



AECL EACL

# Time-Average Model (\*TIME-AVER Module)



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## **Time-Average Model (\*TIME-AVER Module)**

- The time-average model is *not* an average over time of core snapshots
- It is a model in which *lattice cross-sections* at each location (bundle) are averaged over the residence time of the fuel at that location

### **Features of time-average model:**

- Bundle-specific properties
- Lattice properties of each bundle averaged over irradiation interval experienced by fuel at that location - *assuming flux constant in time*
- Axial refuelling scheme taken into account



## Time-Average Model (con't)

- Use indices  $j$  = channel,  $k$  = axial position
- Let  $\hat{\phi}_{jk}$  be the average (assumed constant) fuel flux at position  $jk$
- Let  $T_j$  denote average time between refuellings (“dwell time”) for channel  $j$
- Let  $\omega_{in,jk}, \omega_{out,jk}$  be the irradiation of the fuel as it *comes into* and *exits from* position  $jk$

Then: 
$$\omega_{out,jk} = \omega_{in,jk} + \hat{\phi}_{jk} T_j \quad (1)$$



## Time-Average Model (con't)

Time-average value of cross-section  $\Sigma_i$  at position  $jk$  is the value which preserves average reaction rate:

$$\Sigma_{i,jk}(\text{t.av.}) = \frac{\frac{1}{T_j} \int_0^{T_j} \Sigma_{i,jk}(\omega) \hat{\phi}_{jk} dt}{\frac{1}{T_j} \int_0^{T_j} \hat{\phi}_{jk} dt}$$

Change variables to  $d\omega = \hat{\phi}_{jk} dt$  as before:

$$\Sigma_{i,jk}(\text{t.av.}) = \frac{1}{\omega_{\text{out},jk} - \omega_{\text{in},jk}} \int_{\omega_{\text{in},jk}}^{\omega_{\text{out},jk}} \Sigma_{i,jk}(\omega) d\omega$$

i.e., time-average cross sections are functions of time-average flux, and time-average flux is function of cross-sections (via diffusion equation)

$\therefore$  Self-consistency problem



## Time-Average Model (con't)

- Calculational scheme *not complete* without relationship between dwell time and flux. This relationship is derived below for an N-bundle-shift in a 12-bundle channel
- Immediately after refuelling, first N bundles are fresh while positions 12-N contain shifted bundles:

$$\omega_{\text{in},jk} = \begin{cases} 0 & \text{for } 1 \leq k \leq N \\ \omega_{\text{out},j(k-N)} & N < k \leq 12 \end{cases}$$



## Time-Average Model (con't)

- Exit irradiation in channel  $j$  is average of values of out going irradiation over  $N$  bundles leaving channel:

$$\omega_{\text{exit},j} = \frac{1}{N} \sum_{k=13-N}^{12} \omega_{\text{out},jk}$$

- It can be show that, in general, for an  $N$ -bundle shift we have:

$$\omega_{\text{exit},j} = \frac{T_j}{N} \sum_{k=1}^{12} \hat{\phi}_{jk}$$

- or, equivalently:

$$T_j = \frac{N \omega_{\text{exit},j}}{\sum_{k=1}^{12} \hat{\phi}_{jk}}$$



## **\*TIME-AVER Module**

- The  $\omega_{\text{exit},j}$  and the axial refuelling scheme are the *degrees of freedom* of the problem.

**The code user must first:**

- define regions of refuelling scheme (e.g. 2-bundle-shift for all channels, or regions of 2-bs and others of 4-bs, etc...); in the limit, a different fuelling scheme could be defined for every channel
- define *guess* values for the  $\omega_{\text{exit},j}$  ; again, this can be by region, or, in the limit, by *channel*



## **\*TIME-AVER Module (con't)**

- The time-average calculation then proceeds and should be allowed to iterate until convergence: convergence in the flux *and* in the irradiation ranges  $[\omega_{in,jk}, \omega_{out,jk}]$  (and consequently in the dwell times)
- Once convergence is attained, the user must examine the result to decide if:
  - criticality has been obtained ( $k_{eff} = 1$ , or appropriately close to 1)
  - the desired flux shape has been obtained (look at zone or region fluxes)





## \*TIME-AVER Module (con't)

- If these conditions are satisfied, the calculation can be considered complete.
- if the conditions are not satisfied, adjustments have to be made and the calculation repeated:
  - If criticality has *not* been obtained, then the *average* value of  $\omega_{\text{exit},j}$  has to be adjusted.
  - If the flux shape is not as desired, the *relative* values should be adjusted, or new regions with different values of  $\omega_{\text{exit},j}$  should be defined (e.g., to obtain more or less radial flattening, or compensate for specific local features such as hardware at bottom of calandria)

Example: the flux shape obtained has too much radial peaking; radial flattening is required to satisfy channel-power license limits; the user will flatten the radial flux by increasing the values of  $\omega_{\text{exit},j}$  in *inner* core relative to those in *outer* core; trial and error may be needed to achieve all desired conditions.



## **\*TIME-AVER Module (con't)**

- One more self-consistency problem needs to be considered: the consistency of the  $^{135}\text{Xe}$  concentration with the flux (power).

Two choices are available:

- Do all calculations with an *average*  $^{135}\text{Xe}$  concentration; ignore self-consistency - do not use XE trailer card.
- Demand self-consistency of  $^{135}\text{Xe}$  concentration with power by using XE trailer card - this is the more correct treatment: the  $^{135}\text{Xe}$  concentration will be re-calculated at each iteration of the irradiation ranges (or axial flux shape, or dwell times).



## \*TIME-AVER Module (con't)

- Within the \*TIME-AVER module, there are two main calculational *regimes* or *options* which are very important to distinguish from each other:
  - Solving for the time-average flux shape. Here the full self-consistency problem is solved, i.e. the fluxes,  $\hat{\phi}_{jk}$ , the dwell times  $T_j$ , and the irradiation ranges  $[\omega_{in,jk}, \omega_{out,jk}]$  are all calculated in self-consistent fashion. This is what has been described above. ***This option is selected by setting IPRESRV = 0.***
  - Solving for a *perturbation* in a given time-average core (e.g., calculating device worths). Here only the *perturbed flux distribution* is calculated - the irradiation ranges (and dwell times) obtained previously are kept fixed; self-consistency is not sought. ***This option is selected by setting IPRESRV = 1.***

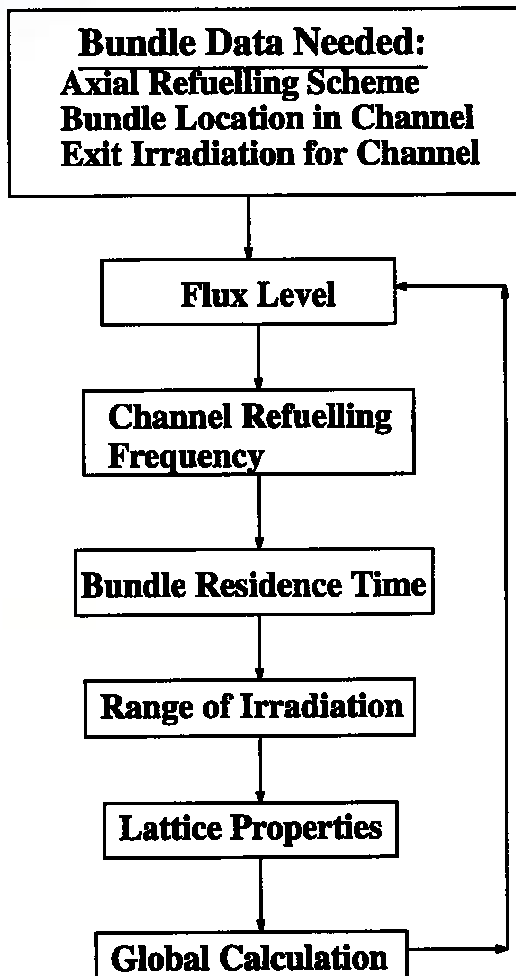


## \*TIME-AVER Module (con't)

- Both options yield a  $k_{\text{eff}}$  value and a flux shape. Only the first option yields also irradiation ranges  $[\omega_{\text{in},jk}, \omega_{\text{out},jk}]$  and dwell times  $T_j$ .
- Note that in both options the XE trailer card can be used to demand self-consistency between the flux distribution and the  $^{135}\text{Xe}$  concentration
- Note also that the flux distribution obtained with the \*TIME-AVER module *has no refuelling ripple* - since all bundles have properties averaged over an irradiation range, and there are no channels which have “recently been refuelled”. Therefore the target time-average channel and bundle powers must be sufficiently lower than the license limits to allow for the refuelling ripple which will be obtained in instantaneous snapshots.



## **Time-Average Calculation**





## **\*TAVEQUIV Module**

- The time-average model gives cross-sections which are averaged over the fuel residence time. The model therefore provides a good approximation to a *long-term-average* picture of the flux and power distributions in the core.
  - However, the time-average model is numerically complicated by the fact that the lattice properties must be obtained by integrating over bundle-specific irradiation ranges.
  - It is useful to have a (much simpler) “snapshot” model which reproduces the time-average power distribution.
- This is obtained with the \*TAVEQUIV module.



## \*TAVEQUIV Module (con't)

- For each bundle in core, this module defines a *single* value of irradiation  $\omega_{inst,jk}$  (i.e., a snapshot model) whose *net effect* is to essentially reproduce the time-average properties. This is achieved by demanding that the local time-average *infinite multiplication constant*  $k$  be matched for each bundle:

$$k_{\infty,inst,jk} = k_{\infty,t.av.,jk}$$

- The instantaneous time-average-equivalent value of irradiation will normally be close to the mid-point of the irradiation range; this serves as the *first guess*, which is then refined:

$$\omega_{inst,jk} \approx (\omega_{in,jk} + \omega_{out,jk}) / 2$$



POSITION  
FLUX

1  $\phi_1$  2  $\phi_2$  3  $\phi_3$  4  $\phi_4$  5  $\phi_5$  6  $\phi_6$  7  $\phi_7$  8  $\phi_8$  9  $\phi_9$  10  $\phi_{10}$  11  $\phi_{11}$  12  $\phi_{12}$

$t = 0$

|              |              |              |              |              |              |              |              |              |                 |                 |                 |
|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|-----------------|-----------------|-----------------|
| $\omega_1^m$ | $\omega_2^m$ | $\omega_3^m$ | $\omega_4^m$ | $\omega_5^m$ | $\omega_6^m$ | $\omega_7^m$ | $\omega_8^m$ | $\omega_9^m$ | $\omega_{10}^m$ | $\omega_{11}^m$ | $\omega_{12}^m$ |
| 0            | 0            | 0            | 0            | 0            | 0            | 0            | 0            | $\phi_1 T$   | $\phi_2 T$      | $\phi_3 T$      | $\phi_4 T$      |

$t = T$

|              |              |              |              |              |              |              |              |                       |                          |                          |                          |
|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|-----------------------|--------------------------|--------------------------|--------------------------|
| $\omega_1^m$ | $\omega_2^m$ | $\omega_3^m$ | $\omega_4^m$ | $\omega_5^m$ | $\omega_6^m$ | $\omega_7^m$ | $\omega_8^m$ | $\omega_9^m$          | $\omega_{10}^m$          | $\omega_{11}^m$          | $\omega_{12}^m$          |
| $\phi_1 T$   | $\phi_2 T$   | $\phi_3 T$   | $\phi_4 T$   | $\phi_5 T$   | $\phi_6 T$   | $\phi_7 T$   | $\phi_8 T$   | $(\phi_1 + \phi_9) T$ | $(\phi_2 + \phi_{10}) T$ | $(\phi_3 + \phi_{11}) T$ | $(\phi_4 + \phi_{12}) T$ |

$t = 0$

|              |              |              |              |              |              |              |              |              |                 |                 |                 |
|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|-----------------|-----------------|-----------------|
| $\omega_1^m$ | $\omega_2^m$ | $\omega_3^m$ | $\omega_4^m$ | $\omega_5^m$ | $\omega_6^m$ | $\omega_7^m$ | $\omega_8^m$ | $\omega_9^m$ | $\omega_{10}^m$ | $\omega_{11}^m$ | $\omega_{12}^m$ |
| 0            | 0            | 0            | 0            | 0            | 0            | 0            | 0            | $\phi_1 T$   | $\phi_2 T$      | $\phi_3 T$      | $\phi_4 T$      |

AVERAGE DISCHARGE  
IRRADIATION

$$= \frac{1}{8} \left\{ \phi_5 T + \phi_6 T + \phi_7 T + \phi_8 T + (\phi_1 + \phi_9) T + (\phi_2 + \phi_{10}) T + (\phi_3 + \phi_{11}) T + (\phi_4 + \phi_{12}) T \right\}$$

$$= \frac{T}{8} \left\{ \phi_1 + \phi_2 + \phi_3 + \phi_4 + \phi_5 + \phi_6 + \phi_7 + \phi_8 + \phi_9 + \phi_{10} + \phi_{11} + \phi_{12} \right\}$$





## **\*INSTANTAN Module**

**Based on time average beginning and end of cycle irradiations, bundle burnup is defined as:**

$$\omega(i, j, k) = \omega_1(k) + f(i, j) (\omega_2(k) - \omega_1(k))$$

**Where  $f(i, j)$  = channel age (0-1.0) as a fraction of dwell time**

**Two main options:**

- 1. random age distribution (based on time average beginning and end of cycle)**
  - User provides seed for random generator
- 2. patterned age distribution**
  - User provides repeating age pattern, usually 7x7 matrix



## **\*INSTANTAN Cont....**

- **Module used to estimate, at the preliminary design stage, snapshot results based on time-average design, i.e.**
  - **Ripple**
  - **Maximum channel and bundle powers**
  - **Generally results in overestimate of these parameters due to “hot spots”, especially using the random age option**
  - **But can be used to compare time-averages**
- **Can also be used as a starting point for equilibrium fuelling study (with \*SIMULATE)**



## **\*SIMULATE Module**

**This model is the most realistic because it represents the reactor as it is on one particular day - a snapshot.**

**Each bundle has an *instantaneous* value of irradiation (  $\omega_{inst,jk}$  )**

- not a *range* of irradianations as in the time-average model.**

**The \*SIMULATE module tracks the reactor operating history by advancing time from a previous snapshot by a *burnup step*.**



## \*SIMULATE Cont....

The \*SIMULATE process is thus:

- Start at the *initial* core: 0 full-power-days (FPD); the irradiation of all bundles is zero. Solve for the flux in this snapshot.
- Take a burn step  $\Delta t$  (e.g., a few FPD) and solve for new snapshot at the same time modifying core conditions if necessary - e.g., boron concentration, device positions, channels refuelled.
- The irradiations from the earlier snapshot at  $t$  to new snapshot at  $(t + \Delta t)$  are updated according to:
$$\omega_{\text{inst},jk}(t + \Delta t) = \omega_{\text{inst},jk}(t) + \hat{\phi}_{jk} \Delta t$$
- Take another burn step, repeat irradiation update and flux/power calculation. Etc...



## **\*SIMULATE Cont....**

- **At each snapshot diffusion equation is solved with instantaneous cross-sections corresponding to instantaneous irradiation distribution (and other instantaneous conditions).**
- **Choices for lattice properties:**
  - **2-group WIMS tables with only burnup dependency with or without distributed xenon**
    - **XE trailer card should be used when consistency is desired between flux distribution and  $^{135}\text{Xe}$  concentration (recommended option)**
  - **Micro-depletion option (WIMSHI trailer card) takes into account both local-parameter effects and the individual nuclide history of each bundle**
- **Instantaneous model will feature a refuelling ripple since individual channels are refuelled at various times.**