle θ is given negative values, the procedure for determining the discharge remains the same for angles between 0 and -15° , except that the head on the gate is measured above the high point rather than above the lip. Discharge computations for negative angles of the gate down to -15.0 are tabulated in E, F, and G of Table 4.

are tabulated in E, F, and G of Table 4.
Plotting values of discharge, reservoir elevation, and gate elevation from Table 4 results in the seven curves in Fig. 12 for which the points are denoted by circles. The extreme lower curve, on which the points are identified by x-marks, represents the discharge of the free crest with the gate completely down. The latter values were obtained from Table 3.

The discharge values shown in Fig. 12 are for one gate only. When more than one gate is in operation, the discharges from the separate gates may be totaled providing the gates are each raised the same amount. The experimental models contained from one to four gates (with the exception of that of Grand Coulee Dam, which contained eleven) so a reasonable allowance for pier effect on the discharge is already present in the results.

The intervals between the eight curves identified by points (Fig. 12) are too great for rating purposes, especially the gap between gate elevations, 2485.75 ft and 2482.5 ft. This is remedied by cross-plotting the eight curves t for result is a straight-line value of discharge. The straight-line value of discharge. The t for various constant values of the discharge as shown in Fig. 13. Fortuna the result is a straight-line variation for any constant value of discharge. The lines in Fig. 13 are not quite parallel and there is no assurance that they will be straight for every drum gate. Nevertheless, this will not detract appreci-

Fig. 11.-RELATIONSHIP OF GATE ELEVATION TO ANGLE θ t_{max} to construct the additional curves are additional curves

ably from the accuracy obtained. Interpolated information from Fig. 13 then utilized to construct the additional curves in Fig. 12. If all curves are considered, Fig. 12 shows the completed rating for the Black Canyon Dam spillway for 0.5-ft gate intervals. For intermediate values, straight-line interpolation is permissible.

$T_{\rm eff}$ and $T_{\rm eff}$ and $T_{\rm eff}$ are demonstrated how an existing control structure, such as α the Black Conclusions Conclusions spill was a rating station. The serve as a rating station. The serve as a rating station. The serve as a rating station of the serve as a rating station. The serve as a rating station. The

This paper has demonstrated how an existing control structure, such the $PL \times G$ the Black Canyon Dam spillway, can also serve as a rating station. The accuracy of rating curves obtained by the method is estimated to approach that of an average current-meter traverse of the river providing that (1) the gate position indicators are made as large as possible and are accurately cali-

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brated, (2) the reservoir gage can be read to within 0.05 ft, (3) nearly atmospheric pressure exists under the sheet of water after it springs from the gate. and (4) all gates are set at approximately the same elevation.

TABLE 4.-HEAD AND DISCHARGE COMPUTATIONS FOR DRUM GATES IN RAISED POSITIONS

¹⁶ In connection with provision (3), the blunt piers on the Black Canyon Dam spillway, Figs. 8 and 9, provide effective aeration under the overfalling sheet of water for all but very small heads with gate completely raised. In the case of provision (4), uniform operation of the gates is also most desirable from the standpoint of stilling basin operation for minimum erosion downstream.

Discharge measurements on the prototype are desirable whenever possible as a check on the accuracy of the foregoing method. Sufficient observations should be taken, however, to establish the fact that the prototype information is consistent and reliable.

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Fla. 13.---Cuoee-PL0rTED **INrrI.L** RATINO CunvEs, BLACK **CANYON DAM IN IDAHO**

Elevation of High Point of Gate, in Feet

ACKNOWLEDGMENTS

The writer wishes to thank C. E. Blee, M. ASCE, chief engineer of the Tennessee Valley Authority for the use of the data on the Norris Dam Spill-' way; Hal Birkeland, M. ASCE, of the International Engineering Corporation, for obtaining permission to include the Bhakra and Capilano Dam spillways in the paper; and the chief engineer of the Panama Canal for use of the data on the Madden Dam spillway. The writer is also grateful to the Bureau of Reclamation for the use of the remainder of the experimental information. He also wishes to thank his engineering associates, H. M. Martin, M. ASCE, D. J. Hebert, and A. J. Peterka, A. M. ASCE, for their most helpful comments and suggestions.

D.I SCUSS ION

Guino Wyss^s.—The information presented by Mr. Bradley is of utmost value for determining the quantities of discharge over drum gates under various heads for any gate position. This information will permit operators in the **field** to adjust the gate position from corresponding chart values in such a manner as to obtain the desired flow. The use of drum gates as an actual metering device for spillway quantity discharges is unique and the results obtained are more practicable and reliable than those obtained by stream gaging, especially when this gaging is conducted during periods of high floods.

It wouhl have been interesting if the author had presented an investigation of the flow, profiles of the upper and lower nappe surfaces, as well as the actual water pressures on the upstream plate of the drum gate by use of charts. This wouhl afford an opportunity to obtain the true loading conditions on the gate during the cycle of operation front fully-raised gate to fully-lowered gate. This information would be important in the (letermination of the buoyancy and loading criteria of the gate structure.

SAM SHULITS,⁷ M. ASCE.--An outstanding contribution to the design and operation of drum gates has been presented in this report of the author's work at the USBR. The paper and its complement² fill a great need.

Since 1928, when the Freeman Scholarships were established, there has been a tremendous development of hydraulic model research in the laboratories of the United States. Although these laboratories are unexcelled in size and quality, many hydraulic engineers have pondered the procession of models (spillways, stilling pools, and river reaches) in the period from 1928 to 1953 with few, if any, summaries or proposals for design to reduce the dependence on models. In MIr. Bradley's work there is strong evidence that the laboratories will produce correlations and syntheses-not more models.

When it is realized that many of the most famous and productive laboratories in the United States did not exist prior to 1928, the lack of correlation and synthesis for general use is understandable. The hope is that other works of similar quality will be added to engineering literature.

Bon BUEHLER,⁸ A. M. ASCE.—An interesting and clever use of data has resulted in a method by which records of gate settings at dams can be made a substitute for missing stream-flow records and can be used to augment existing records. The construction of a dam and reservoir often floods an established stream gage. Unless the gage is replaced below, the dam or upstream from the reservoir, subsequent stream flow usually is not accurately known. Sometimes a Series of damns (each causing the water to back up to the dam above) prevents continuing established gages at the strategic points where they had been

4 Mech. Engr., Bureau of Reclamation, **U. S.** Dept. of the Interior, Denver, **Colo.** IAssociate Prof., Director, Hydr. **Lab.,** Civ. **Eng.** Dept., Pennsylvania State College, State College, Pa-

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t Associate Frot., Director, Hydr. Lab., Civ. Eng. Dept., Fennsylvania State College, S
8 Hydr. Engr., TVA, Knoxville, Tenn.

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located. The less accurate-and more costly-slope stations are not completely satisfactory alternatives to the single-line rating stations.

If the spillway of a dam can be rated with an accuracy comparable to the accuracy obtainable with a gage (as demonstrated by Mr. Bradley for certnin spillway types), and if allowance is made for flow through other water outlets such as turbines, locks, and sluices, the structure is then superior in some respects to the gage. For example, the rating of the dam should be permanent; whereas the rating of a gage usually requires frequent checking.

^IMr. Bradley's method for rating drum gates not only allows records for ordinary stream flow to be supplemented, but also probably gives a more accurate determination of extreme flood rates than do most gages. lIe has made an important contribution to the planning and design of druin-gated structures.

The author has presented a method for rating a spillway at all heads provided the coefficient for one appreciable head is known. He also states that a coefficient for the designed head can be estimated for most spillways by a method previously published.2 The writer, on the other hand, offers a method by which an ogee spillway can be rated, provided its profile shape is known. The method is based on an equation derived by R. N. Brudenell, A. M. ASCE, incidental to studies made on radial gates.9 Mr. Brudenell's equation is

$$
Q = \frac{3.97 L H^{1.62}}{H^{0.12} D} \dots (1)
$$

in which Q is the spillway discharge, in cubic feet per second; L denotes the length of the spillway, in feet; H is the total head on the spillway crest, in feet;

TABLE 5.-FREE DISCHARGES FOR BLACK CANYON DAM IN **IDAIIO**

 \therefore **From Col. 6. Table 3. b** Head at which $C_6 = 3.48$. $\degree C_6$ would be 3.466 for this discharge.

and H_D represents the design head in feet. The design head is that head which produces a standard lower nappe that agrees closely with the spillway profile.

"Flow over Rounded Crests," by R. N. Brudenell. Engineerino News-Record, July 18, 1935, **p. 96.**

Eq. 1 was intended to be used with heads greater than $H_D/4$, although equation has been found to agree closely with model data for somewhat lower heads. Without knowing any coefficients. Eq. 1 gives discharges that agree closely with those obtained by Mr. Bradley for Black Canyon Dam. In the case of Black Canvon Dam. Mr. Bradlev used one known coefficient and the curve of Fig. 7. Free-flow discharges computed by the two methods are shown in Cols. 2 and 3, Table 5. The procedure by which Eq. 1 was applied will be described subsequently.

It is assumed that in choosing Black Canyon Dam for his example.

It is assumed that in choosing Black Canyon Dam for his example the author knew that his method would yield discharges close to known values. The good agreement for all except the low heads shows that, in this example, Eq. 1 (using only the shape of the spillway) also produces suitable results.

The solid-line curve in Fig. 14 also was tested in this manner. The same coefficient at each project was assumed to be known as when the curve in Fig. 7 was tested. Col. 8, Table 6, shows that for appreciable heads the maxi-

mum error is slightly more than 2% (Madden Dam).

cr = **3,97 Ill** W **-**` **.........** . . .(3) ... These comparisons show that the direct application of Eq. 1, Fig. 7 (or

TABLE 6.-COMPARISON OF FREE-FLOW SPILLWAY COEFFICIENTS

Total head, in fect	Coefficient obtained from model test	Using Eq. 1		Using Fig. 7		Usino Fig. 14	
		\boldsymbol{c}_\bullet	Difference. in percent	\boldsymbol{c}_{\bullet}	Difference. in percent	c_{\bullet}	Difference, in percent
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
			GRAND COULER DAM (WASHINGTON)				
35 30 25 20 15 10 5	3.920 3.842 3.745 3.635 3.510 3.352 3.220			3.914 3.831 3.745* 3.655 3.550 3.370 3.138	-0.15 -0.29 0 $+0.55$ $+1.14$ 0.54 × 2.54	3.902 3.827 $3.745*$ 3.651 3.524 3.356 3.168	-0.46 -0.39 0 $+0.44$ +0.40 +0.12 -1.62
			BHAKRA DAM (INDIA)				
$\frac{28}{23}$ 18 Ī3 $\frac{8}{3}$	3.680 3.645 3.550 3.420 3.275 3.120			3.730 $3.645 -$ 3.547 3.434 3.215 2.748.	$+1.52$ 0 0.08 $+$ 0.41 1.83 -11.92	3.732 3.045* 3.543 3.404 3.208 2.854	$+1.41$ 0 -0.20 -0.47 -2.04 -8.53
			SHASTA DAM (CALIFORNIA)				
$\frac{38}{33}$ 28 23 18 13 8 ×.	3.895 3.835 3.760 3.675 3.575 3.465 3.335			3.910 3.839 3.760* 3.677 3.591 3.455 3.215	$_{+~0.10}^{+~0.39}$ 0 0.05 + ∔. 0.45 0.29 3.60	3.899 3.831 $3.760*$ 3.074 3.568 3.429 3.230	+0.10 -0.10 $\bf{0}$ -0.03 -0.20 -1.04 -3.15
			HAMILTON D_{AM} (TEXAS) $H_D = 52$ FT				
$\frac{35}{30}$ 25 20 15 10 5	3.710 3.645 3.580 3.500 3.400 3.290 3.160	3.785 3.716 3.635 3.539 3.420 3.258 2.997	$+2.02$ +1.95 $+1.54$ +1.11 $+0.59$ -0.97 -5.16	3.741 3.662 3.580* 3.494 3.394 3.222 3.000	0.84 ÷ $+0.47$ 0 0.17 0.18 2.07 5.06	3.730 3.659 3.580* 3.490 3.369 3.208 3.029	$+0.54$ $+0.38$ 0 -0.29 -0.91 -2.50 -4.14
			FRIANT DAM (CALIFORNIA)				
20 17 14 11 8 s 2	3.650 3.625 3.550 3.460 3.340 3.175 2.065			3.717 3.639 3.550 ^a 3.458 3.348 3.142 2.723	+ 1.84 0.39 0 0.06 0.24 t 1.04 -8.15	3.706 3.632 $3.550 +$ -3.452 3.319 3.131 2.812	$+1.53$ $+0.19$ 0 -0.23 -0.63 -1.38 -5.16

This government suggests, there must be a constant there are must be a constant of the must

 \mathbf{r} and \mathbf{r} and \mathbf{r} and \mathbf{r} and \mathbf{r} and \mathbf{r} are derived from \mathbf{r} and \mathbf{r} and \mathbf{r} are \mathbf{r} and \mathbf{r} and \mathbf{r} are \mathbf{r} and \mathbf{r} are \mathbf{r} and \mathbf{r} are This good agreement suggests, too, that there must be a close relation Γ between the curve in Fig. *i* and a similar out to show the comparison of the comparison of Γ by using

and Eq. 1, from which

$$
C_q = \frac{3.97 \ H^{1.62}}{H^{0.12} D \ H^{3/2}} \dots \dots \dots \dots \dots \dots \dots \tag{3}
$$

The design head, H_D , was found (by a method to be described subsequently) The design hea Dam, and this value was used in making \ldots Thus, for $H_D = 45$ ft,

$$
C_{q} = \frac{2.5143 \; H^{1.62}}{H^{3/2}} \cdots \cdots \cdots \cdots \cdots \cdots \cdots \qquad (4)
$$

responding Cq-values were computed. The resulting **C,** of **3.07** for a head of $\frac{1}{4}$ for several assumed values of total head, *H*, varying from 2 it to 58.5 ft, co. responding C_q -values were computed. The resulting C_q of 3.97 for a head of 45 ft (H_e) was taken arbitrarily as the known coefficient, C_e . Then the (II/H_e) -ratios and the (C_q/C_q) -ratios were computed for all other heads in the assumed range. The resulting curve is the solid line in Fig. 14. The dashed curve is from Fig. 7. The agreement is close-as expected. Still using H_D equal to 45 ft, the remainder of the process was repeated using the coefficient for the 25-ft head as C_0 , and then using the coefficient for the 12-ft head as C_0 . There was no discernible difference in the curves resulting from the three separate selections. A similar procedure, using H_D equal to 20 ft in Eq. 1, also showed no differences from Fig. 14. It can probably be proved that there should be no difference. was showed no difference.

The curve derived from Eq. 1 then was applied to the 1 way, assuming (as did the author) that the coefficient is 3.48 at a 14.5-ft head. The resultant free discharges are shown in Col. 5, Table 5.

The free-flow coefficients in Table 2 invite further comparisons with Eq. 1 for the four projects for which spillway profiles are given in Fig. 3. It should be remembered that this comparison tests the use of only the spillway shape as a guide to free discharge for the entire range of heads. Col. 4, Table 6, shows that for appreciable heads the maximum error in the four cases is approximately 2% (Hamilton Dam). Observed coefficients in model tests often scatter mately 2% (Hamilton Dam). Observed secretary \mathbb{F}_{int} , 7 for all elevents

as much.
The same coefficients permit testing the curve in Fig. 7 for all eleven agreement of the necessary to ass ways. This test is not as severe, however, because it is necessary to assume one known coefficient at which head agreement becomes perfect. At near-by higher and lower heads, large divergences would not be expected. Col. 6, Table 6, shows that for appreciable heads the maximum error is slightly greater than 2% (Hoover Dam, shape 8-M5). The base coefficient selected to obtain C_9 from the (C_9/C_9) -ratios is designated by a footnote for each project.
These arbitrary selections were made for medium high heads.

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charges for ogee dams at all but low heads. Eq. 1, applied directly to the spillway shape, has the advantage that no coefficients need be known or estimated in advance.

BURBER ON DRUM GATES well as when Fig. 7 is used. In most cases the errors are negative. In most cases the errors are negative. The
These theory are negative. The errors are negative. The errors are negative. The errors are negative. The expe

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The comparisons in Table 6 show a tendency toward errors of some importance at low heads when Eq. 1 or its companion curve in Fig. 14 is used, as well as when Fig. 7 is used. In most cases the errors are negative. These errors are of little concern in planning the safety of a structure against extreme floods, or in considering most other operations such as emptying the reservoir. The errors nonetheless affect the analytical rating of drum gates in the lowered or slightly raised positions. The free-flow coefficients help to determine the direction of the general curves at the large negative angles shown in Fig. 6. Free discharges form the base curve of the rating curves in Fig. 12 and help define the curvature of the low ends of the cross-plot curves in Fig. 13. Low to ordinary heads, corresponding to normal stream flow, can exist for a large part of the time at dams whose reservoir capacities are small. Further study of data for low heads might lead to valuable refinements.

Application of Eq. 1.—Since the factor H_D in Eq. 1 represents the head at which a standard lower nappe shape is a reasonable approximation of the spillway shape (as designed or built), it is only necessary to find this head to apply the formula. Spillway coordinates for a standard crest having a vertical upstream face have been used to find this head.¹⁰ These coordinates are shown in Table 7. The last column in Table 7 refers the horizontal (x) coordinates to the spillway crest because this form is the simplest to apply. In Table 7, *u* **10**, is the distance below the crest elevation.

Using these dimensionless coordinates, standard spillway shapes were plotted (Fig. 15) for values of H_D from 10 ft to 60 ft. In Fig. 15 negative

¹⁰ "Hydroelectric Handbook," by William P. Creager and Joel D. Justin, John Wiley & Sons, Inc., New York, N. Y., 2d Ed., 1950, p. 362.

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horizontal distances indicate the distance upstream from the crest. The spillway shape as designed or built is then drawn on transparent paper. This paper is laid over Fig. 15, and the value of H_D which gives the best fit is selected.
In deciding the best fit it may be found that the profile upstream from the crest. mundates one value and the downstate er of the two indicated values of H_D should be used. For example, H_D should be used. indicates one value and the downstream profile indicates a different value.

TABLE 7.-COORDINATES OF A STANDARD **SPILLWAY CREST**

the shape of Black Canyon Dam spillway upstream from the crest indicated a value of approximately 45 ft for H_D . The downstream shape indicated a value of approximately 25 ft. The larger value was used.

The determination of the H_D -value which gives a reasonable fit requires a certain amount of judgment. When the profile upstream from the crest is the criterion, the lip of the dam will sometimes be the determinant.

the

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Sometimes, however, the lip
droops sharply downward and indicates a lower value than other parts of
the upstream profile. When the downstream shape is the criterion, good results have been obtained by assigning a value of H_D based on the average fit in the zone between points on the spillway where tangents range from 20° to 35° from the horizontal. The exact value of H_D is not too important. Since it enters Eq. 1 in the 0.12 power, a difference of 10% in its value affects the discharge by only 1.15%.
The writer's application of Eq. 1 has been limited to fairly high dams,

Although the total head used in Eq. 1 should include the approach velocity, the accuracy of Eq. 1 when used for low dams, where approach velocity is large, has not been tested.

best fit was far as is known, the application of standard nappe shapes (for which discharge coefficients are known) to actual spillways on a basis of reasonable best fit was first suggested by W. M. Borlund.¹¹ Mr. Borlund used a curve of observed C_e -value plotted against H/H_e . In 1942, C. E. Kindsvater, M. ASCE, suggested a similar procedure in which the curve of C_e versus was derived from Eq. 1. Mr. Kindsvater's work (not published) should give results comparable to those obtained herein.

I'm material presented is regarded as an excellent check on that pr
Mr. Bradlay's work which relates to free discharge over an onee spillway Mr. Bradley's work which relates to free discharge over an ogee spillway

F. B. CAMPBELL,¹² M. ASCE, AND A. A. McCool,¹³ J. M. ASCE.—The experimental data on discharge coefficients for flow over drum gates are a wel-

 v Hydr. $\frac{1}{2}$ U. S. Waterways Experiment Station, Vicksburg, Miss.

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come nddition to the published information on flow over spillways, or the
servation and recording of the flow of streams. A paper by Robert E. Hortor
been a guide for the estimation of fl

affected by the radius of the skin plate, the elevation of the trunnion with
respect to the crest, and the location of the gate seat with respect to the axis
as well as the crest curvature. To complicate any investigations

partly raised drum gates.
The drum gate has the very attractive feature of requiring no mechanical
hoisting equipment for operation. Many of the dams constructed by the
USBR have spillways controlled by drum gates. For ex been developed principally by the USBR.
The discharge coefficients presented by the author are based on model

studies. There should be opportunity to check the coefficients for relatively low heads with partly raised gates in the prototype by current-meter met

It "Flow over Rounded Creat Weirs," by W. M. Borlund, thesis presented to the University of Coloration, at Boulder, Colo., in 1938, in partial fulfilment of the requirement for the degree of Master of Science. ¹³ Chf. Hydr. Engr., Analysis Brauch, Corps of Engrs., U. S. Waterways Experiment Station, Vicksburg, Miss.

¹⁴ "Weir Experiments, Coefficients and Formulas," by Robert E. Horton, *Water Supply and Iran and Cloque Clobert Clobert Clobert Clobert <i>Cloque Cloque Clobert by Robert Cloque Cloque Cloque Cloque Cloque Cloque Cloq* ¹⁴ "Weir Ex
Paper No. 200, b
15 of Paper No. 150 Paper No. 200, Coast and Geodetic Survey, U.S. Dept. of Commerce, Washington, D.C., 1907
of Paper No. 150).
And H. The Center Experiments on the Flow of Water over Weirs. The H. Basin, Annalysin, D.C., 1907.

October, 1888. (Translation by Arthur Marichal and John C. Trautwine, Jr., *Proceedings, Eng*
Club of Philadelphia, Pa., Vol. VII, No. 5, 1890, p. 259.)

¹⁷ "The Improvement of Rivers," by B. F. Thomas and D. A. Watt, John Wiley & Sons, Inc., New York, N. Y., 2d Ed., 1913.

⁴³⁰ O BRADLEY **ON** DRUM **GATES 0** ⁴³¹ CAMPBELL **AND MCCOOL ON DRUM OATES**

ments. Only on rare occasions with large floods is it possible to verify the ments. Only on rare occasions with large floods is it possible to verify the coefficients for high prototype heads over the drum gates in the lowered position.
The author's mention of the failure to obtain discharge measurements during
the 1948 flood over the Grand Coulee Dam spillway emphasizes th

to the becomes evident from a study of Table 2 that the ratio of gate radius to maximum head has a wide range. The writers use the ratio r/H_D , in which H_D is the design head for the spillway. This is the inverse of the ratio used by Mr. Bradley, used so that circular arcs can be traced on dimensionless profiles of x/H_D and y/H_D . bilies of x/H_D and y/H_D .

A comparison has been made of the coefficients for various (r/H_D) -value with the gate down. Only the high-overflow sections with negligible velocity of approach were selected from Table 2 for a study of discharge coefficients. Table 8 shows the value of the discharge coefficients for the condition when the drum gate is down. The percentage difference of the coefficient from that of the Madden Dam coefficient is also shown. It is expected that the accuracy of the discharge measurements and thus the coefficient of discharge is less than 1% TABLE 8.&-COMPARISON OF **DISCHARGE**

TABLE 8.⁻⁻COMPARISON OF DISCHARGE COEFFICIENT

WITH THE GATE DOWN

 $\frac{1}{2}$, denote the data are listed in Table 8 are in the approximate in the approximate $\frac{1}{2}$ character of the data of the time of the time of the state of the chronological order of the time of their design conception.

Because of the increase in the ratio of r/H_D (Table 8), it is of interest to plot the profile for the lower surface of the nappe from a sharp-crested weir with an approach slope of 2 on 3 in terms of x/H_D and y/H_D and to superimpose on it the arcs of circles with radii of r/H_D equal to 1, 2, and 3, as is done in Fig. 16. The center of the radius is located on the axis of the crest. It can be seen that the arc represented by r/H_D equal to 1 is a fair approximation of the true nappe shape. The arcs of r/H_D equal to 2 and 3 indicate a very flat curvature in comparison to the shape of the nappe.

One is tempted to assume, for a crest with a ratio $r/H_D = 3$, that the coefficient would be that for one third the design head of a crest with $4/H_D = 1$.

Model studies for Madden Dam reported by Richard R. Randolph, Jr.,t8 indicate that the coefficient for such a condition is approximately 3.40. Such a coefficient is not in agreement with that for Capilano Dam with r/H_D equal to 3.62 at full head. The lack of agreement does not necessarily vitiate the initial assumption. The difference in the coefficient may be caused by the

Fia. 16.-Lowen Sturace of NAPPE FROM SLOPING WEIR COMPARED WITH CIRCULAR ARCS

difference in shape of the two crests upstream from the circular arc. Furthermore, the scale ratio of the Madden Dam model was only 1:78, and a 10-ft prototype head would be 0.128 ft on the model, which is near the lower limit of reliability for conformity of the discharge coefficient.

J0sEP1 N. BRADLEY,"9 A.M. ASCE.-Mr. Shulits' statements regarding the lack of correlation in laboratory studies are well founded, and the writer is in complete agreement with his views.

Mr. Buehler's analysis for the determination of the designed head, *HD,* for overflow sections formed by a single radius, or for a shape that conforms closely to a single radius, gives satisfactory results. The comparison of discharge coefficients for free flow over various dams, using Eq. 3 with the method offered in the paper, is gratifying. Mr. Buehler's method certainly has merit be-
cause following the determination of H_D , coefficients of discharge can be com-
puted directly for all heads.

Messrs. Campbell and McCool undertook to show that a definite relationship exists between the coefficient of discharge at the designed head and the ratio r/H_D for overflow shapes. This relationship is valid if the overflow shape
can be approximated by an arc of a single radius and if the approach conditions
are favorable—that is, if the approach depth below the cres H_D . This method results in a coefficient of discharge for the designed head only.
When overflow sections are encountered where a single radius does not approximate the overflow shape, or when the approach conditions are

¹⁴ "Hydraulic Tests on the Spillway of the Madden Dam." by Richard R. Randolph. Jr., Transactions, 100Hydr. Engr., Bureau of Reclamation, U.S. Dept. of the Interior, Denver, Colo.

Mr. Wyss suggested that pressures and water surfaces for drum gates at various positions and reservoir levels would be useful to designers in computing gate loadings. A limited amount of information is available, and this will be presented.

Because there was good correlation among the discharge coefficients, it was reasoned that the pressures and related flow patterns would also be well correlated through the same variables.

Pressures and water-surface profiles are plotted in dimensionless coordinates (in terms of the radius of the gate) in Fig. 17. Five positions of the gate are shown for various reservoir levels producing flow over the gate. Pressures and water surfaces are shown for some levels whereas only pressures are

available for others. The broken lines represent pressure, measured vertically, for the reservoir levels indicated at the left of the charts. Upper water-surface profiles are shown by solid lines, and lower water-surface profiles are identified by dash lines. The charts represent a composite, in graphical form, of information from model tests performed on the Grand Coulce, Hamilton, Norris, Friant, and Hoover dams.

To determine graphically the most adverse water load on a particular gate, it is necessary to investigate the pressures for several gate positions. Assuming that the first position is $\theta = 41^{\circ}$, the gate is drawn in this position on a piece of transparent paper to the same scale as that used in Fig. 17. The maximum expected reservoir is indicated for this gate position on the left side of the transparent sheet.

The transparent sheet is then placed over Fig. 17(a), disregarding the origin of coordinates, and matching only the downstream tips of the two gates. The downstream part of all drum gates, regardless of size or radius, will coincide for any given value of θ . The height of the gate, or length of arc, can be expected to vary; this will have a negligible effect on pressures or water-surface profiles in the majority of cases. Should the gate under investigation differ from the height shown in Fig. 17 (a) , a small increase or decrease in the approach-depth results.

Beginning with the chosen reservoir level, the pressure curve is traced from Fig. $17(a)$ onto the transparent paper. It may be necessary to interpolate between two of the pressure curves. The result will be similar to that shown in Fig. $17(f)$.

A similar procedure is then followed for gate positions of 23°, 9° , -3° , and -35° , utilizing Figs. 17(b), 17(c), 17(d), and 17(e), respectively. The result is a composite plot similar to that shown in Fig. 17 (f) . It should be noted that the pressures shown for negative angles of the gate are not as reliable as those for positive angles. Fortunately, the greater water loads occur for positive angles.

Water loads can be determined by scaling the pressures vertically over the gate as indicated by point A in Fig. 17 (f) . If a gate angle other than those shown is desired, interpolation can be made directly on the sheet corresponding to Fig. $17(f)$. Following the establishment of the maximum-pressure curve, values of x/r and y/r are scaled from the sheet corresponding to Fig. 17(f) and are transferred to dimensional values by multiplying by r . Should watersurface profiles be desired, the same method of tracing and scaling can be used.