# Arbitrary Surface Crack Growth due to PWSCC and its Inclusion in PFM Codes

### **Engineering Mechanics Corporation of Columbus**

Presented by Do-Jun Shim

Prepared by Do-Jun Shim and David L. Rudland

Workshop on LBB in PWSCC Systems January 9-11 2008 Hilton Washington DC/Rockville, Executive Meeting Center djshim@emc-sq.com



### Rationale

- Through work on Wolf Creek issue (MRP-216 and NRC confirmatory effort), PWSCC surface crack growth is arbitrary in nature.
- PFM codes use pre-defined, semi-elliptical surface crack influence functions for making crack growth predictions.
- In some cases this assumption can be very conservative - for both crack growth and stability.
- Can this behavior be modeled for use in PFM codes?



# **Objective**

- Conduct sensitivity analyses using PipeFracCAE code to determine the conditions where a surface crack will not grow with a semi-elliptical profile.
- Compare the crack size/time behavior of the arbitrary and idealized (semi-elliptical) surface crack at the deepest and surface locations along the crack front.
- Determine if correction factors to published influence functions can be used to make more accurate leakage time predictions in PFM codes



# Sensitivity Matrix

- Three pipe diameters
- Four weld residual stresses (including no WRS)
- Two levels of bending stresses ( 6.31 ksi and 14.26 ksi)
- Two initial crack lengths (12.5% and 40% of pipe circum.)
- Initial crack depth ( 26% of wall thickness) Fixed
- Axial tension ( 4 ksi ), Internal pressure ( 2.235 ksi ) Fixed
- Total of 48 cases (24 cases completed so far)



# Sensitivity Matrix (cont'd)

Three pipe diameters

Pipe geometry	D <sub>o</sub> (in)	t (in)	$R_i/t$
Small (Relief line)	7.75	1.29	2.00
Medium (Surge line)	15.00	1.58	3.75
Large (Hot leg)	33.94	2.37	6.16

Four weld residual stresses (including no WRS)



Xc = Distance where stress field crosses into compression

Xc<sub>surge</sub> > Xc<sub>relief</sub> > Xc<sub>hotleg</sub>

 $\int mc^2$ 

## **Shape Factor**

- Shape factor is defined as the area under the normalized crack shape
- Shape factor indicates how the crack shape is changing relative to a semi-elliptical shape





#### **Results – Effect of pipe diameter**



#### **Results – Effect of WRS**



### **Results – Effect of bending stress**



#### **Results – Effect of initial crack length**



## **Comparison with Idealized Solution**

- Idealized (semi-elliptical) crack growth using Anderson solution
  - K values at deepest and surface points
- Compare crack growth at deepest and surface points
- Comparison for all 'no WRS' case results



# **Comparison with Idealized Solution (cont'd)**

- Comparison for all 24 cases
- Time to leakage showed some difference for certain cases
- However, crack depth and crack length at leakage show relatively good agreement

![](_page_11_Figure_4.jpeg)

# **Cases Showing Difference in Time to Leakage**

Cases with low bending (6.31 ksi) with Relief or Hot leg WRS

Relatively small K values near the compressive WRS

![](_page_12_Figure_3.jpeg)

## **Cases Showing Difference in Time to Leakage**

![](_page_13_Figure_1.jpeg)

Innovative Structural Integrity Solutions

### **Effect of Influence Functions**

- Curve-fitted influence functions used in the present work
- Slight difference shown between actual and curve-fitted results
- Range of R<sub>i</sub>/t in Anderson solution : from 3 to 100
- Results from Wolf Creek demonstrated the effect of influence function on time to leakage ( $R_i/t = 2$ )
  Curve-fitted

![](_page_14_Figure_5.jpeg)

# Effect of Influence Functions (cont'd)

- Need to compare the crack growth results using the actual influence functions versus the curve-fitted values.
- Also need to investigate the applicability of the influence functions for high-order stress distribution.

- Anderson solution uses FE based  $G_0$  and  $G_1$  values along with weight functions to calculate  $G_2$ - $G_4$  which are used for K calculation for high-order stress distribution

![](_page_15_Picture_4.jpeg)

### Transition from surface crack to TWC

- Generally, when a surface crack penetrates the wall-thickness, the resulting ID TWC length is assumed to be same as the final ID length of the surface crack.
- In some cases, this assumption may be overly conservative, since it ignores the time from leaking surface crack to idealized TWC.

![](_page_16_Figure_3.jpeg)

#### Transition from surface crack to TWC (cont'd)

- Different shape factor at leakage (even for cases on 1:1 line)
- Equivalent idealized TWC may be defined using the shape factor (crack area) at leakage

![](_page_17_Figure_3.jpeg)

![](_page_17_Figure_4.jpeg)

# Summary

- From the sensitivity analyses performed using PipeFracCAE, the effects of each parameter on crack growth behavior were investigated.
- The results demonstrate that for the cases with relatively low bending stress and WRSs with small values of Xc, the PipeFracCAE and Anderson solution showed difference in time to leakage.
- However, the crack lengths at leakage showed relatively good agreement.
- The inaccuracy (curve-fit, weight function) of the influence function may be causing the difference.
- Need to further investigate the applicability of the influence functions.
- Transition from surface crack to TWC may be made by using the shape factor.

![](_page_18_Picture_7.jpeg)