

From: "Gauntt, Randall O" <rogaunt@sandia.gov>
To: "Jason Schaperow" <JHS1@nrc.gov>, "Gauntt, Randa...
Date: Thu, Jul 13, 2000 2:19 PM
Subject: RE: Plume Energy

OK,
This version seems to be right.
Sorry about the false start.
Randy

-----Original Message-----

From: Jason Schaperow [mailto:JHS1@nrc.gov]
Sent: July 11, 2000 1:12 PM
To: rogaunt@sandia.gov
Cc: AXB@nrc.gov; AXN@nrc.gov; CGT@nrc.gov
Subject: Plume Energy

Please see the attached file (WordPerfect8 format). Also, I just FAXed you a copy of the attached file (FAX number (505)-844-8719), in case you do not have a program handy to read it. Thank you very much.

Sincerely,
Jason

CC: TWFN_DO.twf5_po(AXB,AXN,CGT)

I-35

Analysis of Plume Energy Associated with Spent Fuel Pool Storage Accident R.O. Gauntt 7/13/2000

Fuel and Canister Dimensions *****

$$r_{o_clad} := 6.135\text{mm} \qquad r_{fuel} := \frac{0.410}{2} \cdot \text{in}$$

$$r_{i_clad} := 5.322\text{mm} \qquad \text{can_perimeter} := 4.5.215 \cdot \text{in}$$

$$\text{assembly_length} := 4.1\text{m} \qquad \Delta t_{\text{canister}} := 0.12 \cdot \text{in}$$

Fuel Properties *****

$$\rho_{Zr} := 6500 \frac{\text{kg}}{\text{m}^3} \qquad C_{p_{UO2}} := 370 \cdot \frac{\text{joule}}{\text{kg} \cdot \text{K}}$$

$$\rho_{UO2} := 0.95 \cdot 10.96 \cdot \frac{\text{gm}}{\text{cm}^3}$$

$$\rho_{ZrO2} := 5.6 \cdot \frac{\text{gm}}{\text{cm}^3}$$

$$MW_{Zr} := 91.2 \frac{\text{gm}}{\text{mol}} \qquad MW_{N2} := 28 \cdot \frac{\text{gm}}{\text{mol}}$$

$$MW_{ZrO2} := 123.2 \cdot \frac{\text{gm}}{\text{mol}}$$

$$MW_{O2} := 32 \cdot \frac{\text{gm}}{\text{mol}}$$

Fuel Assembly Properties *****

$$\text{mass}_{\text{clad}} := 64\pi \cdot (r_{o_clad}^2 - r_{i_clad}^2) \cdot \text{assembly_length} \cdot \rho_{Zr}$$

$$\text{mass}_{\text{canister}} := \text{assembly_length} \cdot \text{can_perimeter} \cdot \Delta t_{\text{canister}} \cdot \rho_{Zr}$$

$$\text{mass}_{\text{fuel}} := 62 \cdot \pi \cdot r_{\text{fuel}}^2 \cdot \text{assembly_length} \cdot \rho_{UO2}$$

$$\text{mass}_{\text{canister}} = 43.039 \text{ kg}$$

$$\text{mass}_{\text{clad}} = 49.91 \text{ kg}$$

$$\text{mass}_{\text{fuel}} = 225.442 \text{ kg}$$

Enthalpy (Internal Energy) of Zircaloy, UO₂ and ZrO₂ ***
 Properties from MATPRO**

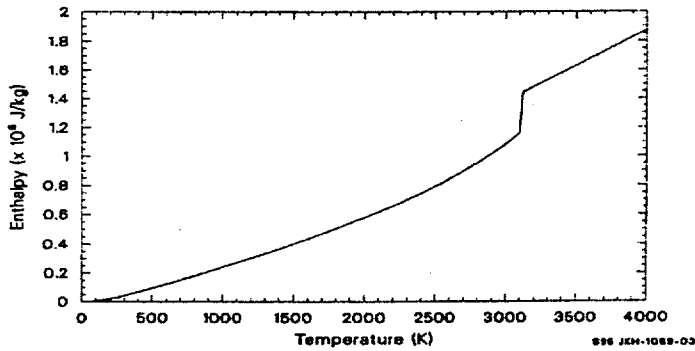
UO₂ Internal Energy *****

$$\begin{aligned}
 K_1 &:= 296.7 \cdot K^{-1} & \theta &:= 535.285 \cdot K & \Delta H_{f_UO2} &:= 2.74 \cdot 10^5 \cdot \frac{\text{joule}}{\text{kg}} \\
 K_2 &:= 2.43 \cdot 10^{-2} \cdot K^{-2} & E_D &:= 1.577 \cdot 10^5 \cdot \frac{\text{joule}}{\text{mol}} & C_{p1_UO2} &:= 503 \cdot \frac{\text{joule}}{\text{kg} \cdot K} \\
 K_3 &:= 8.745 \cdot 10^7 & R &:= 8.3143 \cdot \frac{\text{joule}}{\text{mol} \cdot K} & &
 \end{aligned}$$

$$H_{\text{solid_UO2}}(T) := \left[\frac{K_1 \cdot \theta}{\left(\frac{\theta}{T} - 1 \right)} + \frac{K_2 \cdot T^2}{2} + K_3 \cdot e^{\left(\frac{-E_D}{R \cdot T} \right)} \right] \cdot \frac{\text{joule}}{\text{kg}}$$

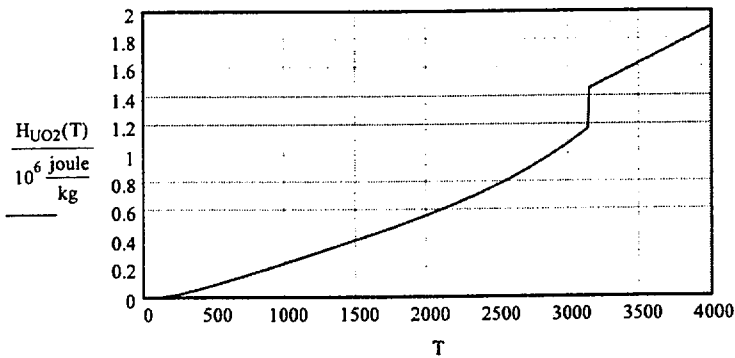
$$H_{UO2}(T) := \Phi(3138K - T) \cdot H_{\text{solid_UO2}}(T) + \Phi(T - 3138K) \cdot \left[H_{\text{solid_UO2}}(3138K) + \Delta H_{f_UO2} + (T - 3138K) \cdot C_{p1_UO2} \right]$$

T := 0K, 10K.. 4000K



MATPRO Data

Figure 2-3. Enthalpy of UO₂ as a function of temperature to 4,000 K.



Curve Fit to MATPRO

Zircaloy Oxide Internal Energy *****

$$H_{300} := 1.194 \cdot 10^4$$

$$H_1(T) := \left[565 \cdot \frac{T}{K} + 3.055 \cdot 10^{-2} \cdot \left(\frac{T}{K} \right)^2 + 1.14 \cdot 10^7 \cdot \left(\frac{K}{T} \right) - 2.102495 \cdot 10^5 + H_{300} \right] \cdot \frac{\text{joule}}{\text{kg}}$$

$$H_2(T) := \left[604.5 \cdot \left(\frac{T}{K} \right) - 1.46 \cdot 10^5 + H_{300} \right] \cdot \frac{\text{joule}}{\text{kg}}$$

$$H_3(T) := \left[171.7 \cdot \left(\frac{T}{K} \right) + 0.1082 \cdot \left(\frac{T}{K} \right)^2 + 2.868 \cdot 10^5 + H_{300} \right] \cdot \frac{\text{joule}}{\text{kg}}$$

$$H_4(T) := \left[171.7 \cdot \left(\frac{T}{K} \right) + 0.1082 \cdot \left(\frac{T}{K} \right)^2 + 3.888 \cdot 10^5 + H_{300} \right] \cdot \frac{\text{joule}}{\text{kg}}$$

$$H_5(T) := \left[815.0 \cdot \left(\frac{T}{K} \right) + 1.39 \cdot 10^5 + H_{300} \right] \cdot \frac{\text{joule}}{\text{kg}}$$

$$H_{ZrO_2}(T) := \begin{cases} H_1(T) & \text{if } [(T > 273.0K) \wedge (T < 1478.0K)] \\ H_2(T) & \text{if } [(T > 1478.01K) \wedge (T < 2000.0K)] \\ H_3(T) & \text{if } [(T \geq 2000.0K) \wedge (T < 2558.0K)] \\ H_4(T) & \text{if } [(T \geq 2558.0K) \wedge (T < 2973.0K)] \\ H_5(T) & \text{if } [(T \geq 2973.01K) \wedge (T < 4100.0K)] \\ 0.0 \frac{\text{joule}}{\text{kg}} & \text{otherwise} \end{cases}$$

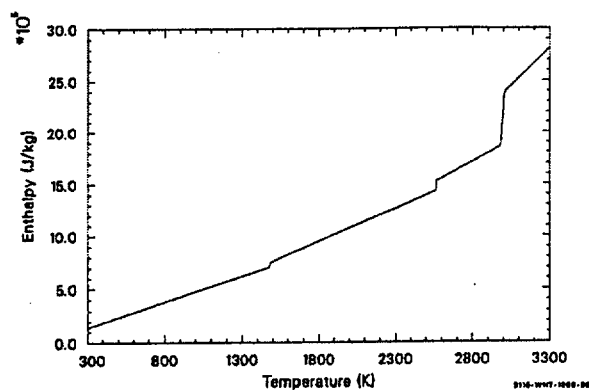
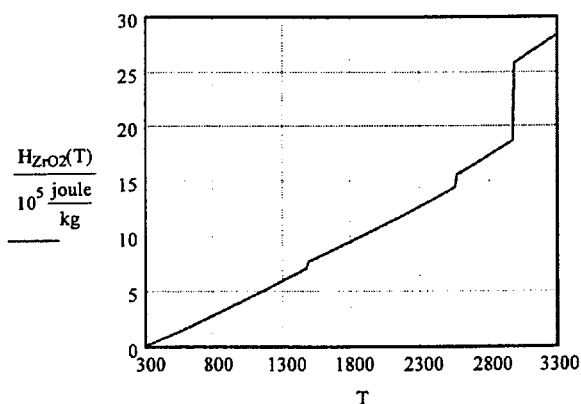


Figure 5-3. Zircaloy oxide enthalpy as a function of temperature.