#### EXTENSIONAL REGIME DATA BASE

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Ground Motion Workshop #2 -Methods, Models, and Preliminary Interpretations

> Doubletree Hotel Salt Lake City, UT

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107.8

9704010133-Part3

#### COLLECTION OF GROUND MOTION DATA

Extensional regimes from which we obtained data:

US Intermountain region (e.g. Basin and Range, Long Valley CA, Yellowstone) Salton Trough, CA

shallow volcanic regions of Central America

western Europe, Italy, Greece

New Zealand

Turkey (extensional jogs in Anatolian fault)

(n.b. -extensional regimes have normal and strike-slip earthquakes. We used both because there are strike-slip events that might affect Yucca Mountain and because there was not much normal faulting data.)

Data criteria:

available in digitized form recorded in small structures (fewer than 3 stories, not from deeply embedded basements, etc) triggered before S wave arrival

moment magnitude  $\geq 5.0$ distance  $\leq 105$  km

Table	7. List	of c	andida	te, relevant, and used	earthquakes					
								<u> </u>		
n ea	rthquake	e is a	"candi	date" if it has been sug	gested for any rea	ason to	be possibly relevant to t	this pr	bject.	
n ea	rthguake	is "	relevan	t" if it is in an extensior	<u>nal regime, has mo</u>	oment m	agnitude >=5.0, and has	<u>s usab</u>	le strong	motion
	' signifie							ļ		
Expla	nation o	fcol	umns:				· · · · · · · · · · · · · · · · · · ·			
	Year	hr:n	nn	Approximate earthqual	ke origin time			1		
	Approx	MAC	à 📃	Approx MAG is ML, M	s, Mw, or other es	timates,	w/o references; italic is	mome	ent magnit	ude
	<b>Rivnt?</b>			Rivnt is our current op	pinion of whether t	his ever	nt is relevant for further	study		
	W&S			This event was studied	d by Westaway an	d Smith	(1989)			
	used\te	ot st	ns	number of usable stat	ions\total number	of static	ons we know about			
	i i								used\tot	used
Year	Month	day	hr:mn	NAME or LOCATION	Approx MAG	Rivnt?	why	W&S	recs	here
1935	10	31	18:38	Helena, Mt	6.2	n	1 rec in 5 story bldg			
1935	10	31	1918	Helena, Mt		n	1 rec in 4 story bldg			
1935	11	21	20:58	Helena, Mt	5.8	n	1 rec in 4 story bldg			
1935	11	28	7:42	Helena, Mt	5.8	n	1 rec in 4 story bldg			
1938	6	6	2:42	Imperial Valley, CA	5	n	extens (16); only rec is S	trig	0\1	
1940	5	19	4:37	Imperial Valley, CA	6.87	<b>Y</b>	IV extens (16)		1\1	у
1949	4	13	19:55	Western Washington	7.1, 6.7	n	too deep (10)	•	<b>0</b> ) 4	
1951	, <b>1</b>	, 24	7:17	Imperial Valley, CA	5.6	n	extens (16); only rec is S	trig	0\1	
1953	6	14	4:17	Imperial Valley, CA	5.5	Y	IV extens (16)		1\1	
1955	12	17	6:07	Imperial Valley, CA	5.4	n	extens (16); only rec is S		0\1	
1959		18	6:37	Hebgen Lake, Mt	7	Y	/S89; stns > 100km, no di	9	1\2	
1962		ុ១០	13:35		ML5.7,Ms5.7(W&S)	*****	1 rec in 3 story bldg	1	414	
1972		23	6:29	Managua	6.2	Y	extensional (26)	1	1\1	L y
1972	~~~~	23	7:17		5	n	extensional (26) bad data	[ 	1\1	
1972	~~~	23	7:19	Managua	5.2	Y	extensional (26)	1		
1972		6	21:44		3.5, 4.4	n	too small(1)	•		
1972		8	12:19		3.9, 4.6	n	too small(1)			
1972		14	18:55		4.6, 4.7	n	too small(1)	•		
1972		14	21:01		3.3, 4.7	n	too small(1)	•		
1972		21	15:06		2.7, 4.0	n	too small(1)	•		
1974		29	15:12		3.5, 4.4	n	too small(1)	•	1\1	
1975		4	5:16	Patras, Greece	4.6, 5.1	n	in WS89; too deep (26)		111	
1975		13	0:22	Xylokastron, Greece	3.9, 4.6	n	too small(1)			
1975	· / · · · · · · · · · · · · · · · · · ·	12	8:23	Corinth, Greece	4.5, 4.8	n	too small(1)	•	015	
1975	8	1	20:02	Oroville, CA	5.7	n	only digital rec is S trig		0\5	

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									used\to1	used
Year	Month	day	hr:mn	NAME or LOCATION	Approx MAG	Rivnt?	why	W&S	recs	here?
1975	8	2	20:22	Oroville, CA	5	Y	in WS89	•	1\2	
1975	8	2	20:59	Oroville, CA	4.4, 5.2	n	in WS89; too small		3/3	
1975	- 8	3	1:03	Oroville, CA	4.5,4.8	n	too small(1)	*		
1975	8	3	2:47	Oroville, CA	3.7, 4.3	n	too small(1)	•		
1975	8	6	3:05	Oroville, CA	4.0, 4.7	л	too small(1)	•		
1975	8	8	7:00	Oroville, CA	4.5, 4.6	n	too small(1)	•		
1975	8	11	6:11	Oroville, CA	4.3, 4.4	n	too small(1)	*		
1975	8	16	5:48	Oroville, CA	3.3, 4.1	n	too small(1)	*		
1975	9	26	2:31	Oroville, CA	2,9, 4,2	n	too small(1)	•		
1975	9	27	22:34	Oroville, CA	Mw 4.67 (21)	n	too small	•		
1976	8	19	1:12	Denizli, Turkey	4.9	n	too small(1)			
1977	12		15:33	Izmir, Turkey	4.3, 4.9	n	too small(1)	•		
1977	12	16	10.000000000000000000000000000000000000	Izmir, Turkey	4.9, 5.3	Y	in WS89	*	1\1	
1978	6		20:03	Thessaloniki, Greece	Ms 6.5	n	densional (25), 1 rec irg b	h *		
1978	7	4		Thessaloniki, Greece	Ms 5.1	n	itensional (25), 1 rec irg b	ldg		
1979	7	18	13:12	Dursunbey, Turkey	4.9, 5.2	Y	in WS89	+	1\1	
1979	9	19		Valnerina, Italy	5.9	Y	in WS89	*	3\7	у
1979	10	15	23:16	Imperial Valley, CA	6.5	Y	IV extens (16)		33\35	У
1979	10	15	23:19	Imperial Valley, CA	4.8	n	IV extens (16)	· · · · ·	16\16	
1979	10	16	6:58	Imperial Valley, CA	5.5	Y	IV extens (16)		1\1	
1980	5	25	16:34	Mammoth Lakes, CA	6.2	Y	extensional (17)	3	2\3	у
1980	5	25	16:36	Mammoth Lakes, CA	ML 5.0	, n	A borderline, only 1 rec - h	ch ,	7\1	
1980	5	25	16:49	Mammoth Lakes, CA	5.8	Y	extensional (17)	*	2\3	у
1980	5	25	19:44	Mammoth Lakes, CA	5.8	Y	extensional (17)	•	2\4	y
1980	5	25	20:35	Mammoth Lakes, CA	5.7	Y	extensional (17)		2\4	у
1980	5	25	20:59	Mammoth Lakes, CA	Mb4.2 ML5.5(20)	Y	extensional (17)		?	
1980	5	26	1:19	Mammoth Lakes, CA	Mb4.4 ML4.7(20)	Y	extensional (17)		?	
1980	5	26	12:24	Mammoth Lakes, CA	Mb4.7 ML5.6(20)	Y	extensional (17)		?	
1980	5	26	18:57	Mammoth Lakes, CA	5.8, 6.1	Y	extensional (17)		1\2	
1980	5	27	14:50	Mammoth Lakes, CA	6	<b>Y</b>	extensional (17)	*	4\6	у
1980	5	27	19:01	Mammoth Lakes, CA	Mm=4.6, TCH 6/23	n	extensional (17), too sma	11 *	6\6	
1980	5	28	4:03	Mammoth Lakes, CA	2.6, 4.0	n	too small(1)	•		
1980	5	28	5:16	Mammoth Lakes, CA	3.7, 4.9	n	too small(1)	•		
1980	5	31	0:58	Mammoth Lakes, CA	2.7, 4.4	n	too small(1)	•		
1980	5	31	10:11	Mammoth Lakes, CA	3.0, 4.2	n	too small(1)	•		
1980	5	31	15:16		, 4.9,ML4.9 Mb4.1	n	too small(1)	•		
1980	5		15:02	Mammoth Lakes, CA	2.9, 4.0	n	too small(1)	•		

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									used\tot	used
Year	Month	day	hr:mn	NAME or LOCATION	Approx MAG	Rivnt?	why	W&S	recs	here?
1980	6	5	19:41	Mammoth Lakes, CA	2.4, 4.3	n	too small(1)	•	. I	
1980	6	9	3:28	Victoria, Mexico	6.32	Y	IV extens (16)		2\7	У
1980	6	9	3:30	Victoria, Mexico	not in PDE	n	bogus event			
1980	6	9	10:00	Mexicali VAlley	Mb4:4, ML4.5 (15)	n	too small			
1980	6	9	23:33	Mexicali Valley	ML4.2(pas)	n	too small			
1980	6	11	4:41	Mammoth Lakes, CA	Mm=4.0 TCH 6/23	n	extensional (17), too small		7\9	
1980	7	16		Volos, Greece	Ms 4.9	n	extensional (25), too small			
1980	8	11		Volos, Greece	Ms5.2, ML4.7		extensional (25)		1\1	
1980	9	26		Volos, Greece	Ms 4.8	n	extensional (25), too small			
1980	11	23	18:34	Campania (Irpinia), Italy	6.9	<u> </u>	in WS89	*	9\19	у
1980	11	23	18:35	Campania (Irpinia), Italy	6.2	Y	in WS89	*	10\10	у
1980	11	24	0:23	Campania (Irpinia), Italy	4.7	n	too small(1)	•		
1980	12	1	19:04	Campania (Irpinia), Italy	4.6	n	too small(1)	•		
1981	1	16	0:37	Campania (Irpinia), Italy	4.7	n	too small(1)	*		
1981	2	24	20:53	Corinth, Greece	6.7	Y	in WS89	•	1\1	
1981	2	25	2:35	Corinth, Greece	6.4	Y	in WS89	*	1\1	
1981	3	4	21:58	Corinth, Greece	Ms6.4(12)	Y	normal (12)		1\1	
1981	4	26	12:09	Westmorland, CA (11)	5.8	Y	IV extens (16)		6\6	у
1981	9	30	11:53	Mammoth Lakes, CA	5.6 Ms5.8 ML5.8(2	Y	extensional (17)		?	
1981	9	30	13:06	Mammoth Lakes, CA	Mb4.7 ML4.6(20)	Y	extensional (17)		?	
1983	1	7	1:38	Mammoth Lakes, CA	Ms5.0 (15) ML5.0	Y	extensional (17)		1\1	
1983	1	7	3:24	Mammoth Lakes, CA	Ms5.0 (15) ML5.4	Y	extensional (17)		1\1	
1983	1	17		Argostoli, Greece (mainsh	Ms 7.0	n	not extensional (25)			
1983	1	17		Argostoli, Greece (aftersh	Ms 5.3	n	not extensional (25)			
1983	1	19		Argostoli, Greece (aftersh	Ms 5.7	n	not extensional (25)			
1983	1	31		Argostoli, Greece (aftersh	Ms 5.3	n	not extensional (25)			
1983	2	2		Zakynthos, Greece	Ms 5.4	n	not extensional (25)			
1983	3	16		Lefkada, Greece (mainsh)	Ms 5.2	n	not extensional (25)			
1983	Э	23		Lefkada, Greece (aftersh)	Ms 5.2	n	not extensional (25)			
1983	3	23		Argostoli, Greece (aftersh	Ms 6.2	n	not extensional (25)			
1983	3	24		Argostoli, Greece (aftersh	Ms 5.5	n	not extensional (25)	1	,	
1983	7	5	12:01	Biga, Turkey	5.8, 6.1	Y	in WS89	*	≤1\5	
1983		6	15:43	North Aegean, Greece	6.74	Y	extensional (25)		1\1	у
1983	8	26		Ouranopolis, Greece	Ms4.9	n	too small			
1983	~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	28	14:06	Borah Peak, ID	6.9	Y	in WS89	*	2\8	<u>y</u>
1983		29	1	Borah Peak, ID	5.1	Y	in WS89	· •	3\5	у
1983	daaraan waxaa aha	1	23:39		Mm=4.8 (23)	n	in WS89	٠		

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25

									used\tot	used
Year	Month	day	hr:mn	NAME or LOCATION	Approx MAG	Rivnt?	why	W&S	recs	here?
1983	10	30	1:24	Borah Peak, ID	3.5, 4.8	n	too small(1)	*		
1983	10	30	1:59	Borah Peak, ID	3.1, 4.7	n	too small(1)	•		
1983	11	2	23:43	Borah Peak, ID	3.5, 4.2	n	too small(1)	•		
1983	11	6	21:04	Borah Peak, ID	3.3, 4.6	n	too small(1)	•		
1983	11	8		Liege, Belgium	5.1	n?	no d<100 km?		?	
1984	2	19		Poligiros, Greece	Ms 4.9	n	ensional (25), too small, S	trig		
1984	3	5	2:07	South Taupo, NZ	5.5	?		*	1\1	
1984	4	29	5:02	Umbria, Italy	5.0, 5.6	Y	in WS89	*	?\6	
1984	5	7	17:49	Lazio-Abruzzo, Italy	5.8	Y	in WS89	•	5\16	У
1984	5	11	10:41	Lazio-Abruzzo, Italy	5.2, 5.5	Y	in WS89	*	?\10	
1984	5	11	10:05	Lazio-Abruzzo, Italy	4.2	n	too small(1)	•		
1984	5	11	11:26	Lazio-Abruzzo, Italy	4.2	n	too small(1)	•		
1984	5	11	13:14	Lazio-Abruzzo, Italy	4.3	n	too small(1)	•		
1984	5	11	13:39	Lazio-Abruzzo, Italy	4.1	n	too small(1)	•		
1984	5	11	16:39	Lazio-Abruzzo, Italy	4.3	n	too small(1)	•		
1984	5	11	23:35	Lazio-Abruzzo, Italy	4.1	n	too small(1)	•		
1984	6	24		Granada, Spain	5	?			1\6	
1984	7	9		Edessa, Greece	Ms5.3, ML4.8	n	nsional (25), 2 recs in big I	bidgs	1/1	
1984	10	4		Zakynthos, Greece	Ms 5.0	n	not extensional (25)	· · · · ·		
1984	10	10		Pelekanada, Greece	Ms5.0, ML4.5	Y	extensional (25)		≥1\2	
1984	11	23	18:08	Round Valley, CA	5.6 Ms5.7 ML6.2(2	Y	extensional (17)		?	
1984	11	23	19:12	Bishop, (Round Valley), CA	4.8 Ms4.7 ML5.4(2	Y	extensional (17)		1\1	
1985	3	З		Amfilochia (main shock)	Ms4.5	n	not extensional (25)			
1985	3	3		Amfilochia (aftersh)	Ms4.5	n	not extensional (25)			
1985	8	31		Lefkada, Greece	Ms 5.2	n	not extensional (25)	, ,		
1985	11	9		Drama, Greece	Ms5.5, ML5.0	Y	extensional (25)		2\2	
1986	2	18		Edessa, Greece	Ms 5.0	Y	extensional (25)	ļ	?	
1986	7	20	14:29	Chalfant Valley, CA	5.8	Y	extensional(18)		5\5	У
1986	7	21	14:42	Chalfant Valley, CA	6.3	Y	extensional(18)		10\11	у
1986	7	21	14:51	Chalfant Valley, CA	5.6	Y	extensional(18)	I	3\3	у
1986	7	31	7:22	Chalfant Valley, CA	5.8	Y	extensional(18)		2\2	у
1986	9	13	17:24	Kalamata, Greece (mainsh	Ms6.2	n	in WS89; 1 rec in big bldg	•	1\1	
1986	9	15	11:41	<b>Kalamata</b> , Greece (aftersh	Ms5.4	n	in WS89; too small	•	3\3	
1986	10	10	17:49	San Salvador, El Salvador	5.76				2\9	y
1987	2	7	3:45	Cerro Prieta, Mexico	MI=5.4	Y	IV extens (16)		1\1	
1987	3	2	1:35	Edgecomb, New Zeleand	5.2	Y	in WS89	*	?\1	
1987	3	2	1:42	Edgecomb, New Zeleand	6.6	Y	in WS89	*	2\3	y

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									used\tot	used
Year	Month	day	hr:mn	NAME or LOCATION	Approx MAG	Rivnt?	why	W&S	recs	here?
1987	3	2	1:51	Edgecomb, New Zeleand	5.8	Y	in WS89	*	1\2	У
1987	11	24	1:54	Elmore Ranch, CA	6.2	Y	IV extens (16)		1\1	у
1987	11	24	13:15	Superstition Hills, CA	6.6	Y	IV extens (16)		2\3	у
1988	8	14	20:03	San Rafael Swell, UT	5.21(27)	1	West US probably extensiona	al	?	
1988	10	16		Kyllini, Greece (mainsh)	Ms 5.9	n	not extensional (25)			
1988	10	17		Kyllini, Greece (aftersh)	Ms 4.4	n	not extensional (25)			
1988	10	20		Kyllini, Greece (aftersh)	Ms 4.1	n	not extensional (25)			
1988	10	22		Kyllini, Greece (aftersh)	Ms 4.5	n	not extensional (25)			
1988	10	23		Kyllini, Greece (aftersh)	Ms 4.3	n	not extensional (25)			
1988	10	23		Kyllini, Greece (aftersh)	Ms 4.5	n	not extensional (25)			
1988	10	23		Kyllini, Greece (aftersh)	Ms?	п	not extensional (25)			
1988	10	28		Kyllini, Greece (aftersh)	Ms 4.4	n	not extensional (25)			
1988	10	31		Kyllini, Greece (aftersh)	Ms 4.3	n	not extensional (25)			
1988	10	17		Kyllini, Greece (aftersh)	Ms 4.4	n	not extensional (25)			
1988	11	11		Kyllini, Greece (aftersh)	Ms 4.3	ុក	not extensional (25)			l
1989	1	30	4:06	So Wasatch Plateau, UT	5.12 (27)		West US probably extension		?	
1990	10	24	6:15	Lee Vining, CA	5.29 (27)		West US probably extension	al	?	
1990		21	Γ	Griva, Greece	Ms5.9	<b>Y</b>	extensional (25)		2\2	
1991	2	24		Korinth, Greece	Ms 6.7	n	not extensional (25)		l 0	l
1991	12	3	17:54	Mexicali, Mexico	5.18 (27)		IV/Baja probably extensiona	1	?	
1992	3	13	17:19	Erzincan, Turkey	6.7	Y	extensional(6)	<u> </u>	1\2	<u>y</u>
1992	4	12	1:02	Roermond, Holland	5.31				3\19	У
1992	6	22	17:43		5.7	?	1	1	1\2	1
1992	6	28	11:58	Landers, CA		n	not extens(19)			
1992	6	28		Big Bear, CA	Mw=5.3 (7)	n	not extens(19)	1	0.04	l
1992	6	29	10:14	1	5.7	Y	normal (7)		8\24	y
1992	9	2	10:26		Mw=5.5 (7)	n	no good records			
1992	10	11	13:09		MI=5.9	n	no records			
1993	3	26		Pyrgos, Greece (aftersh)	Ms 5.0	n	not extensional (25)			
1993	3	26		Pyrgos, Greece (aftersh)	Ms 5.1	n	not extensional (25)			
1993	3	26	· · · · · · · · · · · · · · · · · · ·	Pyrgos, Greece (mainsh)	Ms 5.2	n	not extensional (25)	0E)		
1993	3	26		Pyrgos, Greece (attersh)	Ms 4.9	n	bo small, not extensional (			
1993	3	26		Pyrgos, Greece (aftersh)	Ms 4.7	n	po small, not extensional (	C.C		
1993	4	29		Pyrgos, Greece (aftersh)	Ms 4.8	n	o small, not extensional (2		1	1
1993	4	29	8:21	Cataract Creek, AZ	5.27 (27)		West US probably extension	al	?	
1993		17		Eureka Valley, CA	Mw=6.0 (7)	n	3 analog, no digital recs			
1993		14		Patras, Greece	Ms 5.4	n	ixtensional (25), poor digit	12		

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									used\tot	used
Year	Month	day	hr:mn	NAME or LOCATION	Approx MAG	<b>Rivnt?</b>	why	W&S	recs	here?
1993	9	21	3:28	Klammath Falls, OR	Mw=6.0 (7)	Y	normal (7)		?	
1993	9	21	5:45	Klammath Falls, OR	Mw=6.0 (7)	Y	normal (7)		?	
1993	12	4	22:15	Klammath Falls, OR	Mw=5.5 (9)	Y	normal (9)		?	
1994	2	3	9:05	Drainey Peak, ID	Mw=5.7 (7)	Y?	normal (7)		?	
1994	6	7	13:30	Near Borah Peak, ID	5.01-5.12 (28)	V	Vest US probably extensiona	al	?	
1994	9	12	12:23	Double Springs Flat	5.9	Y			1\5	у
1994	9	12	23:57	Double Springs Flat	_(brk)5.0, Md-reno +	n	no digital records, too small			
1995	4	14	0:32	Western Texas	5.62 (27)	٧	Vest US probably extensiona	al 🛛	?	
1995	5	4		Thesaloniki(?), Greece	Ms 5.8	n	data withheld till mid?1996		?	
1995	5	13	8:47	Kozani, Greece	Ms=6.6 (30)	Y	normal (30)		1\1	
1995	5	15	4:13	Kozani, Greece af A	Ms=5.5 (30)	Y	aftershock, prob extensiona		1\1	
1995	5	17	4:14	Kozani, Greece af B	Ms=5.4 (30)	Y	aftershock, prob extensiona	l	1\1	
1995	5	19	6:48	Kozani, Greece af C	M=5.1 (31)	Y	aftershock, prob extensional	l	1\1	
1995	6	11	18:51	Kozani, Greece af D	M=4.8 (31)	Y	aftershock, prob extensional	I	2\2	
1995	6	15		Greece	Ms=6.0? (31)	?	few small recs r>40km (31	)		
1995	8	17		Ridgecrest, CA	ML=5.4 (32)	Y	normal mech (32)		?\5?	
1995	9	20		Ridgecrest, CA	ML=5.8 (32)	Y	str-slip, extensional (32)		?\5?	
1995	11	22	0416?	Gulf of Aqaba	Mw=7.1(33)	?	Probably extensional(29)		2\7	
1995	11	23	18:08	Gulf of Aqaba aft A	ML=5.4(33)	?	Probably extensional(29)		1\1	
1995	12	26	6:19	Gulf of Aqaba aft B	ML=5.0(33)	?	Probably extensional(29)		1\1	
Footno	otes:									
(1) too	small:	none	of the	magnitudes in Table 1	of WS89 equals o	r excee	ds 5.0			
(6) Erz	incan is	strik	e-slip b	ut is in extensional zor	е.					
				JGR, 1995						
				5) report rake = -14 fo	r this event					
(9) from	n Braur	nmille	er et al	(1995)						
				SSA, 1952)						
(11) se	e Maley	/ and	Ethere	dge (1981), also "Seis	mological Notes",.	BSSA,	v72,1982, also McJunkin	and I	Kaliakin (†	981)
(12) se	e Aber	crom	bie et a	al (1995)						
(13) CI	DMG OS	SMS	86-07,	1986						
(14) CI	DMG 05	SMS	87-04, <sup>-</sup>	1988						
(15)NE										
(16) thi	s Imper	ial V	alley ev	ent determined in exte	nsional region					
(17) Lo	ng Valle	ey ar	nd nearl	by events are extension	nal					
(18) As	sociate	d wit	h range	-front normal faults in	extensional zone					
(19) No	extens	ional	strains	seen in geodetics or	in stress indicator	s				

TABLE 8; RECORDS ON	ITTED BECAUSE OF S	TRUCTURE, S	RIGGER, OR POOR DATA QUA	LITY		
GRAY signifies irrelevant	event					
·····					0.4-1-1	
Earthquaka Nanya	Date	Station No	Station Name	bad blgd?	S trig/ bad data?	Notes
Earthquake Name Helena, Montana	1935 1031 1838	22	Helena Fed Bldg	uiyu i v	Dau uala r	bsmt, 4 story bldg
Helena, Montana	1935 1031 1918	2229	Helena Fed Bidg	J V		bsmt, 4 story bldg
Helena, Montana	1935 1121 2028	2220	Helena Fed Bldg	Ý		bsmt, 4 story bldg
Helena, Montana	1935 1128 0742		Helena Fed Bldg	ý		bsmt, 4 story bidg
Imperial Valley	1938 0606 0242	USGS 117	El Centro Array #9	3	v	S trigger
Imperial Valley	1951 0124 0717	USGS 117	El Centro Array #9		ý	S trigger
Imperial Valley	1955 1217 0607	USGS 117	El Centro Array #9		ý	S trigger
Hebgen Lake, MT	1959 0818 0637	USGS	BOZ - Bozeman, MT	v		3 story bldg
Cache Valley, UT	1962 0830 1335	USGS	LOG - Logan, UT	v		3 story bldg
Oroville	1975 0801 2020	CDWR 1051	Oroville Dam Seismograph Statio	n í	v	S trigger
Oroville	1975 0802 2022		OR1 - Up & Down Cafe		v v	S trigger
Thessaloniki, GR	1978 0620 2003	1	Thessaloniki, City Hotel	y		7 story bldg-Hotel
Thessaloniki, GR	1978 0407 0000		Thessaloniki, City Hotel	v.		7 story bldg-Hotel
Valnerina (Norcia) Italy	1979 0919 2135	ENEA	NOU - Nocera Umbra		l v	S trigger
Valnerina (Norcia) Italy	1979 0919 2135	ENEA	ADT - Arquata del Tronto		v	S trigger
Valnerina (Norcia) Italy	1979 0919 2135	ENEA	MAS - Mascioni		v	S trigger
Valnerina (Norcia) Italy	1979 0919 2135	ENEA	- San Vittorino		v	S trigger
Imperial Valley	1979 1015 2316		Plaster City		v	bad data
Imperial Valley	1979 1015 2316	UNAM 6618	Agrarias		Y	z comp bad, other ok
Imperial Valley	1979 1015 2316		SAHOP Casa Flores		y y	bad data
Imperial Valley	1979 1015 2316	CDMG 5169	Westmorland Fire Sta		У	z comp bad, other ok
Mammoth Lakes	1980 0525 1634	CDMG 54214	Long Valley Dam (Upr L Abut)	у		upper left abutment records contaminated
Mammoth Lakes	1980 0525 1649		Long Valley Dam (Upr L Abut)	y		upper left abutment records contaminated
Mammoth Lakes	1980 0525 1944	CDMG 54214	Long Valley Dam (Upr L Abut)	У		upper left abutment records contaminated
Mammoth Lakes	1980 0525 2035	CDMG 54214	Long Valley Dam (Upr L Abut)	У		upper left abutment records contaminated
Mammoth Lakes	1980 0526 1858	CDMG 54214	Long Valley Dam (Upr L Abut)	y		upper left abutment records contaminated
Mammoth Lakes	1980 0527 1451	CDMG 54214	Long Valley Dam (Upr L Abut)	У		upper left abutment records contaminated
Mammoth Lakes	1980 0531 1516	USC 35	Long Valley Fire Sta		у	S trigger
Victoria, Mexico	1980 0609 0328	UNAM 6604	Cerro Prieto			bad data
Victoria, Mexico	1980 0609 0328		Mexicali Hosp Sot.		у	S trigger
Victoria, Mexico	1980 0609 0328		Victoria		У	glitchy digital data
Victoria, Mexico	1980 0609 0328	UNAM 6624	Victoria Hospital Sotano		У	S trigger
Mammoth Lakes	1980 0611 0441	USGS 45	MGE - McGee Creek		ý	S trigger
Mammoth Lakes	1980 0611 0441	USC 40	USC Convict Lakes		у	S trigger
Campania (Irpinia)	1980 1123 1834	ENEA	AU3 - Auletta		У	S trigger
Campania (Irpinia)	1980 1123 1834	ENEA	BZ4 - Brienza		У	S trigger
Campania (Irpinia)	1980 1123 1834	ENEA	GA4 - Garigliano		У	S trigger
Campania (Irpinia)	1980 1123 1834	ENEA	SS4 - San Severo		у	S trigger
Campania (Irpinia)	1980 1123 1834	ENEA	VI4 - Vieste		у	S trigger

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Table 8 p 1/2

Campania (Irpinia)	Date					
Campania (Irpinia)	Date	Station No	Station Name	blgd?	bad data?	Notes
	1980 1123 1834	ENEA	TC4 - Tricarico		у	S trigger
Biga, Turkey	1983 0705 12:01	ERI	GON - Goenen		у	poor digitization
Biga, Turkey	1983 0705 1201		EDK - Edincik		У	poor digitization
Biga, Turkey	1983 0705 1201		BSR - Balikesir		У	poor digitization
Biga, Turkey	1983 0705 1201	ERI	EDR - Edremit		У	poor digitization
Borah Peak, ID	1983 1028 1406	INEL	ANL 767	У		basement, 6-story bldg
Borah Peak, ID	1983 1028 1406	INEL	ANL 768	y		basement, 4 story bldg
Borah Peak, ID	1983 1028 1406	INEL	CPP-601 basement	y		10 m deep embedment in soil
Borah Peak, ID	1983 1028 1406	INEL	PBF-620	y		second basement, reactor building
	1983 1028 1406	INEL	TRA-642	y		basement, 4-story bldg
Borah Peak, ID Borah Peak, ID	1983 1028 1406	INEL	TRA-670	y		4 story building
Lazio-Abruzzo, Italy	1984 0507 1749		Bussi		у	S trigger
Lazio-Abruzzo, Italy	1984 0507 1749	ENEA	LDP - Lama dei Peligni		y	S trigger
Lazio-Abruzzo, Italy	1984 0507 1749	ENEA	MAN - Manoppello		y	S trigger
Lazio-Abruzzo, Italy	1984 0507 1749	ENEA	ORT - Ortucchio		y	S trigger
Granada, Spain	1984 0624	IGN	Beznar		y	Dam abutment, S trigger
Granada, Spain Granada, Spain	1984 0624	IGN	Alhama		У	bad data
Granada, Spain Granada, Spain	1984 0624	NARS	NE14		У	bad data
Edessa, Greece	1984 0709	1.4.4.4	Edessa	y		5-story bldg, basement
Edessa, Greece	1984 0709	1	Veroia	У		3-story bldg, basement
	1985 1109	1	Drama	y		4-story, basement
Drama, Greece	1986 0721 1442	CDMG 54424	Bishop - Paradise Lodge		у	S trigger
Chalfant Valley Chalfant Valley	1986 0721 1442	CDMG 54214	Long Valley Dam (L Abut)	У		left abutment not used; downstream available
Kalamata, Greece	1986 0913 1724	1001110 0 1211	Kalamata	ý		7, 4-story, basement
Kalamata, Greece	1986 0915 1141		Kalamata	ý		7, 4-story, basement
	1986 0915 1141		Kalamata-2	ý		7, 4-story, basement
Kalamata, Greece	1986 1010 1749	1	HCR Hotel El Camino Real	y		10-story, 2nd floor
San Salvador	1986 1010 1749		HSH Hotel Sheraton	y		10-story, 1st floor
San Salvador San Salvador	1986 1010 1749		IVU Inst. Urban Construction	у		6-story, 1st floor
	1986 1010 1749		UCA Centro Americana Un.	y		6-story, 1st floor
San Salvador San Salvador	1986 1010 1749		MDE Minist de Educacion	У		4-story, 1st floor
	1987 0302 0151		Maraenui Primary School		У	S trigger
Edgecomb, NZ Superstitn Hills (A)	1987 1124 0154	<b>USGS 5210</b>	Wildlife Liquef. Array		У	local liquefaction affected record
	1990 1221		Edessa	y		5-story, basement
Griva, Greece	1992 0622 1743	GNS	Kawerau Police St.		У	S trigger
Matata, New Zealand Double Springs Flat	1992 0022 1745		Indian Creek Dam	V		earth dam crest

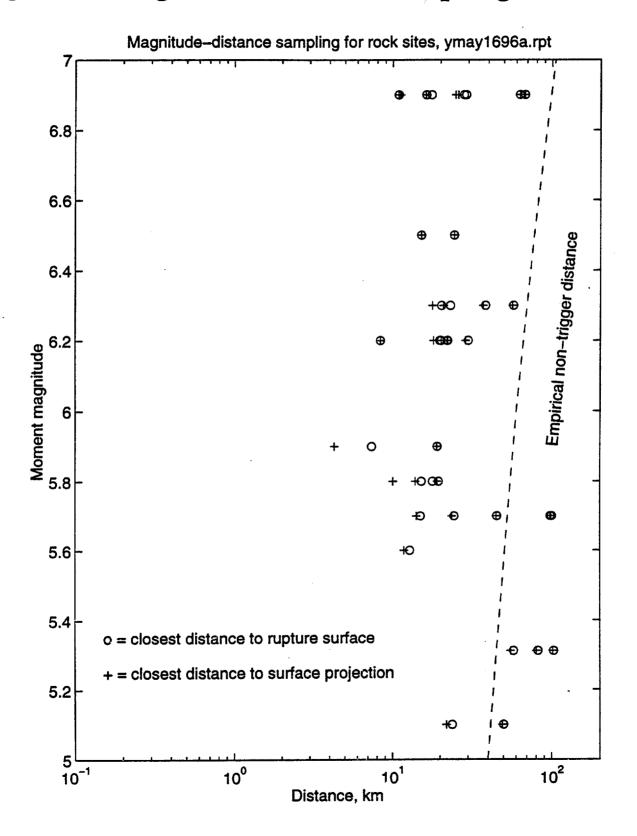
Table 8

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p2/2

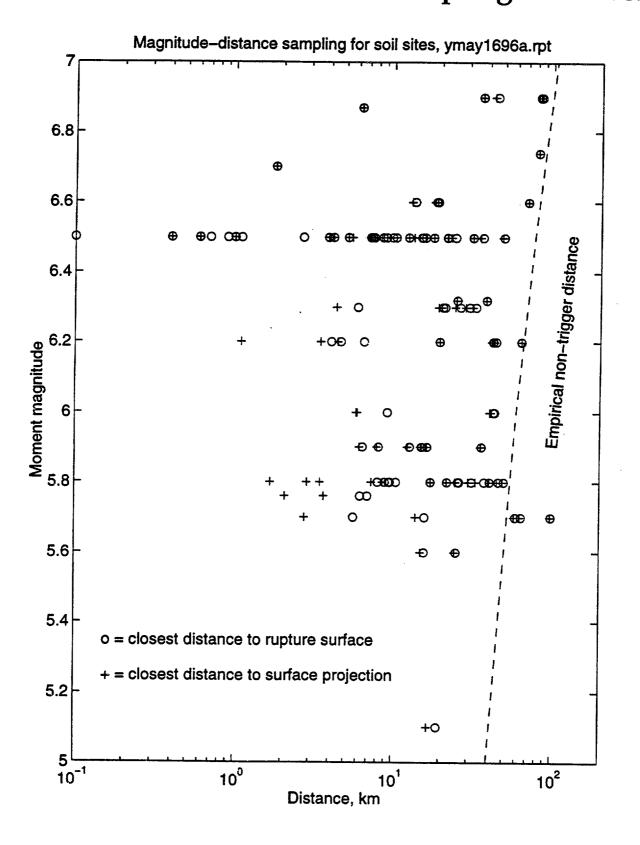
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## Figure 1. Magnitude-distance sampling for rock sites



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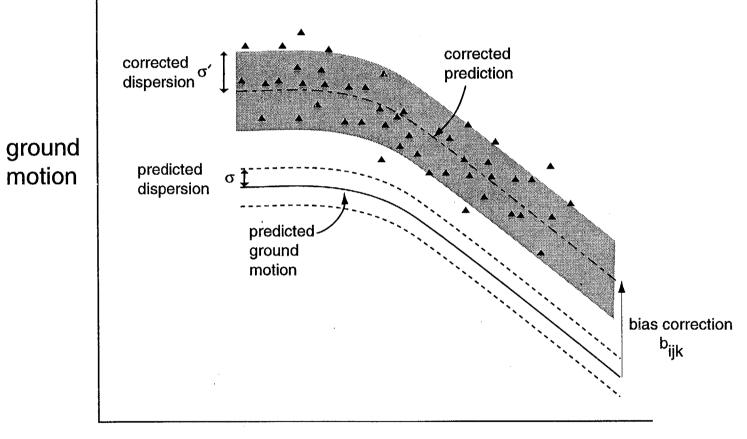
# Figure 2. Magnitude-distance sampling for soil sites



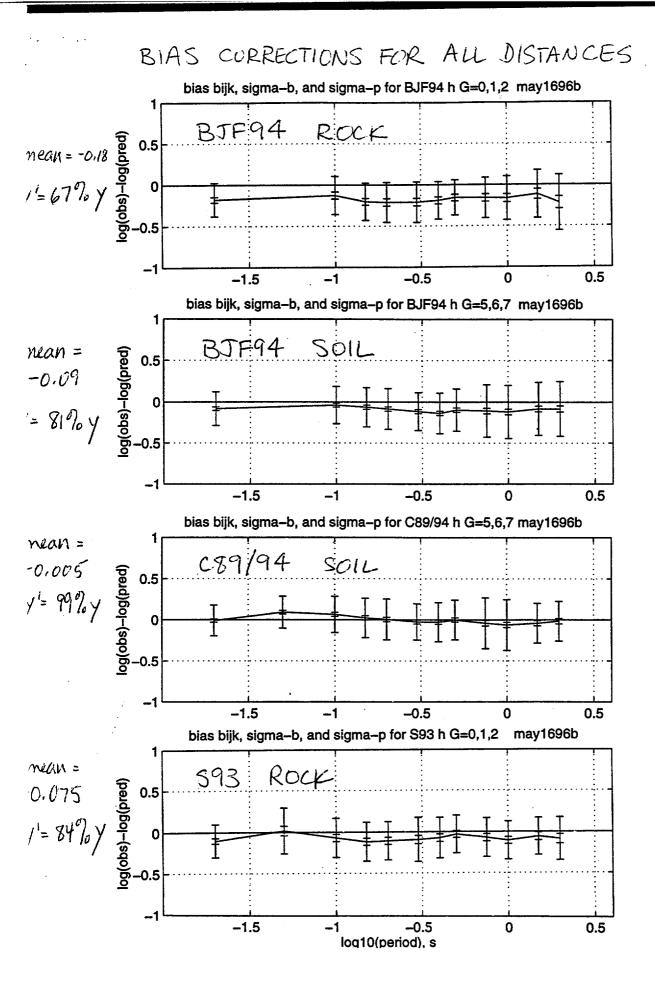
## NOTE: throughout this work,

 $\log = \log_{10}$ 

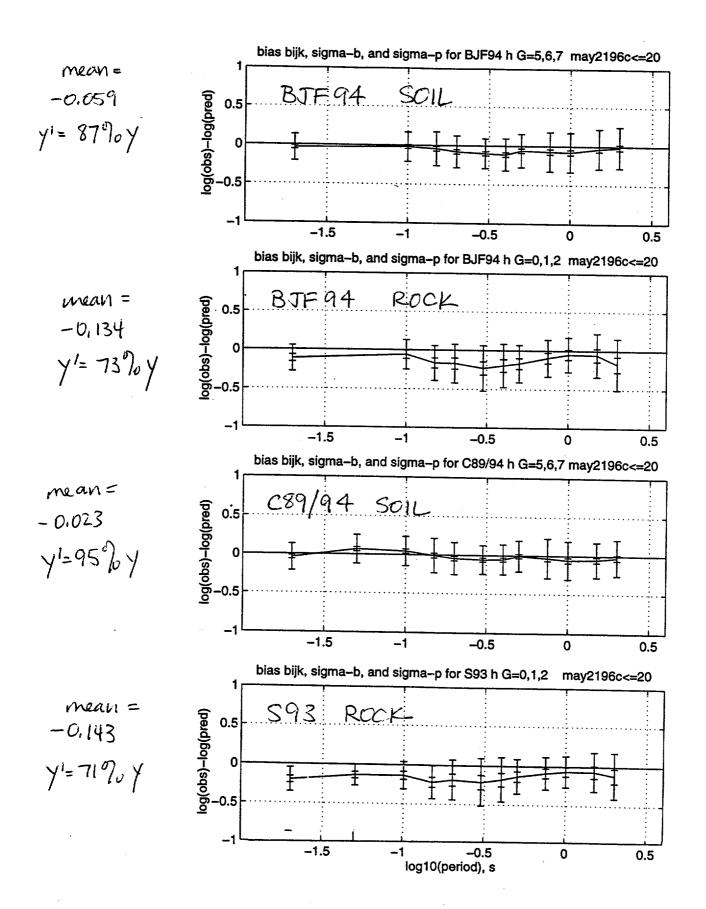
Illustration of bias correction and dispersion correction



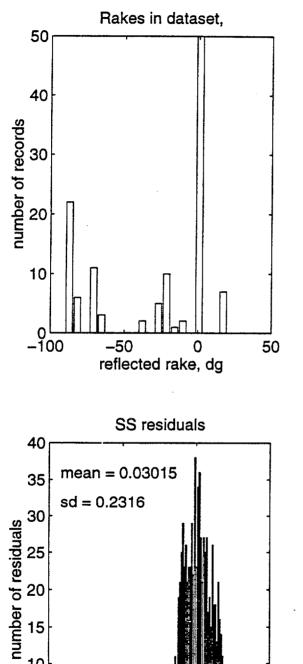
distance



BIAS CORRECTIONS FOR DISTANCES & 20 KM



### Figure 8. Comparison of predicted residuals showing strike slip events to have larger motions than normal faulting events (with caveats).



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0<sup>L</sup> -2

-1

may2196b w/o TAN

mean normal residual = -0.01254

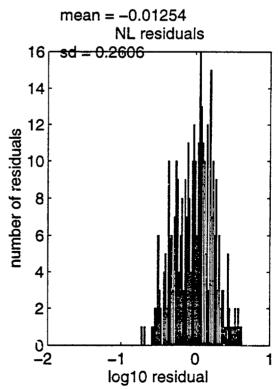
no. of normal residuals = 343

mean str-sl residual = 0.03015

no. of str-sl residuals = 837

Students t value =-2.77

Probability means differ = 0.9943



1

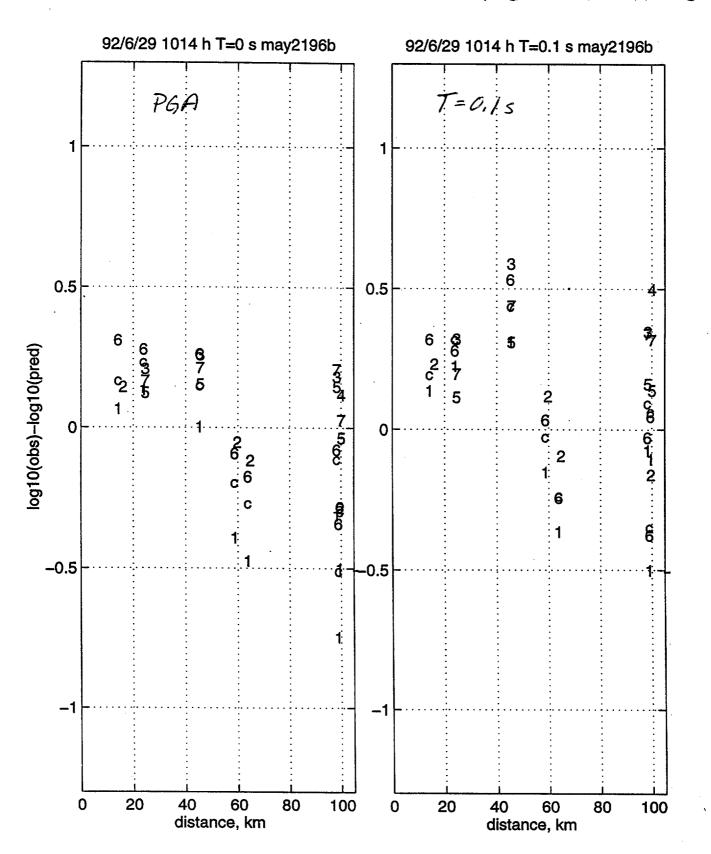
0

log10 residual

### CAVEAT:

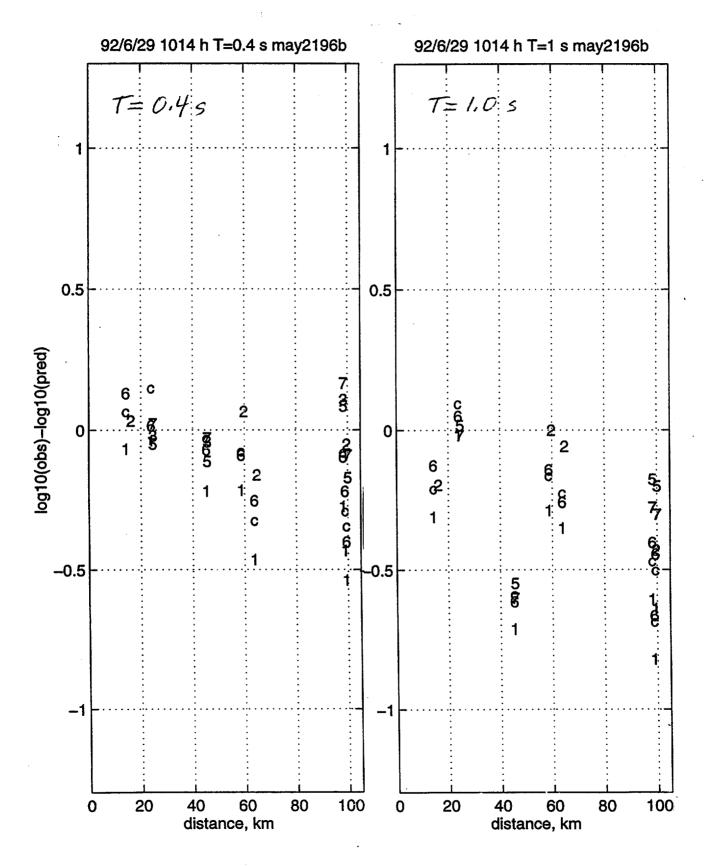
The difference in ground motions between strike-slip and normal faulting events depends on the selection of a reference curve used to calculate residuals. Use of Idriss(1993) or Sadigh et al. (1993) as reference curves leads to strike-slip ground motions *larger* than normal faulting ground motions. SEA96 is probably the more appropriate reference curve because it was derived from this data set using a twostep regression that reduces unwanted correlations. It suffers less distance-dependent residuals than the others, but its residuals are more magnitude-dependent.

## Comparison of Little Skull Mountain ground motions with predictions of various authors

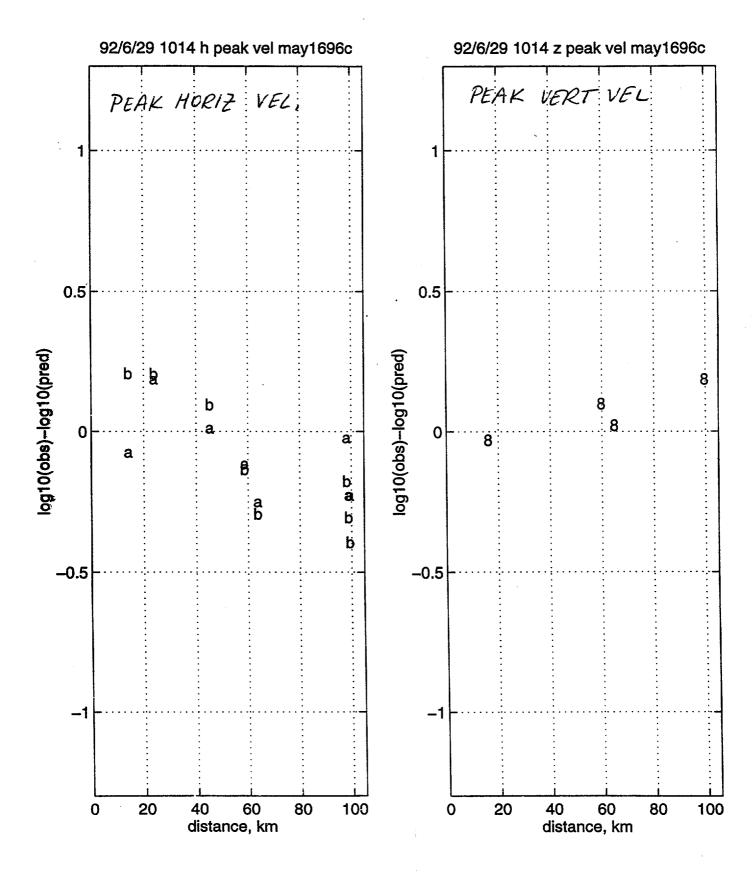


### COMPARISON OF LITTLE SKULL MOUNTAIN HORIZONTAL FGA/PSV WITH VARIOUS FREDICESTIVE RELATIONS

23a



23d



22n

Develop attenuation curves as a function of frequency from weak motion data

Use data from the Little Skull Mountain aftershocks recorded on the Southern Great Basin Seismic Network

Ground motion spectra assumed proportional to

 $S(f) r^{-\gamma} e^{-\pi f(\kappa + T/Q)}$ 

where T is travel time, r is distance, and S(f) is a site response spectrum.

Parameters to be determined:

S(f), site response spectra for groups of stations

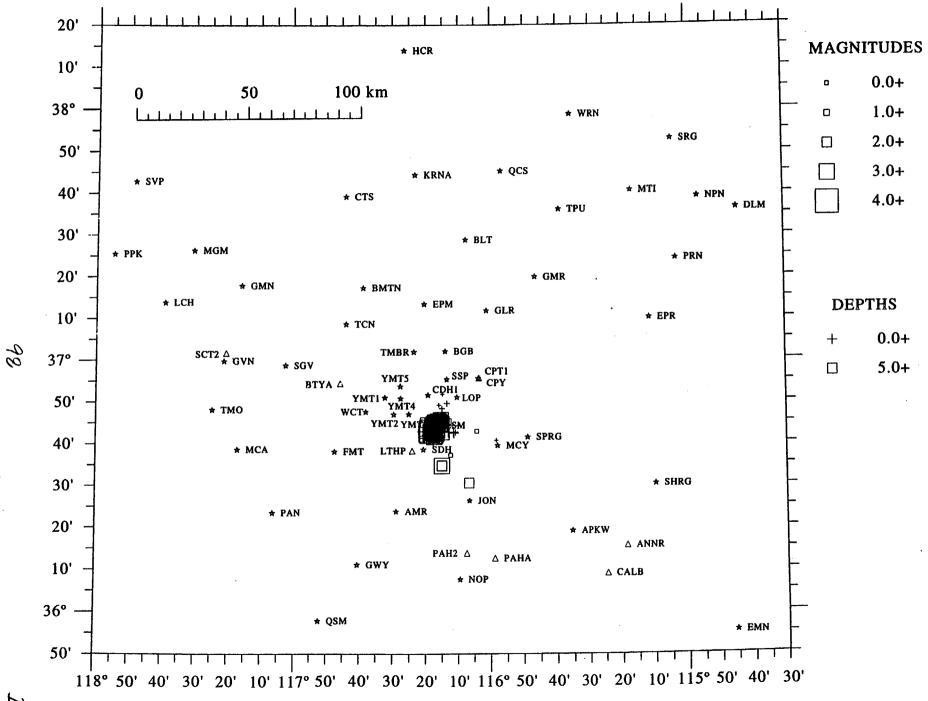
 $\gamma$ , accounts for geometrical spreading

Q is a whole path anelastic attenuation

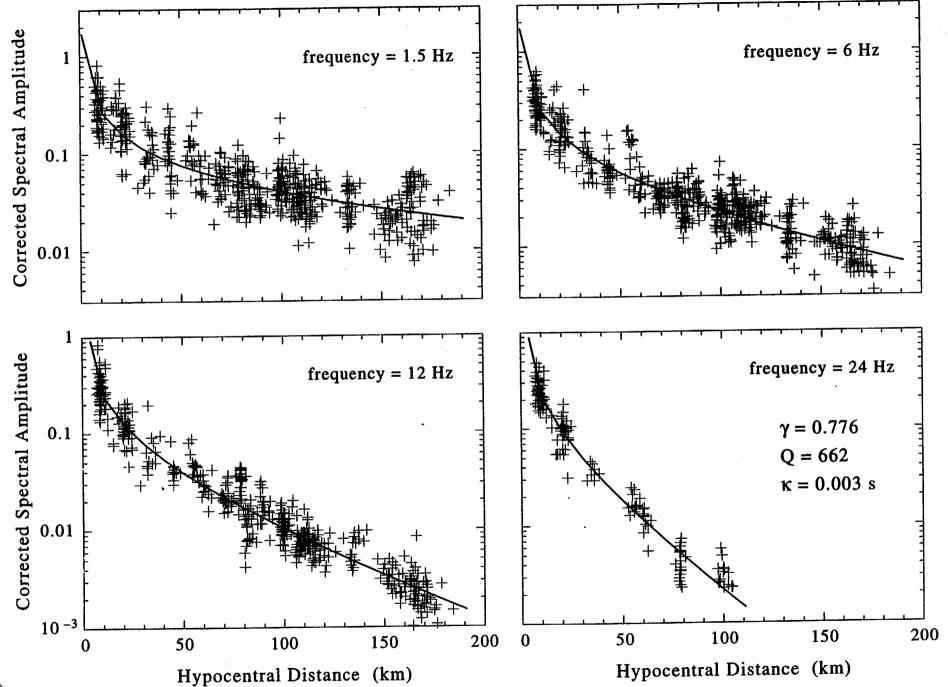
assumed either constant or frequency dependent:

 $Q(f) = Q_0 f^{\alpha}$ 

 $\kappa$  is an average value for all stations and includes the effect of near-station attenuation. (Boatwright, Fletcher, and Fumal, BSSA, 1991; Boatwright, BSSA, 1994).



N



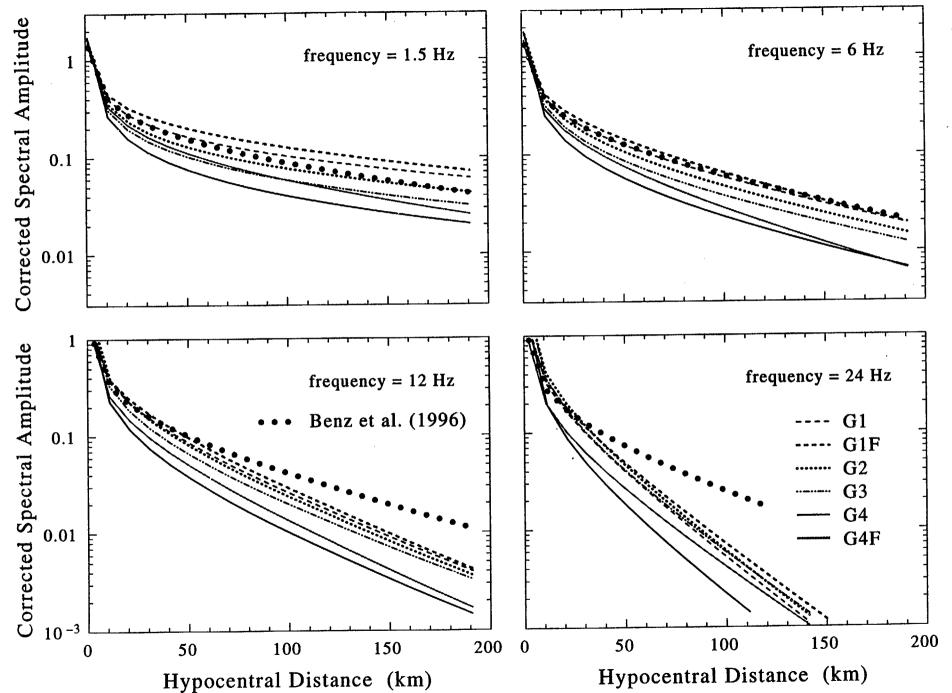
10/

4

grouping	#g	variance	γ	Qo	Q(16)	α	ĸ	median f <sub>C</sub>
G1	3	0.725%	0.526	623	623	0.0	-0.002 s	13.48 Hz
G1F	3	0.722%	0.450	401	608	0.15	-0.001 s	12.87 Hz
G2	8	0.508%	0.609	643	643	0.0	-0.007 s	11.12 Hz
G3	8	0.494%	0.684	706	706	0.0	-0.007 s	10.55 Hz
G4	8	0.394%	0.776	662	662	0.0	+0.003 s	12.41 Hz
G41	8	0.390%	0.722	489	642	0.1	+0.003 s	12.57 Hz
G43	8	0.385%	0.625	274	629	0.3	+0.004 s	12.61 Hz
G4F	8	0.385%	0.601	238	628	0.35	+0.002 s	12.31 Hz
G45	8	0.387%	0.539	159	637	0.5	+0.005 s	11.90 Hz
G47	8	0.399%	0.514	100	696	0.7	+0.007 s	10.59 Hz

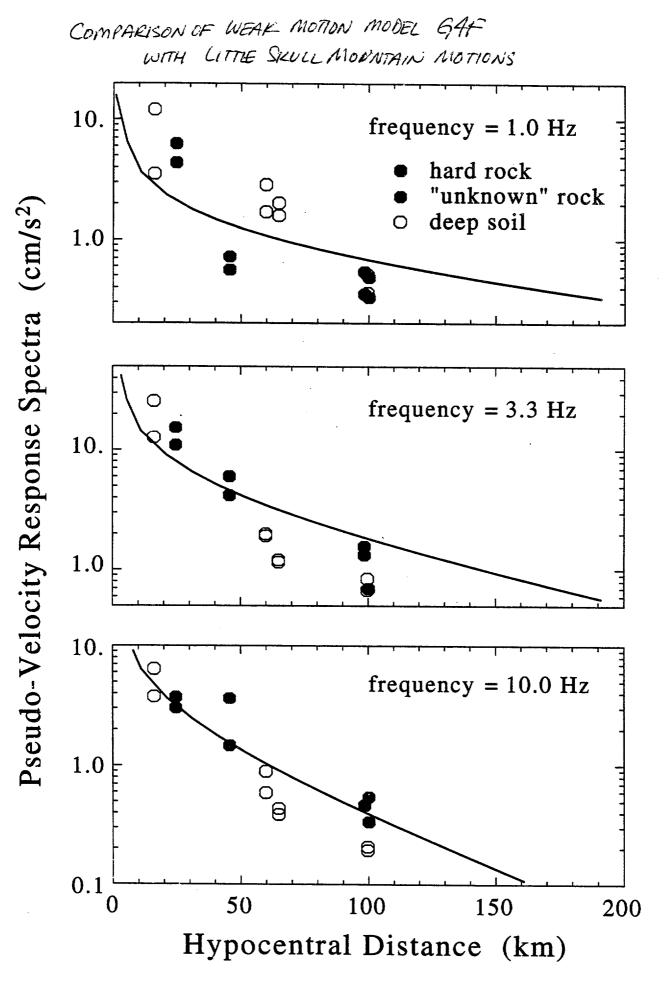
Table 2. Propagation Parameters

Table 2 p1/1



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Results of weak motion study

Considerable tradeoff between geometric spreading exponent  $\gamma$  and  $\alpha$ , exponent of f in frequency dependence of Q

Difficult to define frequency dependence of Q

Q at 16 Hz is 600 - 700 in all models, frequency dependent and independent

κ in the 0.002 - 0.007 range

LSM aftershock ground motions decay with distance a little faster than the result of Benz et al. (1996)

Weak motion decay of ground motion with distance roughly comparable to that observed for Little Skull Mountain strong motion data

### STRESS DROPS IN NORMAL FAULTING EARTHQUAKES

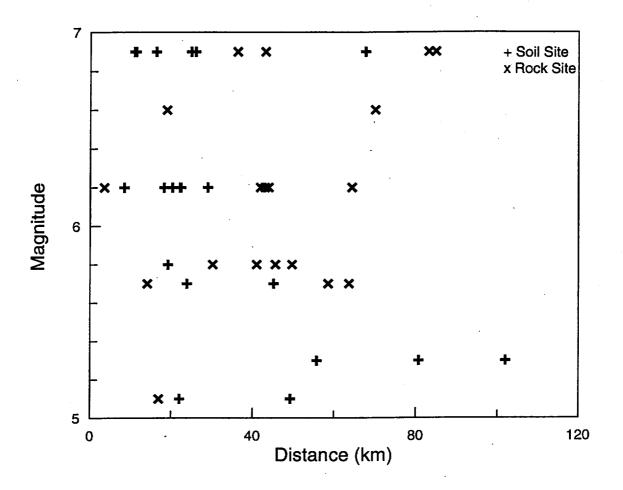
#### GROUND MOTION CHARACTERIZATION WORKSHOP #2

Ann Becker 9 January 1997

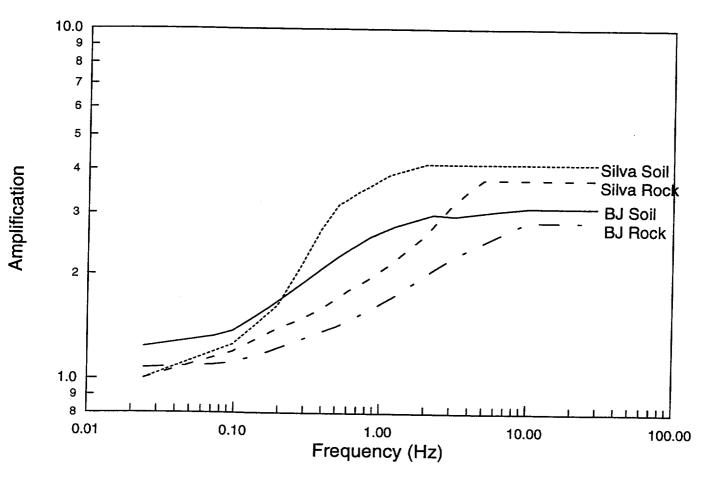
	Date	M <sub>w</sub>	Number of	Nr. 1 C
	Duit	IVIW		Number of
Aleman	5/5/04		Rock <sup>2</sup> Sites	Soil <sup>3</sup> Sites
Abruzzo	5/7/84	5.8	1	4
	17:50		(19.2 km)	(30.2, 41.0,
				45.6, 49.7)
Borah Peak	10/29/83	5.1	2	1
(Aftershock)	23:29		(22.0, 49.3)	(16.9)
Borah Peak	10/28/83	6.9	0	2
(Main Shock)	14:06			(83.1, 84.9)
Irpinia A	11/23/80	6.9	6	2
	19:34:54		(10.9, 11.2, 16.2,	(36.3, 43.1)
			24.9, 25.9, 67.7)	(2010, 1011)
Irpinia B	11/23/80	6.2	6	4
	19:35:04		(8.4, 18.2, 20.3,	(41.9, 43.0,
			22.1, 22.3, 28.9)	43.9, 64.4)
Little Skull	6/29/92	5.7	2	3
Mtn.	10:14		(23.8, 45.2)	(14.1, 58.6, 63.7)
Managua	12/23/72	6.2	0	1
	6:29			(3.5)
New Zealand	3/2/87	6.6	0	2
	1:42		-	(18.9, 70.1)
Roermond	4/13/92	5.3	3	0
	1:20		(55.8, 80.7, 102.1)	v

## EVENTS SELECTED FOR INVERSION<sup>1</sup>

<sup>1</sup> Selection criterion was a predominantly normal mechanism (rake between -45° and -135°) <sup>2</sup> Hard or soft rock (Spudich et al. classes 0, 1, 2) <sup>3</sup> Deep or shallow soil (Spudich et al. classes 5, 6, 7)



#### Magnitude and Distance Distribution Events used in Q/kappa Inversion



**Transfer Functions used in Inversion** 

### **INVERSION RESULTS**

Run #	1	2	3	4
Number of 'Sites'	32	12	32	32
Q	200 <sup>1</sup>	200 <sup>1</sup>	$200^{1}$	346 <sup>1</sup>
η	0.41	0.41	0.41	0.531
Transfer Function	Silva	Silva	Boore-	Silva
			Joyner	
Stress Drop (bars)	··· · · · · · · · · · · · · · · · · ·	<u>,</u>		
Abruzzo	.95	95	165	82
Borah A/S	18	24	30	17
Borah M/S	42	42	69	· 32
Irpinia A	30	32	49	27
Irpinia B	28	27	47	25
LSM	45	33	74	29
Managua	16	16	27	16
NZ	31	31	51	26
Roermond	49	49	91	35
Median	32	34	58	29
Median ĸ, all sites	0.047	0.042	0.048	0.058
Mean $\kappa$ , rock sites	$0.057 \pm$		0.059 ±	0.066 ±
	0.021	× .	0.021	0.020
Mean k, soil sites	0.047 ±		0.048 ±	$0.057 \pm$
	0.018		0.018	0.016
κ (sec)	-			
Abruzzo	0.061	$0.058/0.062^2$	0.063	0.069
Borah A/S	0.033	0.048/0.043 <sup>2</sup>	0.034	0.041
Borah M/S	0.013	$/0.013^{2}$	0.014	0.033
Italy	0.062	$0.067/0.055^2$	0.063	0.070
LSM	0.036	0.016/0.031 <sup>2</sup>	0.037	0.041
Managua	0.066	/0.066 <sup>2</sup>	0.067	0.067
NZ	0.045	$/0.045^{2}$	0.046	0.056
Roermond	0.062	0.062/2	0.065	0.080

<sup>1</sup> Value fixed

<sup>2</sup> Rock value/soil value

#### CONCLUSIONS

Silva:

6 California events Mean magnitude 6.25 Strike-slip Median  $\Delta \sigma$  37 bars  $\kappa \approx 0.05$  cf:

9 Normal earthquakes Mean magnitude 6.1 Normal faulting Median  $\Delta \sigma$  29 bars  $\kappa$  0.047 sec

Boore-Joyner: WNA events Magnitude 6.5 Mixed mechanisms Median  $\Delta \sigma$  70 - 100 bars  $\kappa$  0.035

cf:

9 Normal earthquakes Mean magnitude 6.1 Normal faulting Median  $\Delta \sigma$  58 bars  $\kappa$  0.048

#### **Dinar Earthquake Project**

John Anderson

✓ Where is Dinar?

✓ Plot of the earthquake and station distribution?

✓ Plot of accelerograms.

Map with aftershock locations (Suzi will do)

Source properties

- ✓ moment magnitude (Have Harvard CMT. Suzi will check USGS & Tokyo)
- static stress drop (JA will do)
- ✓ rupture plane (dimensions and dip) (modify if data demand)

Strong Motion - basic analysis

- ✓ Closest distances (Rupture and JB dist) for each station
- Plot of velocity (Yuehua will do)
- Plot of displacement (Yueha will do)
- Fourier spectra (Suzi will do. May allow educated guess of basin depth at Dinar.)
- response spectra at 5% damping (Yuehua will do)
- RMS stress drop (Suzi will do)

Path Properties:

- velocity structure and Q (Erzinincan, northern Nevada & Yucca Mtn models available. Suzi will look for others. Q an educated guess, test with synthetics.)

Site Properties:

- site classification (Dinar has good information. Suzi will look for geologic map of Turkey for the other sites.)
- kappa from weak motion (aftershocks) and strong motion (Suzi will do)

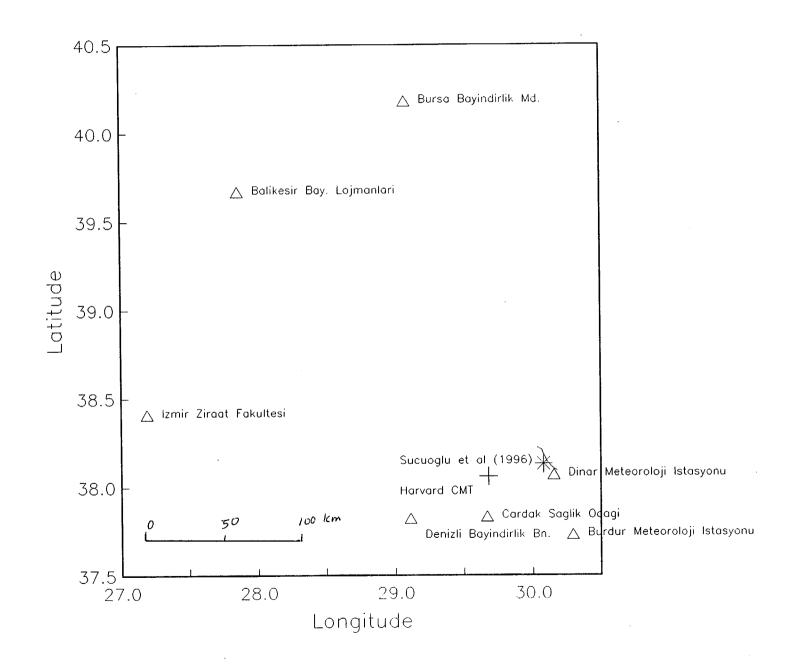
Source model

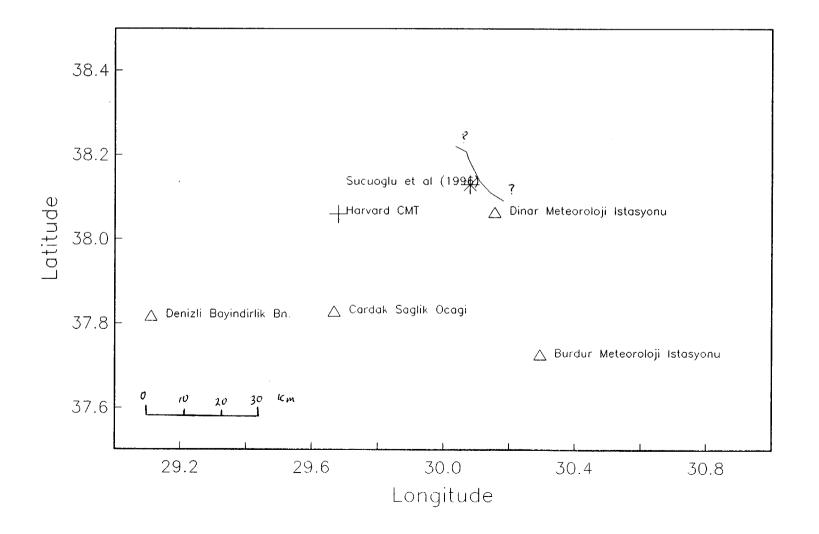
- Composite source model to match statistical properties (Yuehua will do)
- Specific composite source model (Yuehau will do)

Write report (All contribute, JA coordinate) Target date Feb 96.



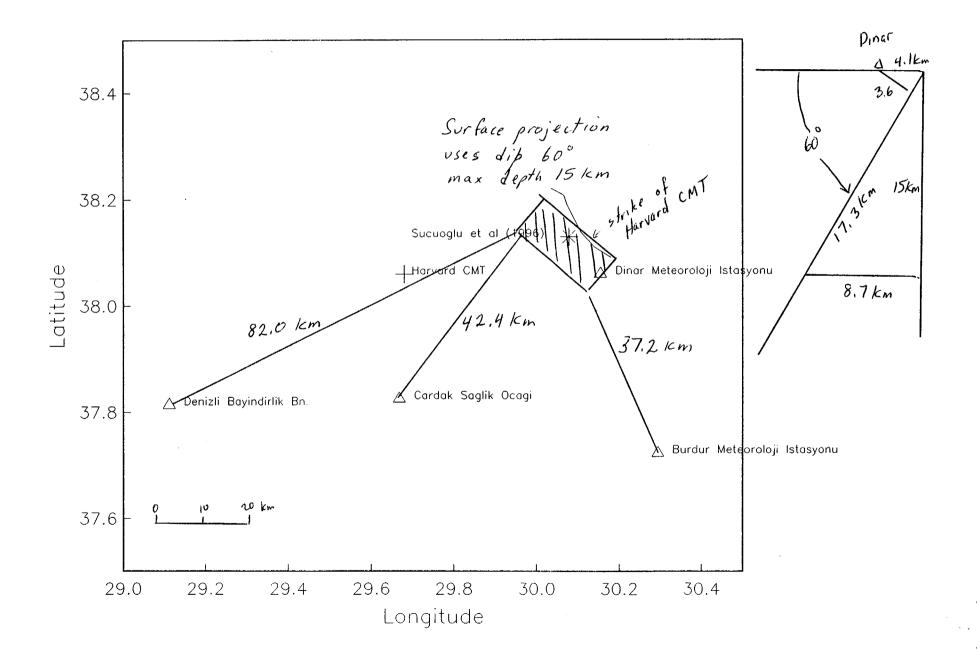
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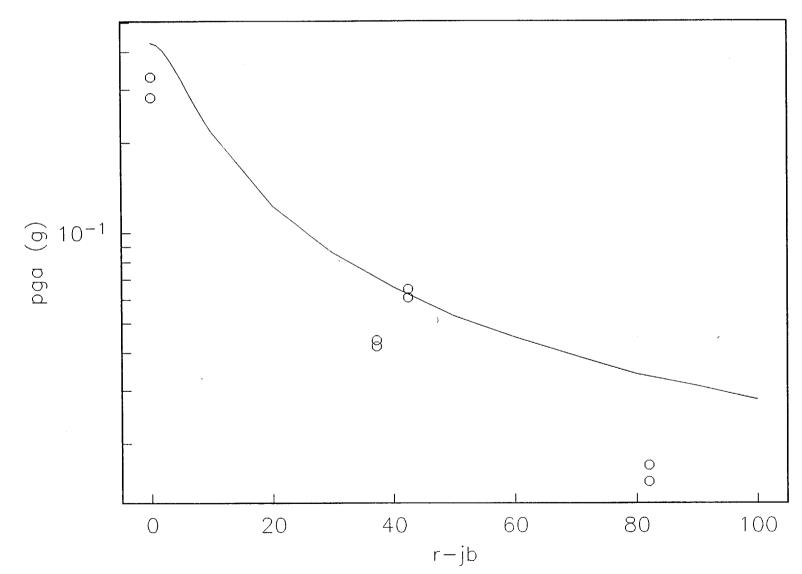




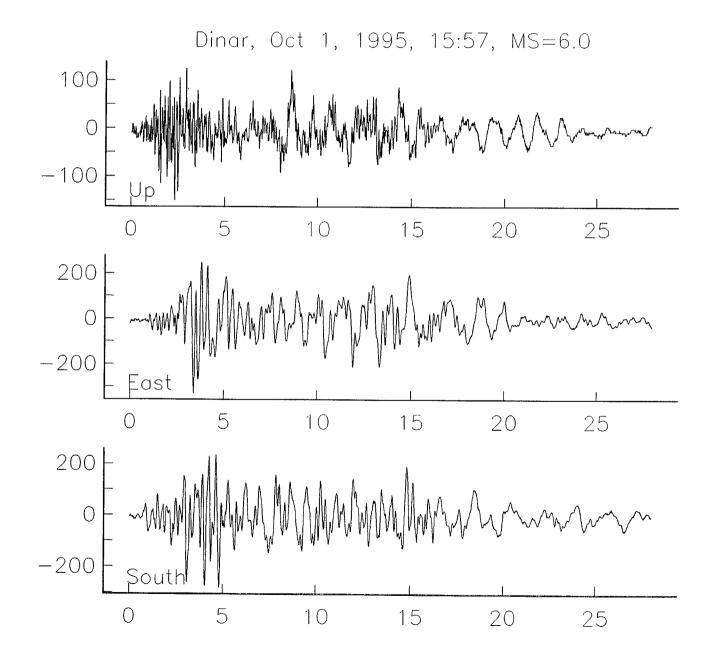
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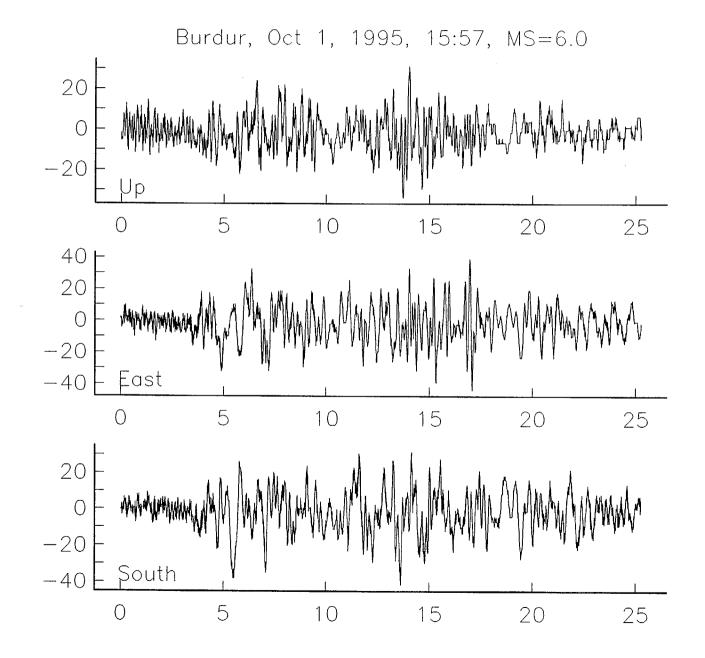


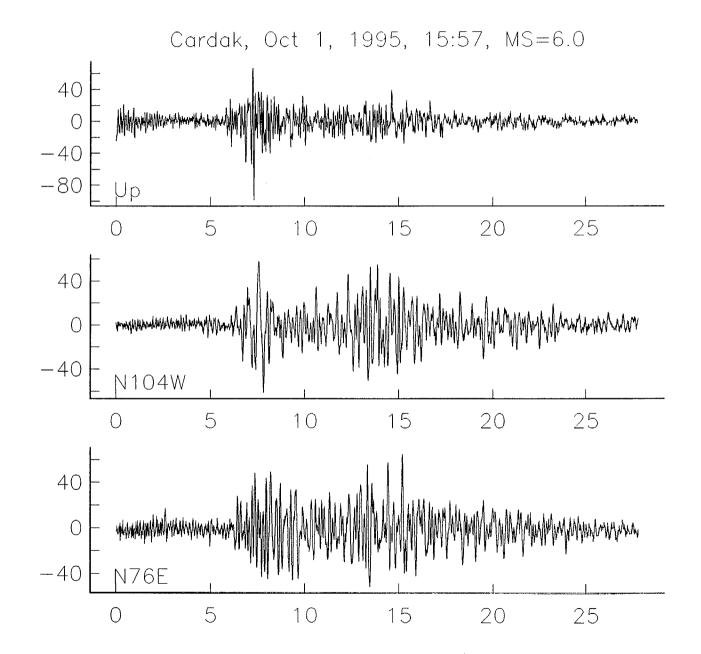


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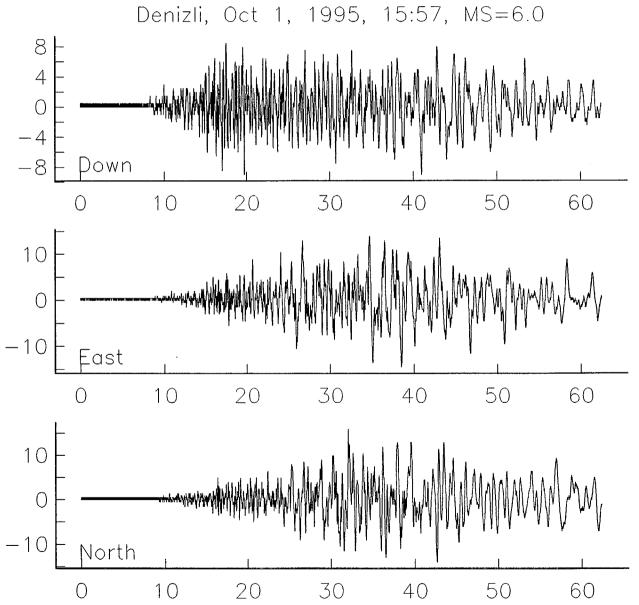


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# Seismic Energy and Stress-Drop Parameters for a Composite Source Model

by John G. Anderson

Abstract This article examines relationships among radiated energy and several stress-drop parameters that are used to describe earthquake faulting. This is done in the context of a composite source model that has been quite successful in its ability to reproduce statistical characteristics of strong-motion accelerograms. The main feature of the composite source model is a superposition of subevents with a fractal distribution of sizes, but all with the same subevent stress drop  $(\Delta \sigma_d)$  that is independent of the static stress drop  $(\Delta \sigma_s)$ . In the model,  $\Delta \sigma_d$  is intended to represent the effective dynamic stress, and it does this well when  $\Delta \sigma_d > 2\Delta \sigma_s$ . The radiated energy in the S wave is  $E_S^{CS} = 0.233 C_E (\Delta \sigma_d/\mu) M_0$ , where  $M_0$  is the seismic moment of the earthquake,  $\mu$  is shear modulus, and  $C_E$  is a dimensionless parameter that equals unity when  $\Delta \sigma_d > 2\Delta \sigma_s$ . The apparent stress  $(\sigma_a)$  is  $\sigma_a = 0.233 C_E \Delta \sigma_d$ . The effective stress is  $\sigma_e \approx 0.44C_E \Delta \sigma_d$ . The Orowan stress drop  $(\Delta \sigma_o)$  is  $\Delta \sigma_o = 0.486 \Delta \sigma_d$ . The root-mean-square (rms) stress drop

$$(\Delta\sigma_{\rm rms})$$
 is  $\Delta\sigma_{\rm rms} = \Delta\sigma_d I_{\theta}^{1/2} \left(\frac{M_0}{M_{os}(R_{\rm max})}\right)^{1/2} \left(\frac{f_c}{f_o}\right)^{1/2}$ ,

where  $f_0$  is corner frequency of the earthquake,  $M_{os}$  ( $R_{max}$ ) and  $f_c$  are the moment and corner frequency of the largest subevent, and  $I_{\theta}^{1/2}$  is a dimensionless constant approximately equal to 1.7. Finally, the Savage-Wood ratio (SWR) is given by SWR  $\approx C_E \Delta \sigma_d/2 \Delta \sigma_s$ . These results clarify the relationships among all of these stress parameters in the context of a complex fault, showing the critical role of the subevent stress drop. They also provide an additional tool for energy, stress, and Savage-Wood ratio estimation. Since the process of modeling strong motion with the composite source uses realistic Green's functions, estimates of energy and stress parameters using this model are expected to have a good correction for wave propagation.

### Introduction

The use of strong-motion accelerograms to estimate the seismic energy release in earthquakes is somewhat problematical. One difficulty is geometrical since at this range the large extent of faulting cannot be ignored. Another difficulty is introduced by the complexities of wave propagation, since site effects, resonances, and a complex mixture of body and surface waves that are not easily separated all contribute to the accelerograms. Thus, methods that derive energy by integrating the observed velocity or its spectrum (e.g., Anderson et al., 1986; Shoja-Taheri and Anderson, 1988) inevitably make some simplifying assumptions whose importance is difficult to assess. Another approach to computing energy is to calculate the energy leaving the source (e.g., Haskell, 1964; Vassiliou and Kanamori, 1982), but at strong-motion distances, typical source models are limited to modeling the low-frequency portion of the spectrum. On many accelerograms, the majority of the energy is carried in waves with frequencies below 1 to 3 Hz (e.g., Vassiliou and Kanamori, 1982; Shoja-Taheri and Anderson, 1988). Still, a method

that more naturally incorporates the full frequency band is desirable.

Recently, Yu (1994) and Zeng et al. (1994) have proposed a composite source model for generating synthetic strong-motion accelerograms. Besides the composite source, which is discussed below, these synthetics utilize synthetic Green's functions generated for a layered medium. Several articles have demonstrated that the synthetics generated with this model are highly realistic, both in appearance in the time domain and in reproducing spectral amplitudes over the entire frequency band (Yu, 1994; Zeng et al., 1994; Yu et al., 1995; Su et al., 1994a, 1994b; Anderson and Yu, 1996; Zeng and Anderson, 1996). Considering this realism, it seems natural to see if it is possible to estimate the energy that leaves the composite source. Thus, the initial motivation for this article is to derive an analytical expression for the seismic energy leaving a composite source as a function of the model parameters.

In the process, it became apparent that in addition to

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energy, it is possible to derive analytical expressions for several of the commonly used stress parameters in the context of this model: apparent stress (Wyss, 1970), effective stress (Brune, 1970), Orowan stress drop (Kanamori, 1977; Vassiliou and Kanamori, 1982), and root-mean-square (rms) stress drop (Hanks, 1979; Hanks and McGuire, 1981). The results give some insight into the meaning of these parameters in the context of a source that is much more complex than the models that are the basis for their original definitions. Even though the composite source is a kinematic model, it is reasonable to expect that characteristics of these relationships will carry over to future models that more thoroughly incorporate the physics of complex faulting.

### Theory

### Composite Source Model

As described by Zeng *et al.* (1994), the composite source model consists of a superposition of radiation from a number of point sources on the fault. The point sources have a distribution of "sizes"

$$n(R) = pR^{-D-1} \tag{1}$$

in which n(R) is the number density of sources with equivalent "radius" R, D is a fractal dimension (generally taken to be 2.0), and p is a constant defined by the constraint that the sum of the moments of the subevents is equal to the moment of the target event. The subevents all have a radius between  $R_{max}$  and  $R_{min}$ . In general,  $R_{min}$  can be chosen small enough that it has no numerical consequences. The subevents are placed at random, with a uniform probability distribution, on the fault plane, with the constraint that their edges do not overlap the edge of the fault; this places an upper limit on  $R_{max}$ . The source time function is generated by starting the rupture at a presumed hypocenter and allowing it to spread at a constant rupture velocity across the fault. Each subevent radiates a time function when the rupture front reaches its center.

Figure 1 shows a view of the slip for one realization of this source. To develop this, I treat each source as a crack with slip function:

$$s(a) = \frac{24}{7\pi} \frac{\Delta \sigma_d}{\mu} (R^2 - a^2)^{1/2},$$
 (2)

where  $\mu$  is the shear modulus, R is the radius of the crack, a is the distance from its center, and  $\Delta \sigma_d$  is the stress drop of the subevent. Figure 1 shows a relatively complex slip distribution resembling a fractal computer-generated topography and the self-similar slip distributions presented by Herrero and Bernard (1994).

Figures 2 through 4 investigate this source and its dependence on the subevent stress drop. Figure 2 shows realizations of the composite source time function for a rectanpg 2



Figure 1. A perspective view of the "slip function" on a fault for the composite source model.

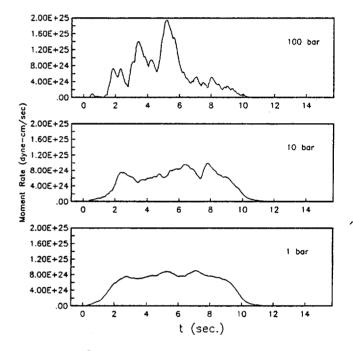


Figure 2. Realizations of the moment rate of a composite source for three values of the subevent stress drop. The fault has length L = 30 km and width W = 10 km. The three values of subevent stress drop are  $\Delta \sigma_d = 1$ , 10, and 100 bars, as shown. The fault has  $M_0 = 6 \times 10^{25}$  dyne-cm, and according to equation (3), it has  $\Delta \sigma_r = 12.7$  bars for all three cases.

gular fault (expressed as seismic moment rate) with three values of  $\Delta \sigma_d$ : 1, 10, and 100 bars. It is evident that lower values of  $\Delta \sigma_d$  are associated with a smoother time function. Figure 3 shows average spectra associated with these three values of  $\Delta \sigma_d$ . Figure 4 is the equivalent of Figure 3, except that a square fault was used. These spectra are proportional to spectra of velocity seismograms. Thus, at the lowest frequencies, the spectra increase proportional to f, with the level determined by the moment. At the highest frequencies, the spectra decrease approximately as  $f^{-1}$ , as appropriate for an  $\omega$ -square model (Hanks, 1979). The lowest corner frequency in Figures 3 and 4 is controlled by the fault dimension:  $f_0$ =  $(2T_d)^{-1}$ , where  $T_d$  is fault length/rupture velocity. The spectra have multiple corners and variable behavior above  $f_0$ , with several showing an intermediate slope (between f and  $f^{-1}$ ) before achieving the high-frequency behavior. CorSeismic Energy and Stress-Drop Parameters for a Composite Source Model

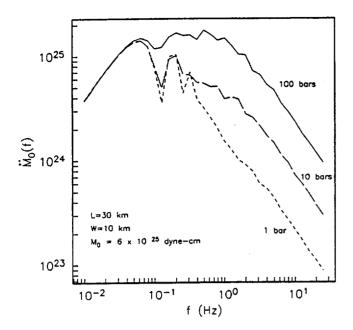


Figure 3. Average Fourier amplitude spectra generated from composite source models for the fault used in Figure 2. Each curve is the average of spectra from 25 realizations. Since energy is proportional to velocity, through equation (6) it is proportional to  $\dot{M}_0(t)$ . Thus, to emphasize the contribution to the energy, these are averages of Fourier spectra of the first derivative of time series such as in Figure 2. The spectra are appropriate in the far field perpendicular to the fault, with no adjustment for, or averaging over, the azimuth from the fault to the station. Individual realizations show little variability at low (<0.05 Hz) or high (>5 Hz) frequencies.

ner frequencies higher than  $f_0$  can be controlled by fault width or rise time. The net result is that as  $\Delta \sigma_d$  increases,  $f_0$ remains constant, but the higher corner frequencies are increased, and the spectra are systematically enriched in highfrequency energy.

### Static Stress Drop

For a composite event, with seismic moment  $M_0$ , the average static stress drop,  $\Delta \sigma_s$ , is determined by the usual formulas (e.g., Kanamori and Anderson, 1975). For a strike slip fault with length L greater than width W, it is

$$\Delta \sigma_s = \frac{2M_0}{\pi W^2 L}.$$
 (3)

For a dip-slip fault with long, narrow proportions, it is

$$\Delta \sigma_s = \frac{4(\lambda + \mu)M_0}{\pi(\lambda + 2\mu)W^2L}.$$
(4)

Equations (3) and (4) assume the fault ruptures the surface. In Equation (4),  $\lambda$  is the Lame constant. For a circular fault with radius R, it is

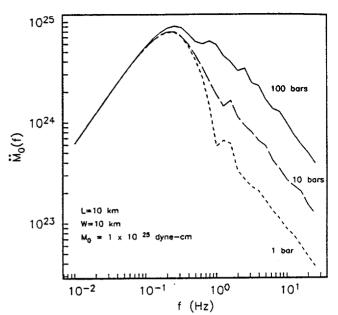


Figure 4. Equivalent of Figure 3, except that the fault has L = 10 km and W = 10 km, and  $M_0 = 1 \times 10^{25}$  dyne-cm. According to equation (5), a circular fault with the same area and moment has  $\Delta \sigma_s = 24$  bars.

$$\Delta \sigma_s = \frac{7M_0}{16R^3}.$$
 (5)

These relations use only the average slip, and thus complexity such as that seen in Figure 1 is not incorporated. Kanamori and Anderson (1975) suggest that a gross global average for  $\Delta \sigma_s$  is about 60 bars. They suggest that  $\Delta \sigma_s$ averages 30 bars for interplate earthquakes and 100 bars for intraplate earthquakes. Considering that the stress drop is proportional to the strain drop, it is evident from Figure 1 that locally on the fault, the composite source model allows for static stress drops that are larger or smaller than average.

In the composite source model, the subevent stress drop  $(\Delta \sigma_d)$  is independent of  $\Delta \sigma_s$ . The three source moment rates in Figure 2, and corresponding average spectra in Figure 3, are constrained to have the same value of  $\Delta \sigma_s$ , 13 bars. When  $\Delta \sigma_d = 100$  bars, then  $\Delta \sigma_d > \Delta \sigma_s$ , and the model is equivalent to the partial stress-drop model (Brune, 1970). As shown by Smith *et al.* (1991), it has a broad intermediate slope. Interpretation of the cases where  $\Delta \sigma_d \leq \Delta \sigma_s$  will be deferred.

### Radiated Energy

The radiated energy is, in general, sensitive to the shape of the spectrum of the radiated waves, particularly near the corner frequency (e.g., Smith *et al.*, 1991). Thus, considering Figures 3 and 4, it is evident that the energy will depend on the subevent stress drop  $\Delta \sigma_d$ . Fortunately, it is possible to estimate the energy that is radiated from a composite source model without deriving an explicit expression for the shape

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of the average spectrum. The derivation begins by determining the energy radiated from a subevent of radius R. The total energy is initially derived by integrating that result over the subevents. This initial approach assumes energy of the subevents is additive because they are randomly located and add incoherently. This point will be investigated further below.

The energy radiated by a point double-couple source may be derived starting with the equations in Aki and Richards (1980) for the far-field displacement  $u(\mathbf{x}, t)$  at location  $\mathbf{x}$  from a point source at the origin in an infinite homogeneous medium:

$$u(\mathbf{x}, t) = \frac{\mathbf{A}^{FP}}{4\pi\rho\alpha^3 r} \dot{M}_0 \left( t - \frac{r}{\alpha} \right) + \frac{\mathbf{A}^{FS}}{4\pi\rho\beta^3 r} \dot{M}_0 \left( t - \frac{r}{\beta} \right) \quad (6)$$

in which r is the source-to-station distance;  $\dot{M}_0(t)$  is the moment rate at the source;  $\rho$  is density;  $\alpha$  and  $\beta$  are the P and S velocities, respectively; and  $A^{FP}$  and  $A^{FS}$  are radiation patterns. Specifically,  $A^{FP} = \sin 2\theta \cos \phi \hat{r}$ , and  $A^{FS} = \cos 2\theta \cos \phi \hat{\theta} - \cos \theta \sin \phi \hat{\phi}$  in which  $\theta$  is the polar angle.

The kinetic energy in an elemental volume is  $1/2\rho \dot{u}^2 dV$ . The kinetic energy radiated into the far field is obtained by integrating this over all space. One may easily choose time late enough that all near-field and intermediate-field terms are zero. To carry out the integral, it is convenient to substitute  $dr = \alpha dt$  or  $dr = \beta dt$  for the P and S waves, respectively. Then, assuming that the potential energy is equal to the kinetic energy, the total radiated energy in the P wave from a point source is, as found by Vassiliou and Kanamori (1982),

$$E_{P} = \frac{I_{M_0}}{15\pi\rho\alpha^5},\tag{7}$$

and the total radiated energy in the S wave from a point source is

$$E_{S} = \frac{I_{M_0}}{10\pi\rho\beta^5} \tag{8}$$

in which

$$I_{M_0} = \int_0^\infty \dot{M}_0^2(t) dt.$$
 (9)

Based on these results, the total energy in the S wave is 23.4 times the energy in the P wave for a point source in a Poisson solid. Thus, for simplicity of expressions, it is sufficient to deal with the S waves alone and adjust the final result upward by 4%.

In their implementation of the composite source model, Zeng *et al.* (1994) assumed, following Brune (1970), that each subevent has the following moment rate:

$$\dot{M}_{\rm os}(t) = (2\pi f_c)^2 M_{\rm os} t e^{-2\pi f_c t} H(t)$$
(10)

in which case

$$I_{M_{os}} = \frac{1}{4} (2\pi f_c)^3 M_{os}^2. \tag{11}$$

It is important to note that both the subevent moment,  $M_{os}$ , and the subevent corner frequency,  $f_c$ , are functions of R. About 90% of the moment has been released at  $t_{90} = 0.619/t_c$ .  $f_c$ , and 99% of the moment has been released at  $t_{99} = 1/f_c$ . We will take  $t_{90}$  as a best estimate and  $t_{99}$  as an upper limit to the rise time of the pulse.

Zeng *et al.* (1994) used the same relationship as Brune (1970, 1971) between the source radius and corner frequency:

$$f_c(R) = \frac{2.34\beta}{2\pi R}.$$
 (12)

In this model, the moment of a subevent is related to R by

$$M_{os}(R) = \frac{16}{7} \Delta \sigma_d R^3 \tag{13}$$

in which  $\Delta \sigma_d$  is the subevent stress drop. Combining equations (8), (11), (12), and (13), the energy radiated in the S wave from a single Brune pulse for a source of radius R is

$$E_{S}^{\text{Brune}}(R) = 0.233 \frac{\Delta\sigma}{\mu} M_{os}(R), \qquad (14)$$

where  $\mu$  is the shear modulus ( $\mu = \rho \beta^2$ ). If all of the subevents add incoherently, the total energy in the S wave is

 $E_{S}^{CS} = \int_{R_{\min}}^{R_{\max}} n(R) E_{S}(R) dR.$ (15)

To evaluate equation (15), using equations (1) and (14), it is also necessary to use the expression from Zeng *et al.* (1994):

$$p = \frac{7M_0}{16\Delta\sigma_d} \frac{3-D}{(R_{\max}^{3-D} - R_{\min}^{3-D})}$$
(16)

in which  $M_0$  is the seismic moment of the mainshock, equaling the sum of the moments of all the subevents. Carrying out the integration and combining and rearranging,

$$E_{S}^{CS} = 0.233 \, \frac{\Delta \sigma_d}{\mu} \, M_0. \tag{17}$$

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This can be adjusted upward by 4% to account for the P-wave energy.

Several numerical experiments have been used to investigate the importance of the assumption underlying equation (15) that the subevents add incoherently. The experiments consist of generating composite source time functions (as in Fig. 2), using equations (7), (8), and (9) to determine the radiated energy and comparing with the prediction in equation (17). The results are expressed as a correction factor ( $C_E$ ), which is defined as

$$C_E = \frac{S \text{-wave energy from equation (8)}}{S \text{-wave energy from equation (17)}}.$$
 (18)

The results are summarized in Figure 5, for several fault models, as a function of normalized subevent stress drop. The normalized subevent stress drop is defined as  $\Delta \sigma_s^{\dagger}$ , where  $\Delta \sigma_s^* = M_0/W^2 L$ . The reason for using  $\Delta \sigma_s^*$  instead of  $\Delta \sigma_s$  from equations (3), (4), or (5) is to remove the ambiguity that arises from different mechanisms (i.e., strikeslip or dip-slip) or from arbitrary decisions on which equation to use when the aspect ratio is close to unity, and to make it possible to interpolate between curves for small aspect ratios. The mechanism does not affect the radiated energy estimates since it is derived using an infinite space model. This normalization is convenient for our usual procedure for generating composite source time functions, which is to define L and W even for nearly circular faults.

The main features of  $C_E$  are that it is larger than 1.0, a function of L/W, and a decreasing function of subevent stress drop. Thus, for small subevent stress drop, interference of subevent radiation is constructive, and equation (15) gives a stochastic lower bound on the radiated energy. For subevent stress drop greater than  $\Delta \sigma_s$ , it is asymptotic to approximately 1.0. For  $\Delta \sigma_d > 2\Delta \sigma_s$ , subevents are incoherent, and equation (17) can be used directly. At small values of  $\Delta \sigma_d$ , the value of  $C_E$  decreases approximately as  $\Delta \sigma_d^{-1}$ . Summarizing, a final estimate of the radiated seismic energy, incorporating subevent coherence, is

$$E_S^{CS} = 0.233 \ C_E \frac{\Delta \sigma_d}{\mu} M_0. \tag{19}$$

It is necessary to consult Figure 5 to obtain the value of  $C_E$  to use in equation (19). As before, this can be adjusted upward by 4% to account for the *P*-wave energy.

The result in equation (19) is quite simple in its form. The seismic energy is linearly proportional to the stress drop of the subevents. The stress drop, in turn, through equations (10), (12), and (13), is inversely related to the rise times ( $\tau$ ) of the subevents ( $\tau \sim \Delta \sigma_d^{-1/3}$ ) and, thus, the average rise time of the overall average displacement of the composite source. Thus, we obtain the expected result (e.g., Vassiliou and Kanamori, 1982) that for a fixed moment, the radiated energy is increased as the rise time decreases ( $E_s \sim \tau^{-3}$ ).

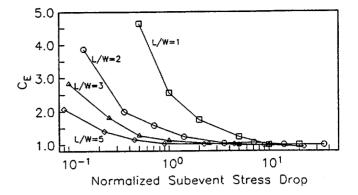


Figure 5. Energy ratio,  $C_E$ , as defined in equation (18). The normalized stress drop is  $\Delta \sigma_d / \Delta \sigma_s^*$ , where  $\Delta \sigma_s^* = M_0 / W^2 L$ , as discussed in the text. All of these computations use  $R_{\text{max}} = L/2$ , but the result is not very sensitive to smaller values.

In the development of the composite source model by Zeng *et al.* (1994) and Yu (1994), and other applications, estimation of the stress drop of the subevents has been unconstrained. Equation (19) suggests a simple method to constrain it, if the energy of the target event is known independently. An alternative approach, developed by Yu *et al.* (1996) for the composite source model used here, is to match an assumed (and empirically calibrated) spectral shape (e.g., Joyner, 1984; Tumarkin *et al.*, 1994).

Some insight is gained by a comparison between the energy radiated by a smooth Brune pulse and by a composite source of the same seismic moment. This can be obtained directly from equations (14) and (19). Setting the moments equal in (14) and (19), one obtains

$$\frac{E_S^{CS}}{E_S^{\text{Brune}}} = \frac{C_E \,\Delta\sigma_d}{\Delta\sigma_{\text{static}}}.$$
(20)

Thus, if the subevents have the same stress drop as the static stress drop of a single smooth mainshock, the energy that is radiated is increased by about 30%. To obtain this ratio, it is also necessary to adjust for the difference between  $\Delta \sigma_s^*$  and  $\Delta \sigma_s$  from equation (5) by finding the radius of the fault with the same area. Figure 4 shows spectra that approximately match this situation. When  $\Delta \sigma_d = 100$  bars and thus  $\Delta \sigma_d > \Delta \sigma_s$ , the spectrum has a relatively broad frequency band with an intermediate slope. Conversely, when  $\Delta \sigma_d = 1$  bar and thus  $\Delta \sigma_d \ll \Delta \sigma_s$ , the spectrum of the composite source falls off significantly faster than  $f^{-1}$  above the corner. However, the effect of subevent coherence is apparent in this case, causing the spectrum to match the spectrum for  $\Delta \sigma_d = 10$  bars to a frequency substantially above the corner frequency.

### Strain Energy

Based on Kanamori and Anderson (1975), the change in strain energy is

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$$\Delta W = \frac{M_0}{\mu} \bar{\sigma}, \qquad (21)$$

and the radiated energy is related to this by

$$E_{I} = \eta \Delta W, \qquad (22)$$

where  $\eta$  is the seismic efficiency. Comparing equations (19), (21), and (22), we find that

$$\eta \bar{\sigma} = \frac{0.243}{0.243} C_E \Delta \sigma_d. \tag{23}$$

Thus, the composite source model yields an estimate of the product of seismic efficiency and average stress but does not help determine either factor by itself.

# Apparent Stress

Wyss (1970) defined the apparent stress of an earthquake as  $\sigma_a = \eta \bar{\sigma} = \mu E_I/M_0$ . Thus, for the composite source, one obtains

$$\sigma_{a} = \frac{0.233}{0.233} C_{E} \Delta \sigma_{d}.$$
(24)

Thus, in the context of the composite source model, the apparent stress is proportional to the subevent stress drop.

### Effective Dynamic Stress

Effective dynamic stress (or effective stress) ( $\sigma_e$ ) is defined as the difference between the initial shear stress at the beginning of faulting and the dynamic frictional stress. Its estimation is based on Brune's (1970) demonstration that the particle velocity at the fault is proportional to this stress parameter. Based on Brune (1970) and subsequent studies [reviewed by Kanamori and Anderson (1975) or Kanamori (1994)],

$$\dot{D} = C_{\mu\nu}\sigma_{\epsilon}\beta/\mu \tag{25}$$

in which  $\dot{D}$  is the rate of sliding of opposite sides of the fault during the earthquake, and  $C_{pv}$  is a constant with a value between about 1 and 2, depending on the model. While recognizing that there is this factor of 2 uncertainty, this article follows Kanamori (1994) in using  $C_{pv} = 1$ .

Measurements of  $\sigma_e$  use equation (25) with inferred particle velocity on the fault (e.g., Kanamori, 1972b; Abe, 1974) or estimate  $\Delta \sigma_d$  from the velocity pulse recorded nearby (e.g., McGarr *et al.*, 1981; Shoja-Taheri and Anderson, 1988). However, these two parameters are not the same. Combining the definition of the moment (equation 13) and the area ( $\pi R^2$ ) to get the average slip, combining this with the best estimate of the rise time ( $t_{90}$  defined above), and using equation (12), one obtains that the Brune pulse has an estimated effective stress of  $\sigma_e = (0.44/C_{pv}) \Delta \sigma_d$ . A rationale could be found for replacing the lead coefficient (0.44) with values between 0.27 (based on the upper limit on rise time) and 1.70 (based on the rise time that would result from the peak moment rate). Still, the mismatch in the best estimate introduces another factor of 2 uncertainty into estimates of  $\sigma_{e}$ .

Beyond this, as with the energy estimate, coherent subevents will combine to give an effective rate of sliding between the opposite sides of the fault that is greater than the rate in an individual subevent. For this reason,  $\sigma_{e}$  for a composite source model is greater than or equal to the effective stress that would characterize the largest subevents if they were isolated. In fact, the composite source model is incapable of describing earthquakes with  $\sigma_e$  significantly smaller than  $\Delta \sigma_s$ . Low values of  $\sigma_s$  should result in a slow earthquake or a tsunami earthquake. However, neither the duration at the source nor the rise time increases (Fig. 2) as  $\Delta \sigma_d$ decreases below  $\Delta \sigma_s$ . This is because the durations of the subevents are fixed by their radius (equations 10 and 12) and are independent of  $\Delta \sigma_d$ . The maximum rise time is thus  $f_c^{-1}(R_{\text{max}})$ . The low slip in each subevent (e.g., equation 13) then becomes compensated with larger numbers of subevents (equation 16) that add coherently. Combining relations,  $\sigma_e/\Delta\sigma_d$  cannot be less than ~1.17 for a strike-slip fault,  $\sim 0.88$  for a dip-slip fault, or  $\sim 0.27$  for a circular fault. Considering this, the relationship

$$\sigma_e = \frac{0.44C_E}{C_{pv}} \Delta \sigma_d \tag{26}$$

is probably a reasonable approximation within all the uncertainties, since  $C_E$  is a measure of the net coherency of the subevents.

It may be possible to develop a modified composite source model without this limitation. One approach to try is to set the number of subevents so that their area is on the same order as the area of the fault being modeled. The subevent stress drop could be set to the effective stress and control the rate of sliding on the fault in the subevents. Equation (10) would have to be replaced with a function that is controlled by the rate of sliding and stops at the right time to match the seismic moment of the mainshock. The distribution of subevents in this approach might resemble the distribution in the composite source model for the normal earthquakes with high values of  $\Delta \sigma_d$ , where it has been proven successful.

### Savage-Wood Inequality

Savage and Wood (1971) presented a model that introduces physics of faulting to develop a relationship between static and effective dynamic stress drops. In this model, if the final stress on the fault is less than or equal to the frictional stress, then  $\sigma_a \leq \Delta \sigma_s/2$ . Considering equation (24), <u>adjusted to include *P*-wave energy</u>, this will be true if  $\Delta \sigma_d$  $\leq 2.06 C_E^{-1} \Delta \sigma_s$ . In this model, equality occurs when the final and frictional stresses are equal. Following Savage and



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Seismic Energy and Stress-Drop Parameters for a Composite Source Model

Wood (1971) and Smith et al. (1991), the Savage-Wood ratio (SWR) is defined as

$$SWR = \frac{2\sigma_a}{\Delta\sigma_s}.$$
 (27)

Smith *et al.* (1991) argue that a partial stress-drop earthquake (e.g., Brune, 1970) with an intermediate slope above the first corner frequency proportional to  $f^{-1}$  gives SWR > 1. In the context of the composite source model, equation (27) gives

$$SWR = \frac{\frac{0.436}{9.47} C_E \Delta \sigma_d}{\Delta \sigma_s}.$$
 (28)

As noted above, these two stress drops are independent parameters input into the composite source model. These considerations suggest that they are linked through the physics of the earthquake-generating process. It is evident that an understanding of the Savage-Wood ratio has direct applications to prediction of strong ground motions.

Savage and Wood (1971) suggested that typically SWR  $\sim 0.3$ , thus implying that the Savage-Wood inequality is valid, but they show a considerable amount of scatter with some earthquakes showing SWR > 1. Kanamori and Anderson (1975) suggested that typically,  $\sigma_a \simeq \Delta \sigma_s/2$ , implying that SWR  $\sim 1$ . Data given by Kanamori (1994) would imply that SWR < 1, but he emphasizes that there are large uncertainties, and thus probably for that data, SWR is not distinguishable from unity. Smith *et al.* (1991) suggest that for several earthquakes with well-determined energy estimates, SWR > 1, meaning that the Savage-Wood inequality is violated. Earthquake models using the composite source model could eventually provide a large set of estimates of SWR that will help to clarify this situation.

Savage-Wood ratios in Figure 3 drop from 5 to ~0.4 as  $\Delta \sigma_d$  decreases from 100 bars to 1 bar. As noted above, the composite source model is not capable of producing a source time function with a long rise time, so significantly smaller values of SWR cannot be synthesized here. The case where  $\Delta \sigma_d = 100$  bars has a broad spectral shape as expected for a case with SWR > 1 (Smith et al., 1991). Equation (28) and Figures 3 and 4 invite a discussion of the case where  $\Delta \sigma_d \ll \Delta \sigma_s$ . Considering Savage and Wood (1971), one interpretation of this is that it corresponds to a source model with "overshoot," in which the inertia of the moving blocks carries the opposite sides to a final equilibrium position with final stress that is less than the dynamic frictional forces. However, in the modified composite source model proposed earlier, the low SWR would be achieved using subevents with a low effective stress and thus a very long rise time. This is a very different mechanism, more akin to tsunami earthquakes or slow earthquakes (e.g., Kanamori, 1972a; Kanamori and Hauksson, 1992; Kanamori and Kikuchi, 1993).

### Orowan Stress Drop

Vassiliou and Kanamori (1982) show that when the final and dynamic frictional stresses are equal, i.e., the Orowan (1960) conditions are met, then the radiated seismic energy is

$$E_{i} = \frac{M_0 \Delta \sigma_0}{2\mu} \tag{29}$$

in which  $\Delta \sigma_0$ , the "Orowan stress drop," is the difference between the initial and final stresses on the fault. Comparing equation (29) with equation (19), we find

$$\Delta \sigma_0 = 0.48 \not \subset_E \Delta \sigma_d \tag{30}$$

in which the coefficient includes *P*-wave radiation. Equation (30) demonstrates that  $\Delta \sigma_0$  is about half of the subevent stress drop that is used in the composite source model and, considering equation (26), that  $\sigma_e \approx \Delta \sigma_0$ , as also noted by Kanamori (1994).

Kanamori (1977) used the result, similar to equation (29), that  $E_{f} = M_0 \Delta \sigma_s / 2\mu$ , together with an average range of  $\Delta \sigma_s$  between 20 and 60 bars, to establish the  $M_W$  magnitude scale. Considering equation (29), it appears that the additional assumption that the static stress drop approximately equals the effective dynamic stress or the Orowan stress drop is embedded in his equations.

# **RMS Stress Drop**

Hanks (1979) recognized that the rms acceleration is proportional to a stress-drop parameter, and McGuire and Hanks (1980) and Hanks and McGuire (1981) demonstrated that this stress-drop parameter ( $\Delta \sigma_{\rm rms}$ ) shows much less variation than the variation typically seen in estimates of static stress drop (equations 2 through 4). This section relates  $\Delta \sigma_{\rm rms}$  to parameters in the composite source model.

It is useful to quickly review the derivation of rms acceleration as a function of the Fourier spectrum. Here, the derivation is for a site in the infinite, homogeneous medium instead of for a site on the free surface, as used by Hanks (1979). Defining the duration of faulting at the source as  $T_d$ , the rms acceleration is

$$a_{\rm rms}^2 = \frac{1}{T_d} \int_0^\infty a^2(t) dt$$
 (31)

in which a(t) is the acceleration time series. By Parseval's theorem, it is easily shown that

$$a_{\rm rms}^2 = f_0 \int_0^\infty |a^2(f)| \, df, \tag{32}$$

where a(f) is the Fourier transform of a(t). Equation (32)

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differs from Hanks (1979), who used the approximation that  $f_0 = T_d^{-1}$ , while I used  $f_0 = (2T_d)^{-1}$ . This is a better approximation for the corner frequencies in Figures 3 and 4, as noted above, and is also consistent with the theoretical corner of one-sided pulses of duration  $T_d$ . The Fourier transform of the far-field S-wave acceleration (from equation 6) with the moment rate given by equation (10) is, as noted by Brune (1970),

$$|a_{s}(f)| = \frac{\mathbf{A}^{FS}}{4\pi\rho\beta^{3}r} \frac{(2\pi f)^{2}M_{os}}{\left(1 + \left(\frac{f}{f_{c}}\right)^{2}\right)}.$$
 (33)

This function is essentially flat for  $f > f_c$ . In reality, there is also an upper limit to the flat part of the spectrum, given the generic label  $f_{max}$  (Hanks, 1982). Changing the lower and upper limits of the integral in equation (32) to  $f_c$  and  $\bar{f}_{max}$ , respectively, substituting equation (33), and integrating, one obtains

$$a_{\rm rms} = \mathbf{A}^{FS} \frac{\pi}{\sqrt{2}} \frac{M_{os} f_c^3}{\beta^3} \frac{1}{\rho r} \left(\frac{f_0}{f_c}\right)^{1/2} \left(\frac{f_{\rm max}}{f_c} - 1\right)^{1/2}.$$
 (34)

Using equations (12) and (13), one finds that

$$\frac{M_{os}f_c^3}{\beta^3} = 0.118\Delta\sigma. \tag{35}$$

If this substitution is made in equation (34), and if  $f_{\text{max}} \gg f_c$ , one obtains

$$a_{\rm rms} = 0.158 \, \frac{\Delta \sigma_{\rm rms}}{\rho r} \left(\frac{f_0}{f_c}\right)^{1/2} \left(\frac{f_{\rm max}}{f_c}\right)^{1/2},$$
 (36)

where  $\mathbf{A}^{FS}$  has been replaced by the rms value used by Hanks  $(\mathbf{A}^{FS} = 0.6)$ . Hanks (1979) assumed a model with total stress drop on a circular fault and thus equated  $f_c$  with  $f_0$ . The ratio of these two frequencies in equation (36) adjusts for the difference in duration of the direct S wave from the actual fault and the circular fault assumption. If these durations (or frequencies) are equal, equation (36) becomes

$$a_{\rm rms} = 0.158 \frac{\Delta \sigma_{\rm rms}}{\rho r} \left(\frac{f_{\rm max}}{f_c}\right)^{1/2}.$$
 (37)

Equation (37) differs from Hanks (1979) only by the leading constant. To obtain his coefficient of 0.445, one multiplies equation (37) by 2 to account for the different relationship between corner frequency and fault duration, multiplies by 2 to account for the free surface, and divides by  $\sqrt{2}$  to account for partitioning of energy between two horizontal components.

As an aside, there should also be a correction for difference in velocity at the surface and at the depth of faulting. pg 8

Day (1996) has shown theoretically that in a layered halfspace with infinite Q, the rms response over a sufficiently broad spectral bandwidth depends only on the average velocity near the surface and is independent of the properties of the intervening layers. Anderson *et al.* (1996) extended this to an attenuating medium in numerical experiments and found that the average Q is a second critical factor. These results apply directly to the rms acceleration, since it depends on a broadband spectral property.

Equations (31) to (37) demonstrate the steps that need to be followed to determine the rms acceleration from the composite source model. The acceleration spectrum of radiation from the composite source is the superposition of numerous spectra, each having the shape of equation (33), but with the moment and corner frequency functions of R. We make the simplifying assumption that these spectra add incoherently, and thus obtain

$$|a^{2}(f)| = \int_{R_{\min}}^{R_{\max}} n(R) \left| \frac{\mathbf{A}^{FS}}{4\pi\rho\beta^{3}r} \frac{(2\pi f)^{2}M_{os}(R)}{1 + \left(\frac{f}{f_{c}(R)}\right)} \right|^{2} dR.$$
(38)

With a change of variables, and the assumption that  $R_{\text{max}} \gg R_{\text{min}}$ , this is transformed to

$$|a^{2}(f)| = 1.165(\mathbf{A}^{FS})^{2} (3 - D) \left(\frac{2.34\beta}{2\pi R_{\max}}\right)^{3-D} \frac{M_{0} \Delta \sigma \beta}{(\mu r)^{2}} f^{D-1} I_{\theta}(f)$$
(39)

in which

$$I_{\theta}(f) = \int_{\theta_{\min}}^{\theta_{\max}} \frac{\tan^{5-D}\theta}{\sec^{2}\theta} \, d\theta.$$
 (40)

The frequency dependence enters through the limits of the integral:

$$\theta_{\min} = \tan^{-1} \left( \frac{2\pi f R_{\min}}{2.34\beta} \right), \qquad (41a)$$

$$\theta_{\max} = \tan^{-1} \left( \frac{2\pi f R_{\max}}{2.34\beta} \right). \tag{41b}$$

The integrand for equation (40) is shown in Figure 6. The rapid monatonic increase of the integrand indicates that the greatest contribution comes from the upper limit of integration. Thus, the result is most sensitive to  $R_{max}$ .

Numerical experiments for a range of  $R_{\min}$  confirm that  $I_{\theta}$  is not sensitive to this parameter for typical values. These same experiments show that  $I_{\theta}$  takes values between about 1.0 and 5.0 for nearly the entire range of f and  $R_{\max}$  encountered in applications of the composite source model. The

Seismic Energy and Stress-Drop Parameters for a Composite Source Model

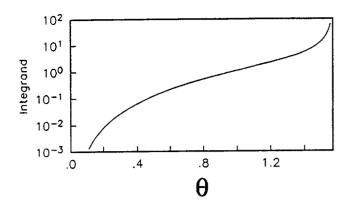


Figure 6. Integrand for  $I_{\theta}$ , as in equation (40).

functional dependence can be roughly approximated as  $\sim f^{0.25}$  in some of these experiments. This dependence makes it impractical to obtain a closed-form expression for  $a_{\rm rms}$  when a(f) is substituted into equation (32). As an approximation, we treat  $I_{\theta}$  as a constant. Then, substituting equation (39) into equation (32), integrating, simplifying, and assuming as before that  $A^{FS} = 0.6$ , leads to the following result:

$$a_{\rm rms} = 0.158 \sqrt{\frac{3-D}{D-1}} I_{\theta}^{1/2} \left(\frac{M_0}{M_{\rm os}(R_{\rm max})}\right)^{1/2} \frac{\Delta \sigma_d}{\rho r} \\ \left[ \left(\frac{f_{\rm max}}{f_c}\right)^{D-1} - 1 \right]^{1/2}. \quad (42)$$

In this approximation,  $I_{\theta}^{1/2}$  takes numerical values between about 1.0 and 2.0, as shown in Figure 7. Choosing an intermediate value, say 1.7, would not be particularly misleading, but one could take an average of the appropriate curve for frequencies  $f \leq f_{max}$ .

In equation (42), the rms acceleration for the composite source model is proportional to the subevent stress drop. The ratio of moments in this equation can be correlated to the total number of subevents. The rms acceleration is thus logically increased as the square root of this ratio since the subevent contributions are incoherent at high frequencies.

When equation (42) is equated with equation (36), we obtain the following relationship between  $\Delta \sigma_{rms}$  and  $\Delta \sigma_{d}$ :

$$\Delta \sigma_{\rm rms} = \Delta \sigma_d \sqrt{\frac{3-D}{D-1}} I_{\theta}^{1/2} \left(\frac{M_0 f_c}{M_{os}(R_{\rm max})f_0}\right)^{1/2} \left(\frac{f_{\rm max}}{f_c}\right)^{(D/2)-1}.$$
(43)

For the typical case where D = 2, this simplifies to

$$\Delta \sigma_{\rm rms} = \Delta \sigma_d I_{\theta}^{1/2} \left( \frac{M_0}{M_{os}(R_{\rm max})} \right)^{1/2} \left( \frac{f_c}{f_0} \right)^{1/2}.$$
(44)

Thus, the rms stress drop will be larger than the subevent

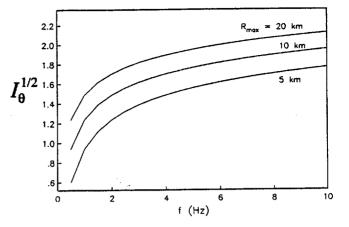


Figure 7. Numerical values of  $I_{\theta}^{1/2}$  for the case where D = 2 and  $R_{\min} = 0.1$  km. The results are shown for three values of  $R_{\max}$ .

stress drop, since all of the multipliers for  $\Delta \sigma_d$  are greater than one.

### Applications

Many of the parameters discussed in this article have been evaluated for the 1985 Michoacan, Mexico, earthquake. Testing the model on these parameters is actually a relatively demanding application since the earthquake was somewhat unusual. Anderson et al. (1986) show that peak accelerations were far below expectations, and the computed energy based on near-field records was much smaller than predicted by regressions. Table 1 presents first the parameters for the composite source model, as developed by Yu (1994), that provide a reasonable fit to statistical properties of accelerograms for the Michoacan earthquake. In developing this model, Yu (1994) used Green's functions for a layered medium to more fully represent the effects of wave propagation on the ground motions. The seismic moment, rupture velocity, and fault dimensions were constrained from other studies, so only the subevent stress drop was a free parameter. The value of  $\Delta \sigma_d = 10$  bars was determined to provide a good match between the statistical properties of the synthetics and the data.

The second part of Table 1 compares predictions from the composite source model with stress and energy parameters for this earthquake derived from earlier studies. The energy based on equation (19) is 10% larger than the energy estimated by Anderson *et al.* (1986) from near-field records. Anderson *et al.* point out that the Gutenberg–Richter energy formula predicts that the energy for this event would be 9  $\times 10^{23}$  ergs, which is a factor of 9 times larger than their estimate. Equation (19) has done a very good job of predicting the energy. The apparent stress estimates based on equation (24) and obtained from the Anderson *et al.* (1986) estimate for the energy are in proportion to the energy estimates.

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Stress and Energy Parameters Michoacan, Mexico, Earthquake, 19 September, 1985 ( $M_W = 8.1$ )

Composite source model				
Seismic moment (dyne-cm)	$1.1 \times 10^{28}$			
Fault dimension (km)	$178 \times 80 \text{ km}$			
Subevent stress drop (bars)	10 bars			
Maximum radius of subevent (km)	20 km			
Rupture velocity (km/sec)	2.8 km/sec			
Fractal dimension D	2.0			
Applications of this article	Predictions from above parameters†	Observations**	Ratio (observation/CSM predictio	n)
$C_{\mathcal{E}}$ (from Fig. 5, validated by independent calculation)	1.3			
Radiated energy (equation 19) (ergs)	$1.1 \times 10^{23}$	$1.0 \times 10^{23}$	0.9	
Static stress drop (equation 4) (bars)	8	19	2.4	
Apparent stress (equation 24) (bars)	senter 3	3.0††	1.0	
Effective dynamic stress (equation 26) (bars)	6	6-12#	1.0-2.0	
Savage-Wood ratio (equation 28)	0.8	0.3‡‡	0.4 5	
rms stress drop (equation 44) (bars)	<del>200</del> Z/O	50325 <sup>‡</sup>	0.2%-1.6	0.24-1.5

\*These parameters are those used by Yu (1994).

\*\*Anderson et al. (1986), except as noted otherwise.

†This uses  $\mu = 3.3 \times 10^{11}$  dyne/cm<sup>2</sup>.

††This estimate is from the definition and the estimates of seismic moment and energy. Anderson et al. (1986) merely state "under 6 bars."

‡Anderson et al. (1986) give this range for effective dynamic stress. The value of 6 bars is internally consistent with parameter choices in this article, as discussed in the text.

‡‡Presented here from the definition (equation 27).

<sup>4</sup>Based on horizontal components of accelerogram from the closest station, Caleta de Campos, which give  $a_{rms}$  or 39 and 45 cm/sec<sup>2</sup>, or an average of 42 cm/sec<sup>2</sup>. These were substituted into equations (36) or (37), except with the Hanks (1979) coefficient of 0.445 since this is a free-surface observation. The factor of 2 associated with the difference in relation between duration and corner frequency was kept, but for the purpose of compensating for the soft material at the surface. Other parameters are  $\rho = 2.8$  gm/cm<sup>3</sup>, r = 24 km,  $f_{max} = 4.5$  Hz. The uncertainties are associated with a range of values of  $f_c$  from 0.025 to 0.5 Hz, as discussed in the text.

Anderson *et al.* (1986) derived the effective dynamic stress very directly from the near-field velocity of a station that recorded a static offset. The estimate of 6 bars is consistent with the decisions in this article on how uncertainties in coefficients are handled, and the same as the prediction using equation (26) using the parameters of Yu's (1994) composite source model also.

The SWR (equation 28) is 0.8 for the parameters of the composite source model used by Yu (1994). In considering this, it may be important to note that Yu used a fault width (80 km) that is greater than the width of the aftershock zone (50 km, Anderson et al., 1986), and when the narrower fault width is used, the estimated static stress drop is increased to 19 bars. A smaller fault might also be compensated by a smaller subevent stress drop. Both of these effects would decrease SWR, and thus it seems that by this method, SWR is smaller than unity for this earthquake. On the other hand, based on a combination of teleseismic and local spectra, Smith et al. (1991) estimated SWR  $\approx$  4 to 8 for the event, about an order of magnitude larger. The discrepancy is part of a larger problem of reconciling local and teleseismic estimates of the seismic energy (e.g., Winslow and Ruff, 1995).

Equation (44) predicts an rms stress drop for the Michoacan earthquake of  $\frac{205}{205}$  bars. The moment of the largest subevent is, from equation (13),  $1 \times 10^{26}$  dyne-cm, so the square root of the moment ratios in equation (44) gives a factor of 7.8. From the accelerograms in Anderson *et al.* (1986), the duration of the strongest shaking is about 20 sec, implying that it is appropriate to use  $f_0 = 0.025$  Hz. For  $R_{\rm max} = 20$  km, equation (12) gives  $f_c = 0.060$  Hz. Thus,  $0.06f_1$ the term in the ratio of corner frequencies contributes a multiplicative factor of 1.6 in equation (44). Finally, using the 1.6 factor of 1.7 for  $I_{\theta}$  leads to the prediction that in this case,  $\Delta \sigma_{\rm rms}$  will be 20 times greater than  $\Delta \sigma_d$ .

Anderson et al. (1986) did not compute the rms acceleration, but horizontal components of accelerograms from one of the stations (Caleta de Campos) give an average of about 42 cm/sec<sup>2</sup>. The range of rms stress drops in Table 1 (50 to 210 bars) is based on this value. There are two problems associated with determining  $\Delta \sigma_{\rm rms}$  from  $a_{\rm rms}$ . The first is with the definition of the lower corner frequency. Hanks (1979) defined  $\Delta \sigma_{\rm rms}$  to explain the level of the flat portion of the acceleration spectrum. For the Michoacan earthquake, the spectrum is approximately flat from 0.5 to 4.5 Hz. The problem is that the lower frequency of this flat part is larger than either  $f_0$  (= 0.025 Hz) or  $f_c(R_{max})$  (= 0.060 Hz). The second problem is that the ratio  $f_0/f_c$  is quite different from unity, but a ratio of 1 is assumed in going from equation (36) to (37). The uncertainty range on observed values of  $\Delta \sigma_{\rm rms}$ , from 50 to 325 bars, was determined using the range of  $f_c$  from 0.025 to 0.5 Hz in equation (37), and the range of  $f_c$  from 0.06 to 0.5 Hz in ratio of  $f_{max}/f_c$  in equation (36). The ratio of the observed value of  $\Delta \sigma_{\rm rms}$ , from equation (36),

1.8

to the predicted value, from equation (44), ranges from 0.55 to 1.6 for  $f_c$  from 0.06 to 0.5 Hz. Considering the approximations made in the derivation of equation (44), this agreement is satisfactory.

Yu (1994) did not discuss, in detail, her choice of model parameters. While by trial and error they do an excellent job of fitting the seismograms, there was no attempt to optimize them in any formal sense. Considering this, the agreement, within uncertainties, of all of the predicted parameters with independent estimates is quite encouraging. Thus, it seems reasonable to suggest that the relationships among the various stress-drop parameters considered here are predicted by the composite source model, using the equations given in this article.

# Discussion

This article introduces the opportunity to evaluate methods that estimate the energy radiated from earthquakes. Methods to estimate this energy tend to make simplifying assumptions that do not fully take into account the complexities of wave propagation, including the mix of body and surface waves and resonances near the surface, and the complexity of the earthquake source. However, for the composite source model, it is possible to determine the amount of energy leaving the source in the form of far-field radiation. The synthetic seismograms, generated with theoretical Green's functions for a layered medium and modified to accommodate random scattering into the seismic coda, incorporate most of the major factors in wave propagation with the notable exception of basin resonances. Therefore, a test of energy equations is possible.

In the context of the composite source model, the roles of static stress drop and subevent stress drop are very clear and independent. The static stress drop is, as usual, proportional to the average slip divided by a characteristic dimension (Kanamori and Anderson, 1975; Brune, 1976). The subevent stress drop is independent of the static stress drop and determines the rise time of the displacement on the fault. In reality, though, they could be linked through the physics of earthquake generation. This article shows that the apparent stress, the effective stress, the Orowan stress drop, and the RMS stress drop are all proportional to the subevent stress drop. The relationships derived in this article have been confirmed, within uncertainties, for the case of the Michoacan, Mexico, earthquake, and application to other earthquakes is underway.

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# **Seismic Energy** and **Stress Drop Parameters** for a Composite **Source Model**

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# Introduction

This paper presents a technique to estimate seismic energy release in earthquakes from strong motion accelerograms. The methods which derive energy from strong motion by integrating the observed velocity seismogram or its spectrum (e.g. Anderson et al, 1986; Shoja-Taheri and Anderson, 1988) inevitably make some simplifying assumptions about the wave propagation whose importance is difficult to assess. This paper takes the alternative approach of computing energy leaving the source (e.g. Haskell, 1964; Vassiliou and Kanamori, 1982).

Yu (1994) and Zeng et al (1994) have proposed a composite source model for generating synthetic strong motion accelerograms. These synthetics utilize synthetic Green's functions generated for a layered medium. Thus many of the complexities of wave propagation are incorporated. Several papers have demonstrated that the synthetics generated with this model are highly realistic, both in appearance in the time domain and in reproducing spectral amplitudes over the entire frequency band (Yu, 1994; Zeng et al, 1994; Yu et al, 1995; Su et al, 1995a,b; Anderson and Yu, 1996; Zeng and Anderson, 1996). Considering this realism, it seems natural to derive an analytical expression for the seismic energy leaving a composite source.

In addition to energy, it is possible to derive analytical expressions for several of the commonly used stress parameters in the context of this model: apparent stress (Wyss, 1970), effective stress (Brune, 1970), Orowan stress drop (Kanamori, 1977; Vassiliou and Kanamori, 1982), and RMS stress drop (Hanks, 1979; Hanks and McGuire, 1981).

# Composite source model

Credits: Zeng et al (1994), Yu (1994)

The composite source model superimposes radiation from a number of point sources on the fault. The point sources have a distribution of "sizes":

$$n(R) = pR^{-D-1}$$

n(R) = the number of sources with equivalent "radius" R

D = a fractal dimension (generally taken to be 2.0)

$$p = \frac{7M_o^T}{16\Delta\sigma_d} \frac{3-D}{(R_{\max}^{3-D} - R_{\min}^{3-D})}$$

 $M_o^T$  = moment of target event

 $\Delta \sigma_d$  = subevent stress drop

Subevent spatial distribution: random, uniform on the fault plane.

Subevent radiates when the rupture front reaches its center.

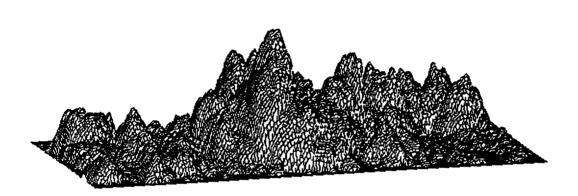
Subevent time function:  $\dot{M}_o(t) = (2\pi f_c)^2 M_o t e^{-2\pi f_c t} H(t)$ 

Rupture starts at epicenter, grows with rupture velocity v.

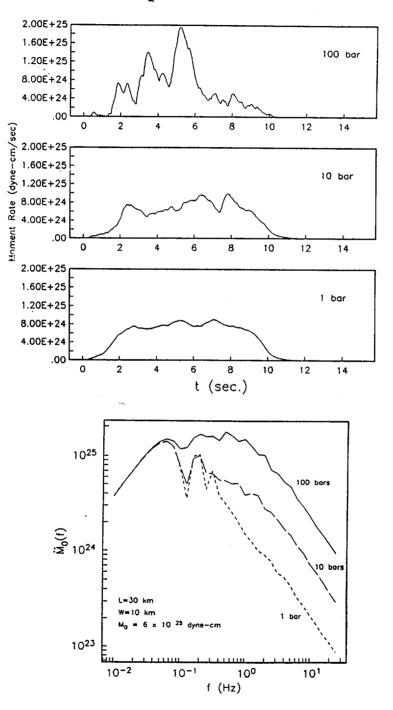
24. A

View of the composite source, assuming  $s(r) = \frac{24}{7\pi} \frac{\Delta \sigma_d}{\mu} (R^2 - a^2)^{1/2}$ 

for each subevent:



The following figures shows realizations of the composite source time function for a rectangular fault (expressed as seismic moment rate) with three values of  $\Delta \sigma_d$ : 1, 10, and 100 bars, and associated Fourier spectra.



John Anderson AGU Poster, December 1996

# Static stress drop, $\Delta \sigma_s$

Usual formulas (e.g. Kanamori and Anderson, 1975).

Strike slip, length L greater than width W, surface rupture:

$$\Delta \sigma_s = \frac{2M_o}{\pi W^2 L}$$

**Dip slip fault,** length L greater than width W, surface rupture:

$$\Delta \sigma_s = \frac{4(\lambda + \mu)M_o}{\pi(\lambda + 2\mu)W^2L}$$

Circular fault, radius R:

$$\Delta \sigma_s = \frac{7M_o}{16R^3}$$

Note: In the composite source model, the subevent stress drop  $(\Delta \sigma_d)$  is independent of  $\Delta \sigma_s$ .

# Radiated energy

Energy radiated to far field from a point source (e.g. Vassiliou and Kanamori, 1982):

$$E_P(R) = \frac{I_{M_o}}{15\pi\rho\alpha^5}$$
$$E_S(R) = \frac{I_{M_o}}{10\pi\rho\beta^5}$$
$$I_{M_o} = \int_0^\infty \dot{M}_o^2(t)dt$$

Note:  $E_s = 23.4 E_p$ 

For a subevent in the composite source model:

$$E_{S}^{Brune}(R) = 0.233 \frac{\Delta \sigma_{d}}{\mu} M_{o}(R)$$

Total energy in a composite source S wave:

$$E_s^{CS} = 0.233 C_E \frac{\Delta \sigma_d}{\mu} M_o^T$$

Adjust upwards by 4% to account for the P wave energy.

Explanation of factor  $C_E$ 

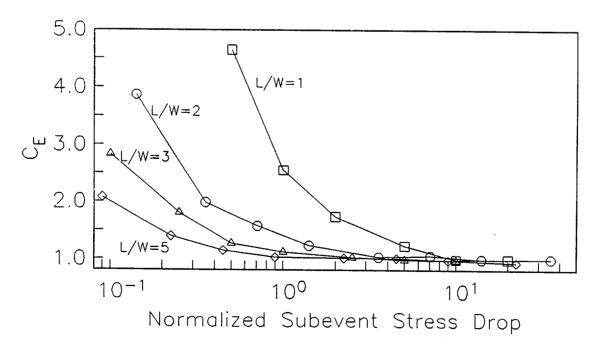
This factor is estimated in numerical experiments, to correct for coherence of the radiation from subevents. When there are few subevents and the radiation is totally incoherent,  $C_E = 1.0$ .

The figure below shows  $C_E = 1.0$  several fault models, as a function of normalized subevent stress drop. The normalized subevent stress drop is defined as

 $\Delta \sigma_d / \Delta \sigma_s^*$ where

$$\Delta \sigma_s^* = \frac{M_o}{W^2 L}.$$

I used  $\Delta \sigma_s^*$  instead of  $\Delta \sigma_s$  to remove the ambiguity that arises from different mechanisms (i.e. strike-slip or dip-slip) or aspect ratios. With the composite source the mechanism does not affect the radiated energy estimates since it is derived using an infinite space model.



# Strain Energy

Change in strain energy (Kanamori and Anderson, 1975):

$$\Delta W = \frac{M_o}{\mu}\overline{\sigma}$$

Radiated energy:

$$E_s = \eta \Delta W$$

where  $\eta$  = seismic efficiency

So:

2

$$\eta \sigma = 0.243 C_E \Delta \sigma_d$$

# Apparent stress $\sigma_a$

Definition (Wyss, 1970):  $\sigma_a = \eta \overline{\sigma} = \mu E_s / M_o$ 

So:

$$\sigma_a = 0.243 C_E \Delta \sigma_d$$

# *Effective Dynamic Stress*, $\sigma_e$

Definition (Brune, 1970): Difference between the initial shear stress at the beginning of faulting and the dynamic frictional stress. From Brune (1970), the particle velocity at the fault,  $\dot{D}$ , is proportional to  $\sigma_e$ .

Kanamori and Anderson (1975), or Kanamori (1994) give:

$$\dot{D} = C_{pv} \sigma_e \beta / \mu$$

 $C_{pv} \sim 1 - 2$ , depending on the model<sup>2</sup>.

For a Brune pulse:  $\sigma_e = \frac{0.44}{C_{pv}} \Delta \sigma_d$ .

This is based on the average slip and the rise time to release 90% of the total seismic moment. The lead coefficient (0.44) is uncertain between 0.27 and 1.70.

For the composite source,

$$\sigma_e = \frac{0.44C_E}{C_{pv}} \Delta \sigma_d$$

is probably a reasonable approximation within all the uncertainties, since  $C_E$  is a measure of the net coherency of the subevents.

<sup>2</sup> While recognizing that there is this factor of two uncertainty, this paper follows Kanamori (1994) in using  $C_{nv} = 1$ .

# **Orowan stress drop**, $\Delta \sigma_o$

Definition: the difference between the initial and final stresses on the fault.

Assuming the final and dynamic frictional stresses are equal, i.e. the Orowan (1960) conditions are met, then the radiated seismic energy is (Vassiliou and Kanamori, 1982):

$$E_s = \frac{M_o \Delta \sigma_o}{2\mu}$$

Composite source model estimation:

$$\Delta \sigma_o = 0.486 C_E \Delta \sigma_d$$

# **RMS Stress Drop**, $\Delta \sigma_{rms}$

Hanks (1979) defines  $\Delta \sigma_{rms}$  from RMS acceleration:

$$a_{rms}^2 = \frac{1}{T_d} \int_0^\infty a^2(t) dt$$

 $T_d$  = duration of faulting at source.

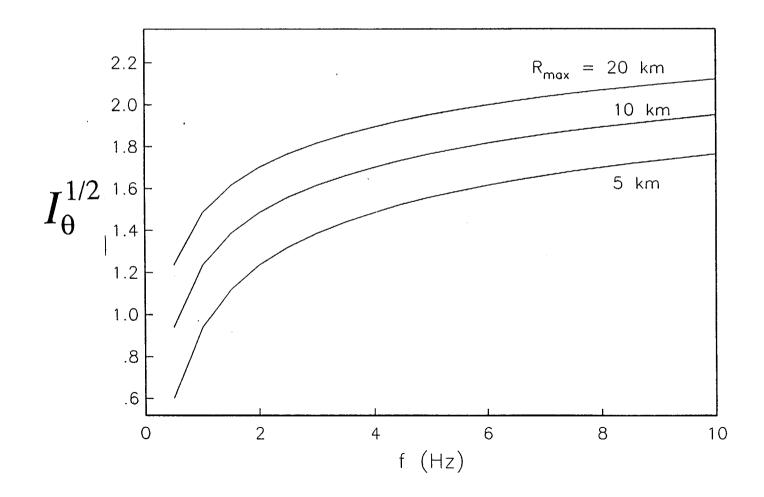
After some work, in an infinite medium:

$$a_{rms} = 0.158 \frac{\Delta \sigma_{rms}}{\rho r} \left(\frac{f_{max}}{f_c}\right)^{1/2}$$

For the composite source model, with some approximations, and taking the typical case where D = 2:

$$\Delta \sigma_{rms} = \Delta \sigma_d I_{\theta}^{1/2} \left( \frac{M_o}{M_{os}(R_{\text{max}})} \right)^{1/2} \left( \frac{f_c}{f_o} \right)^{1/2}$$

The RMS stress drop will be larger than the subevent stress drop, since all of the multipliers for  $\Delta \sigma_d$  are greater than one.



· · ·

# Savage-Wood Inequality, (SWR)

Definition (Savage and Wood, 1971):

$$SWR = \frac{2\sigma_a}{\Delta\sigma_s}$$

Composite source model:

 $SWR = \frac{0.486 \, C_E \, \Delta \sigma_d}{\Delta \sigma_s}$ 

Savage and Wood (1971) model: static and effective dynamic stress drops are linked through the physics of the earthquake generating process.

SWR < 1 --> overshoot

SWR > 1 --> partial stress drop (sense of Brune, 1970)

Observations show considerable scatter:

Savage and Wood (1971):  $SWR \approx 0.3$ considerable scatter (some earthquakes have SWR > 1).

Kanamori and Anderson (1975):  $SWR \approx 1$ .

Smith et al. (1991): *SWR* > 1

# Applications

Yu (1994) developed a composite source model for the 1985 Michoacan, Mexico, earthquake (M8.1). Many of the other parameters discussed in this paper have been estimated independently. Table 1 first describes the composite source model, then compares predictions using these parameters with the independent estimates.

Yu (1994) did not discuss, in detail, her choice of model parameters. While by trial and error they do an excellent job of fitting the seismograms, there was no attempt to optimize them in any formal sense. Considering this, the agreement, within uncertainties, of all of the predicted parameters with independent estimates is quite encouraging.

# Table 1 Composite Source Model Parameters Michoacan, Mexico Earthquake, September 19, 1985 (M<sub>w</sub>=8.1).

Composite Source Model<sup>3</sup>

Seismic Moment (dyne-cm)  $1.1 \times 10^{28}$ 

Fault dimension (km) 178 × 80 km

Subevent stress drop (bars) 10 bars

Maximum radius of subev- 20 km ent (*km*) Rupture velocity (*km/sec*) 2.8 km/sec

Fractal dimension D 2.0

<sup>3</sup> These parameters are those used by Yu (1994).

Table 1 (continued) Stress and Energy Parameters Michoacan, Mexico Earthquake, September 19, 1985 (M <sub>w</sub> =8.1).							
	Predictions from csm parameters <sup>5</sup>	Observed <sup>4</sup>	Ratio (observed / CSM predic- tion)				
$C_E$	1.3						
Radiated Energy (ergs)	$1.1 \times 10^{23}$	$1.0 \times 10^{23}$	0.9				
Static stress drop (bars)	8	19	2.4				
Apparent stress (bars)	3.0	$3.0^{6}$	1.0				
Effective dynamic stress (bars)	6	6-12 <sup>7</sup>	1.0-2.0				
Savage-Wood Ratio	0.8	0.3 <sup>8</sup>	0.4				
RMS stress drop (bars)	200	50-325 <sup>9</sup>	0.25-1.6				

4 Anderson et al. (1986), except as noted otherwise.

7 Anderson et al (1986) give this range for effective dynamic stress. The value of 6 bars is internally consistent with parameter choices in this paper, as discussed in the text.

8 Presented here from the definiton (Equation 27).

9 Based on horizontal components of accelerogram from the closest station, Caleta de Campos, which give  $a_{rms}$  of 39 and 45 cm/sec<sup>2</sup>, or an average of 42 cm/sec<sup>2</sup>. These were substituted into Equations (36) or (37), except with the Hanks (1979) coefficient of 0.445 since this is a free surface observation. The factor of 2 associated with the difference in relation between duration and corner frequency was kept, but for the purpose of compensating for the soft material at the surface. Other parameters are  $\rho = 2.8 \text{ gm/cm}^3$ , r = 24 km,  $f_{max} = 4.5 \text{ Hz}$ . The uncertainties are associated with a range of values of  $f_c$  from 0.025 Hz to 0.5 Hz, as discussed in the text.

**<sup>5</sup>** This uses  $\mu = 3.3 \times 10^{11} dyne/cm^2$ .

<sup>6</sup> This estimate is from the definition and the estimates of seismic moment and energy. Anderson et al (1986) merely state "under 6 bars".

# Summary

In the context of the composite source model, the static stress drop and subevent stress drop are independent. In reality, they could be linked through the physics of earthquake generation. This paper shows that the apparent stress, the effective stress, the Orowan stress drop, and the RMS stress drop are all proportional to the subevent stress drop. From parameters of the composite source model, it is easy to estimate energy and all of these stress parameters.

The results give some insight into the meaning of several stress parameters in the context of a source that is much more complex than the models that are the basis for their original definitions. Even though the composite source is a kinematic model, it is reasonable to expect that characteristics of these relationships will carry over to future models that more thoroughly incorporate the physics of complex faulting.

In the development of the composite source model by Zeng et al (1994) and Yu (1994), and other applications, estimation of the stress drop of the subevents has been unconstrained. These results suggest a simple method to constrain it, if the energy, or any of the related stress parameters, of the target event is known independently.

# **Earthquake Size as a Function of Fault Slip Rate**

# John G. Anderson<sup>1</sup>

This presentation is based on the following publication:

John G. Anderson, Steven G. Wesnousky<sup>2</sup>, and Mark W. Stirling<sup>3</sup> (1996). Earthquake Size as a Function of Fault Slip Rate, Bulletin of the Seismological Society of America 86, 683-690.

Presentation to Seismic Source Characterization Workshop on Hazard Methodologies October 16-18, 1996 Doubletree Hotel Salt Lake City, Utah

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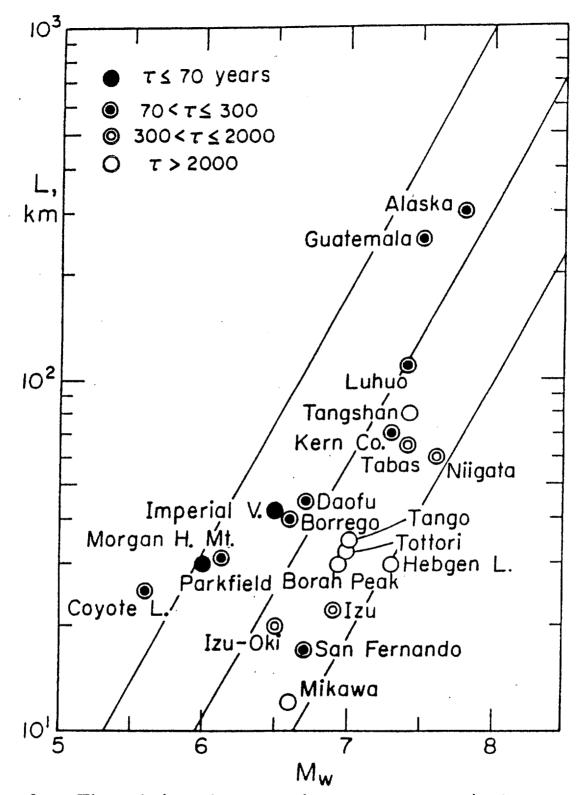


Fig. 2. The relations between the moment magnitude,  $M_W$ , and the fault length, L. The solid lines indicate the trend for a constant stress drop.

Kanamori and Allen, 1986

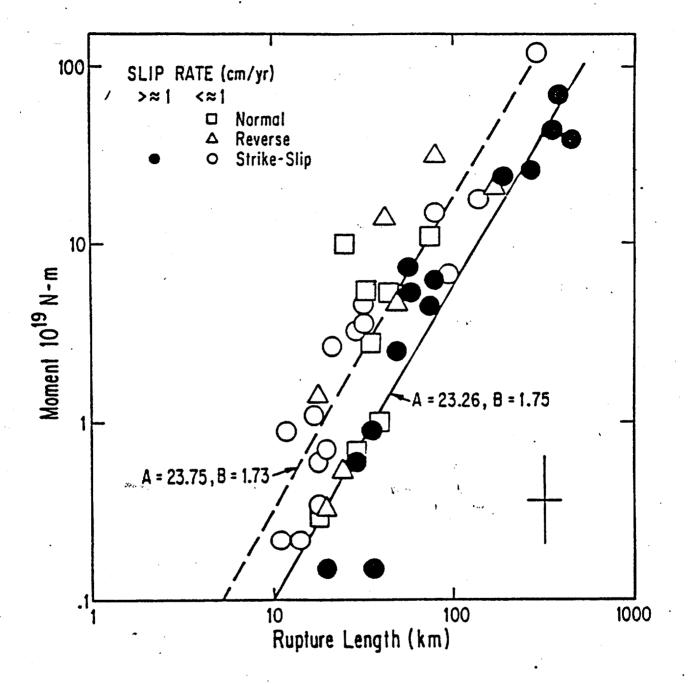


Fig 14.

Earthquake rupture length versus earthquake moment, this figure distinguishes faults with slip rates above and below 1 cm/yr, and indicates the sense of displacement for the data points (from Wesnouski, 1986)

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Table 1					
Historical	Earthquake Data				

ło.	Year	Location	M <sub>0</sub> (× 10 <sup>26</sup> dyne-cm)	M.,	Refs*	Length (km)	Refs*	Slip Rate (mm/yr)	Refs*
1	1811	New Madrid, Missouri		8.2 <sup>f</sup>	86	60-250*	93, 70	0.01-2 <sup>/.m</sup>	70, 93
2	1848	Marlborough, New Zealand	-	7.ŀ	88	95*	83	.4-10 <sup>r</sup>	5, 105
6	1857	Fort Tejon, California	53-87"	7.7–7.9 <b>*</b>	1	360-400 <sup>s</sup>	1, 16	16-43 <sup>1</sup>	12
	1868	California California	1.56ª	6.8°	78	48 <sup>s</sup> -52'	78, 108	8-10 <sup>1.4</sup>	4
;	1872	Owens Valley, California	1844ª	7.4 <b>-</b> 7.7*	92	108 <sup>s</sup>	92	1-3'	92
	1888	Canterbury, New Zealand	-	7.0–7.3 <sup>f</sup>	94	25-35*	87, 94	11–25'	18, 19, 87
	1891	Nobi, Japan	- 15ª	7.4 <sup>e</sup>	37	80 <sup>s</sup>	39	1-104	21
	1896	Rikuu, Japan	144.6	7.4 <sup>e</sup>	39	36-50 <sup>h,i</sup>	38, 39	$0.1 - 1^{i}$	21
I	1906	San Francisco, California	35-43ª	7.6–7.7*	1	420–470 <sup>s</sup>	1, 62	15-28'	23, 24, 25, 26
)	1915	Pleasant Valley, Nevada	3-8"	6.9 <b>-</b> 7.2*	17, 78	348	17	0.3-1'	27, 28
	1927	Tango, Japan	4.6°	<b>7</b> .1 <sup>e</sup>	40	33 <sup>h,i</sup>	40	0.01-1'	21
		- · ·	4.0 2.7 <sup>a.b</sup>	6.9°	42	22 <sup>s,i</sup>	36, 42	1-10'	21, 29
	1930	N. Izu, Japan Long Reach	0.41 <sup>c,d</sup>	0.9 6.4 <sup>e</sup>	42 78	23 <sup>h</sup>	78	0.1-6'	12
	1933	Long Beach, California Parkfield,	0.41 <sup>-1</sup>	6.1 <sup>e</sup>	6	20 <sup>1</sup>	7	29-39 <sup>4</sup>	61
	1934 1939	California Erzincan,	45ª	7.7 <sup>e</sup>	59	350 <b>s</b>	30	5 <sup>1</sup> -25"	31, 84, 107
	1939	Turkey Imperial Valley,	2.7 <sup>c.d</sup>	6.9 <sup>e</sup>	78	60 <sup>s</sup>	8, 9	18-23'	32
	1940	California Erbaa Niksar,	2.7 2.5ª	6.9 <sup>e</sup>	59	50 <b>*</b>	30	5'-25"	31, 84, 107
	1942	Turkey Gerede-Bolu,	2.5 24ª	7.6°	59	190 <sup>g</sup>	30	5'-25"	31, 84, 107
,	1952	Turkey Kern County,	11 <sup>a</sup>	7.3 <sup>e</sup>	10	75'	10	38.5'	10
)	1953	California Golen-Yenice,	7.3ª	7.2*	59	58 <sup>8</sup>	30	5'-25"	31, 84, 107
	1954	Turkey Fairview Peak,	6.4 <sup>c.d</sup>	7.2*	78	4664 <sup>*</sup>	64	0.01–1 <sup>1</sup>	103
ļ	1954	Nevada Dixie Valley,	2.9 <sup>c.d</sup>	6.9 <sup>e</sup>	78	46 <sup>*</sup>	64	0.3–1'	27, 28
	1954	Nevada San Miguel,	1.0 <sup>c.d</sup>	6.6 <sup>e</sup>	78	22 <sup>h</sup>	78	0.1-0.5'	33
	1959	Mexico Hebgen Lake,	10.3	7.3°	58	26 <sup>s</sup>	20	0.8-2.5'	34
		Montana	32 <sup>d</sup>	7.6 <sup>e</sup>	48	80 <sup>*</sup>	48	0.01-1'	21
i	1964	Niigata, Japan				378	3	2939 <sup>1</sup>	6, 61
	1966	Parkfield, California	0.15 <sup>d</sup>	6.1°	2		3 30	2959 5'-25"	31, 84, 107
	1967	Mudurnu Valley, Turkey	8.8°	7.3°	96	80 <sup>s</sup>			
	1968	Borrego Mtn, California	1.2°	6.7°	11	30-45 <sup>s.h</sup>	13, 14	1.4-5 <sup>1</sup>	12, 106
)	1971	San Fernando, California	1.0 <sup>c.d</sup>	6.6 <sup>e</sup>	78	16 <sup>s</sup> -17 <sup>h</sup>	78	2-7.5'	35, 41 43
)	1973	Luhuo, China	19°	7.5°	72	89 <sup>8</sup> -110 <sup>h</sup>	78	5-10 <sup>4</sup>	
	1979	Coyote Lake, California	0.051 <sup>c.d</sup>	5.8 <sup>e</sup>	78	14 <sup>k.j</sup>	95, 73	15-194	44
2	1979	Imperial Valley, California	0.6 <sup>d</sup>	6.5°	52	30.5*	15	18-23'	32
5	1981	Daofu, China	1.3 <sup>c</sup>	6.7 <sup>e</sup>	75	46 <sup>h</sup>	75	5-10 <sup>1</sup>	43

(continued)

		Location	$M_0$ (× 10 <sup>26</sup> dyne-cm)	М.,	Refs*	Length (km)	Refs*	Slip Rate (mm/yr)	Refs*
10.  34	Year 1983	Coalinga,	0.54 <sup>d</sup>	6.5ª	60	25 <sup>#</sup>	46	1-7"	45, 91
35	1983	California Borah Peak,	2.1 <sup>c</sup> -3.5 <sup>d</sup>	6.8-7.0 <sup>e</sup>	56, 57	30 <b>*39.5</b> *	90, 74	0.070.3'	34
36	1984	Idaho Morgan Hill,	0.2 <sup>c.d</sup>	6.2 <b>*</b>	78	30 <sup>4</sup>	67	3-6.4'	47, 49
37	1986	California N. Palm Springs,	0.16 <sup>c,d</sup>	6.1ª	78	9 <sup>s</sup> -16 <sup>h</sup>	78	14-25'	50
38	1 <b>987</b>	California Edgecumbe,	0.63 <sup>c,d</sup>	6.5 <b>°</b>	78	18 <sup>s</sup> -32 <sup>k</sup>	78	1.3-2.8'	51
39	1987	New Zealand Superstition	1.1°	6.7 <sup>e</sup>	68	278	69	2-6'	12
40	198 <b>9</b>	Hills, California Loma Prieta,	3.0°	7.0ª	76	34 <sup>i</sup>	77	12–28 <sup>1.0</sup>	53, 24, 91
<b>‡</b> 1	1990	California Luzon,	39 <sup>e</sup>	7.7°	65	110 <sup>s</sup> -120 <sup>h</sup>	66	10-20'	104
12	1992	Philippines Landers,	6-11.5 <sup>c.d</sup>	7.1-7.3 <sup>e</sup>	97–101	70 <sup>s.h</sup>	71, 82	0.08-2'	12, 54
43	1994	California Northridge, California	0.76–2.6 <sup>c.d</sup>	6.5–6.9 <b>*</b>	22, 63, 79, 85, 89, 102	8-16 <sup>h.i.k</sup>	80, 81, 22	1.4-1.7'	55

#### Table 1 (Continued) Historical Earthquake Data

Explanation of Data

The superscripts beside each of the estimates of  $M_o$ ,  $M_w$ ,  $L_s$  and slip rate represent the following:

 $M_{o}$  estimated from (a) geological observations, (b) intensity data, (c) body waves, and (d) surface waves.  $M_{w}$  estimated from (e)  $M_{o}$ , using the equation log  $M_{o} = 16.1 + 1.5M$  (Hanks and Kanamori, 1979). If a range of  $M_{o}$  is given, then the equivalent range

of M<sub>w</sub> is shown; (f) intensity data. Length estimated from (g) geological observations, (h) aftershock distribution, (i) geodetic data, (j) broadband data, and (k) borehole-dilatational strain-

meter data. Slip rate estimated from (1) geological observations; (m) the equation  $U^{g} = \dot{M}_{b}^{g}/\mu LW$ , in which  $U^{g}$  is the slip rate,  $\dot{M}_{b}^{g}$  is the seismic moment rate [New Madrid  $M_0^{\alpha}$  is calculated by estimating the  $M_0$  of the 1811 event from log  $M_0 = 16.1 + 1.5M$  (Hanks and Kanamori, 1979), and then dividing  $M_0$  by return times estimated from paleoliquefaction studies],  $\mu$  is the rigidity modulus, and L and W are the fault length and width; (n) geodetic data; and (o) slip partitioning studies.

\*The references for the data sources are as follows:

1. Sieh (1978). 2. Tsai and Aki (1969). 3. Brown and Vedder (1967). 4. Lienkaemper et al. (1991). 5. Knuepfer (1992). 6. Bakun and McEvilly (1984). 7. Wilson (1936). 8. Brune and Allen (1967). 9. Trifunac (1972). 10. Stein and Thatcher (1981). 11. Petersen et al. (1991). 12. Petersen and Wesnousky (1994), 13. Clark (1972). 14. Hamilton (1972). 15. Sharp et al. (1982). 16. Hanks and Kanamori (1979). 17. Page (1935). 18. Van Dissen and Yeats (1991). Cowan and McGlone (1991). 20. Witkind (1964). 21. Research Group for Active Faults of Japan (1992). 22. Hudnut et al. (1994). 23. Prentice (1989). 24. Sims (1991). 25. Niemi and Hall (1992). 26. Clahan et al. (1994). 27. Wallace and Whitney (1984). 28. Bell and Katzer (1990). 29. Okada and Ikeda (1991). 30. Ambraseys (1970). 31. Straub and Kahle (1994). 32. Thomas and Rockwell (1996). 33. Hirabayashi et al. (1995). 34. Doser (1985a). 35. Sharp (1981). 36. Matsuda (1974). 37. Mikumo and Ando (1976). 38. Matsuda et al. (1980). 39. Thatcher et al. (1980). 40. Kanamori (1973). 42. Abe (1978). 43. Teng et al. (1983). 44. Savage et al. (1979). 45. Trumm et al. (1986). 46. Urhammer et al. (1983). 47. Galehouse (1991). 48. Abe (1975). 49. Bird and Kong (1994). 50. Hardin and Matti (1989). 51. Nairn and Beanland (1989). 52. Kanamori and Regan (1982). 53. Weber and Anderson (1990). 54. Jennings (1975). 55. Yeats and Huftile (1995). 56. Doser and Smith (1985). 57. Tanimoto and Kanamori (1986). 58. Doser (1985b). 59. Sykes and Quittmeyer (1981). 60. Kanamori (1983). 61. Sieh and Jahns (1984). 62. Thatcher (1975). 63. Thio and Kanamori (1994a). 64. Caskey et al. (1995). 65. Romanowicz (1992). 66. Yoshida and Abe (1992). 67. Bakun et al. (1984). 68. Bent et al. (1989). 69. Sharp et al. (1989). 70. Nuttli (1983). 71. Ad Hoc Working Group on the Probabilities of Future Large Earthquakes in Southern California (1992). 72. Zhou et al. (1983b). 73. Reasenberg and Ellsworth (1982). 74. Crone et al. (1987). 75. Zhou et al. (1983a). 76. Hanks and Krawinkler (1991). 77. Marshall et al. (1991). 78. Wells and Coppersmith (1994). 79. Zhao (1994). 80. Dreger et al. (1994). 81. Johnston and Linde (1994). 82. Sieh et al. (1993). 83. Lensen (1978). 84. Oral et al. (1995). 85. Wald and Heaton (1994b). 86. Johnston and Kanter (1990). 87. Cowan (1990). 88. Eiby (1973). 89. Thio and Kanamori (1994b). 90. Kanamori and Allen (1986). 91. Jones and Wesnousky (1992). 92. Beanland and Clark (1995). 93. Wesnousky and Leffler (1992). 94. Cowan (1991). 95. Bouchon (1982). 96. Hanks and Wyss (1972). 97. Freymueller (1994). 98. Johnson et al. (1994). 99. Wald and Heaton (1994a). 100. Cohee and Beroza (1994). 101. Dreger (1994). 102. Song et al. (1994). 103. J. Caskey, personal comm. 104. T. Nakata, personal comm. 105. Berryman (1979). 106. Gurrolo and Rockwell (1996). 107. Barka and Gulen (1988). 108. Yu and Segall (1995).

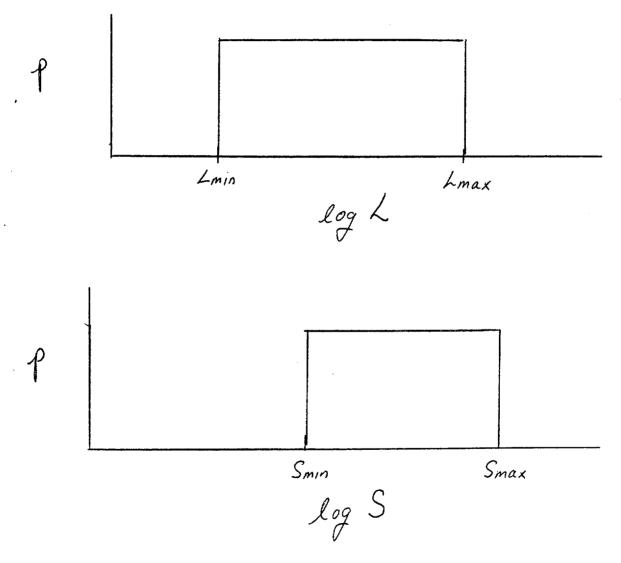
Proposed Regression Equation

# $M_W = A + B \log L + C \log S$

Monte Carlo Method

## 10,000 Runs

 $M_{W}$ , L, S choosen at random within their bounds



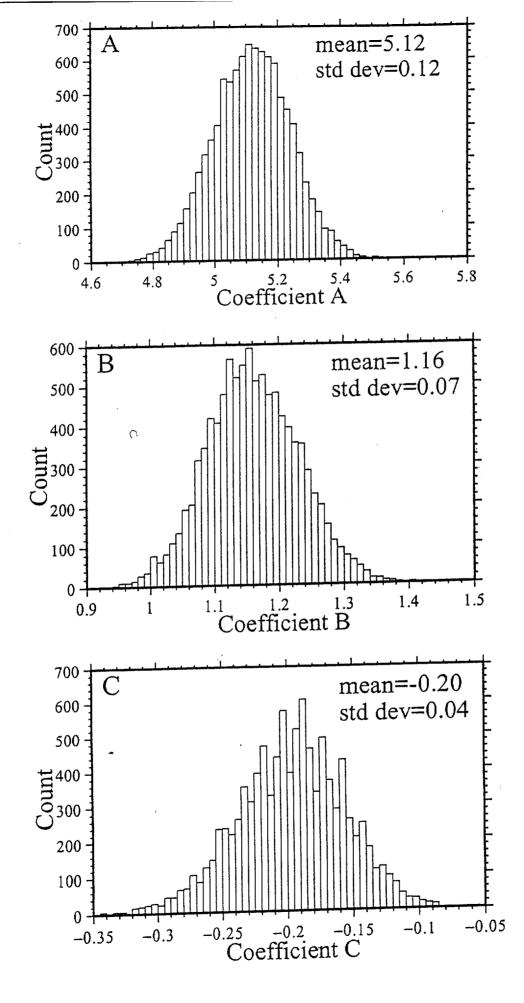
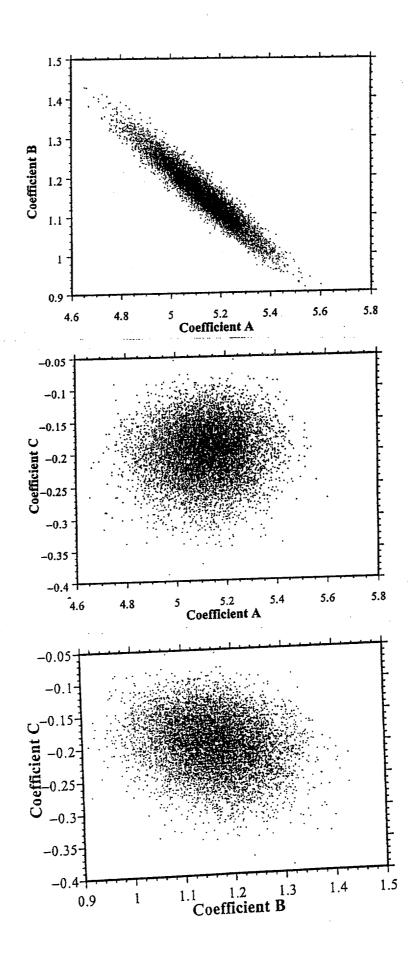
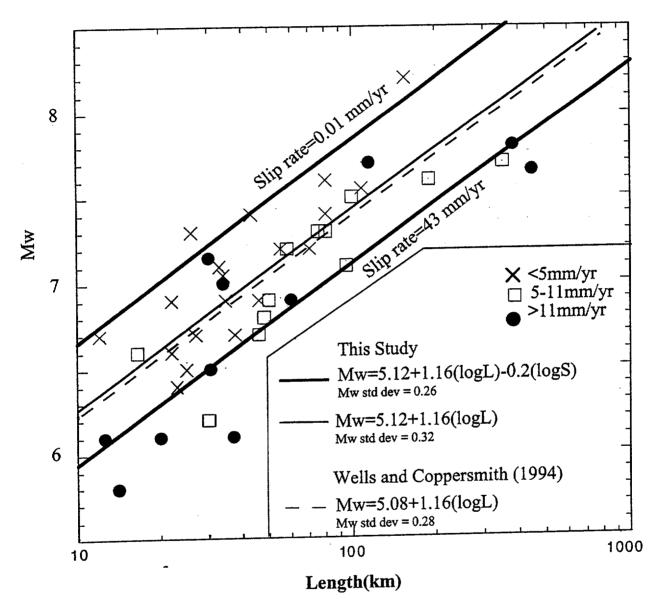


Fig 2





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Variance Reduction

L2 Norm (Standard Deviation)

$$\boldsymbol{\sigma} = \left\{ \frac{1}{N} \sum_{i=1}^{N} (M_i - \hat{M}_i)^2 \right\}^{1/2}$$

Excluding slip rate:

Including slip rate:

 $\sigma = 0.26$ 

 $\sigma = 0.32$ 

This variance reduction is significant with 75% confidence.

L1 norm: variance reduction is significant with 95% confidence.

C is never closer to zero than -0.05, indicating less than one chance in  $10^4$  of finding a set of parameters, within the specified ranges of the data, for which the coefficient on slip rate is zero.

Seismic moment

$$M_o = \mu L W D$$

Moment magnitude

$$M_W = 2/3(\log M_o - 16)$$

Combining relations:

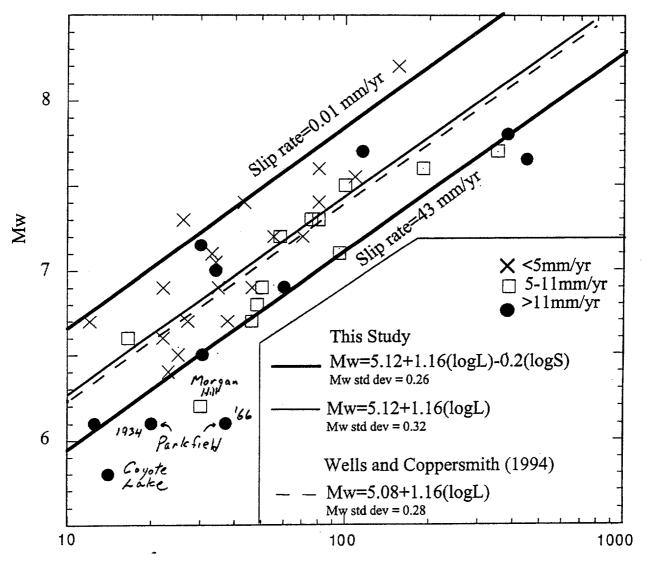
 $M_W = 2/3 \log L + 2/3 \log D + 2/3 (\log \mu + \log W - 16)$ 

For our data, W has a narrow range so the last term is nearly constant.

If  $D \propto W$ , B should be 0.67. (W model) If  $D \propto L$ , B should be 1.33. (L model)

In our regression,  $B = 1.16 \pm 0.07$ . This is closer to the L model, but it differs from the L model prediction by over twice its standard deviation.

**ALL EVENTS** 



Length(km)

MLS Table	for Normal Faults								
		Range		Range		Used		Pred.	
			М	L	S	L	S	Magnitude	Residual
	Pleasant Valley, Neva		7.05		.3-1	34	0.6	6.95	0.10
	Fairview Peak	7.2		46-64	.01-1	55	0.1	7.36	-0.16
	Dixie Valley	6.9	6.9	46	.3-1	46	0.6	7.10	-0.20
	Hebgen Lake	7.3	7.3	26	.8-2.5	26	1.4	6.73	0.57
	Borah Peak	6.8-7.0	6.9	30-39.5	.073	35	0.14	7.10	-0.20
38	Edgecumbe, NZ	6.5	6.5	18-32	1.3-2.8	25	1.9	6.68	-0.18
							Average R	esidual	-0.01
							Standard d	eviation	0.31
MLS for ext	ensional environments								
	Owens Valley	7.4-7.7	7.55	108	3-Jan	108	2	7.41	0.14
10	Pleasant Valley, Neva	6.9-7.2	7.05	34	.3-1	34	0.6	6.95	
	Imperial Valley 1940	6.9	6.9	60	18-23	60	21.5	6.89	0.01
21	Fairview Peak	7.2	7.2	46-64	.01-1	55	0.1	7.36	-0.16
22	Dixie Valley	6.9	6.9	46	.3-1	46	0.6	7.10	-0.20
	Hebgen Lake	7.3	7.3	26	.8-2.5	26	1.4	6.73	0.57
	Imperial Valley 1979	6.5	6.5	30.5	18-23	30.5	21.5	6.55	
35	Borah Peak	6.8-7.0	6.9	30-39.5	.073	35	0.14	7.10	
38	Edgecumbe, NZ	6.5	6.5	18-32	1.3-2.8	25	1.9	6.68	
							Average R	esidual	0.00
							Standard d		0.25

# Conclusions

The distribution of coefficient C shows that a regression that does not include slip rate as a parameter will systematically overestimate the expected magnitudes on the fastest slipping faults, and will systematically underestimate the expected magnitudes on the slowest slipping faults.

Faults with slower slip rates tend to fail in earthquakes with higher static stress drop.

# Earthquake Size as a Function of Fault Slip Rate

by John G. Anderson, Steven G. Wesnousky, and Mark W. Stirling

Abstract Estimates of the potential size of earthquakes on mapped active faults are generally based on regressions of earthquake magnitude  $(M_w)$  versus length (L)of fault rupture for historical earthquakes. The fault slip rate (S) has been ignored in formal prediction equations, but more accurate predictions of future earthquake magnitudes on mapped faults may be obtained when it is included. A least-squares regression for a data set of 43 earthquakes occurring on faults for which slip rates are reported shows  $M_w = 5.12 + 1.16 \log L - 0.20 \log S$ , where L is in units of Km and S is in units of mm/yr. The result indicates that the largest earthquakes will occur on the slowest slipping faults if the rupture length is held constant.

#### Introduction

The estimate of earthquake size on mapped faults is fundamental to seismic hazard analysis. As a result, there is a long history of efforts to use historical data to develop regressions between earthquake size (magnitude or seismic moment) and earthquake rupture length, area, or fault displacement. A thorough review of past efforts, a synthesis of new observations, and the development of new regressions has recently been put forth by Wells and Coppersmith (1994). The slip rate of the fault on which an earthquake occurs has been generally ignored in such regressions when applied to seismic hazard analysis, except by Wesnousky (1986) who sorted the faults into high and low slip rate categories. However, within the community of seismologists concerned with the mechanics of faulting, it has been previously established that there also exists a dependency of earthquake size on earthquake return time and the tectonic environment in which earthquakes occur (e.g., Kanamori and Allen, 1986; Scholz et al., 1986). Here, we use observations from 43 earthquakes that occurred on faults for which slip rates are reported and develop a regression for moment magnitude  $(M_w;$  Hanks and Kanamori, 1979) as a function of surface rupture length (L) and fault slip rate (S). Our result shows that the inclusion of fault slip rate in such regressions reduces the misfit between predicted and observed values of  $M_{w}$  as compared with regressions based solely on L and, hence, can yield more accurate predictions of future earthquake magnitudes on active faults.

#### Data and Analysis

We start with a list of 43 historical earthquakes for which there exist estimates of the moment magnitude  $M_w$ , the fault rupture length L, and the slip rate S of the respective fault on which the earthquake occurred (Table 1). The data are the result of a global search of observations, limited to earthquakes that occur in regions where the seismogenic depth is 15 to 20 km. The distribution of the data is shown in Figure 1.

The regression we develop has the form

$$M_w = A + B \log L + C \log S, \tag{1}$$

where A, B, and C are constants to be determined by the regression. We avoid assuming a preferred slip rate or rupture length for each fault in our study by using a Monte Carlo approach. Values of S for each fault were chosen at random, assuming the probability density of log S is constant between the minimum and maximum estimates. Likewise, in setting up each regression, we chose L at random, assuming the probability density of  $\log L$  is constant between its minimum and maximum values or between a range of  $\pm 20\%$  of the rupture length if minimum and maximum values are absent in Table 1. This range is the average of rupture length ranges shown in Table 1.  $M_w$  is similarly chosen at random between the minimum and maximum values, or between the range of  $M_{w} - 0.3$  and  $M_{w} + 0.3$  if the minimum and maximum values are absent in Table 1. The width of the interval on the magnitude  $(\pm 0.3)$  is chosen to represent an uncertainty on the moment of plus or minus a factor of 3, which we believe to be conservative in most cases.

We generated 10,000 Monte Carlo realizations consistent with the above ranges of data, and for each we used a standard least-squares technique (e.g., Menke, 1989) to find A, B, and C. The distribution of values for A, B, and C is shown in Figure 2. There is almost no correlation between B and C in the Monte Carlo simulations (Fig. 3), indicating that the rupture length and slip rate act independently. The mean values and standard deviations of these distributions may be taken for regression coefficients:

$$M_w = (5.12 \pm 0.12) + (1.16 \pm 0.07)\log L - (0.20 \pm 0.04)\log S.$$
(2)

)

Table 1
Historical Earthquake Data

No.	Year	Location	$M_0$ (×10 <sup>26</sup> dyne-cm)	M <sub>w</sub>	Refs*	Length (km)	Refs*	Slip Rate (mm/yr)	Refs*
1	1811	New Madrid,		8.2 <sup>f</sup>	86	60-250*	93, 70	0.01-2 <sup>1,m</sup>	70, 93
2	1848	Missouri Marlborough, New Zealand	_	7.1 <sup>f</sup>	88	95 <sup>8</sup>	83	4-10'	5, 105
3	1857	Fort Tejon, California	53-87ª	7.7 <b>-</b> 7.9 <sup>e</sup>	1	360-400 <sup>s</sup>	1, 16	16–43 <sup>7</sup>	12
4	1868	California California	1.56 <sup>a</sup>	6.8°	78	48 <sup>g</sup> 52 <sup>i</sup>	78, 108	8–10 <sup>1.n</sup>	4
5	1872	Owens Valley, California	18–44ª	7.4–7.7 <sup>e</sup>	92	108 <sup>8</sup>	92	1-3'	92
6	1888	Canterbury, New Zealand	<u> </u>	7.0–7.3 <sup>f</sup>	94	25–35 <sup>8</sup>	87, 94	11-25'	18, 19, 87
7	1891	Nobi, Japan	$-15^{a}$	7.4 <sup>e</sup>	37	80 <sup>s</sup>	20	1.10/	
8	1896	Rikuu, Japan	14 <sup>a,b</sup>	7.4 <sup>e</sup>	39		39 28 20	1-10'	21
9 9	1906	San Francisco,	35-43ª	7.4- 7.6–7.7 <sup>e</sup>		36-50 <sup>4,1</sup>	38, 39	0.1-1'	21
0		California			1	420–470 <sup>s</sup>	1, 62	15–28'	23, 24, 25, 26
	1915	Pleasant Valley, Nevada	3-8ª	6. <del>9</del> –7.2 <sup>e</sup>	17, 78	348	17	0.3–1′	27, 28
1	1927	Tango, Japan	4.6 <sup>a</sup>	7.1 <sup>e</sup>	40	33 <sup>h,i</sup>	40	0.01-11	21
2	1930	N. Izu, Japan	2.7 <sup>a,b</sup>	6.9°	42	22 <sup>8,i</sup>	36, 42	1-10'	21, 29
3	1933	Long Beach, California	0.41 <sup>c.d</sup>	6.4 <sup>e</sup>	78	23 <sup><i>h</i></sup>	78	0.1–6 <sup>1</sup>	12
4	1934	Parkfield, California	0.15 <sup>d</sup>	6.1 <sup>e</sup>	6	20 <sup>h</sup>	7	29–39 <sup>4</sup>	61
5	1939	Erzincan, Turkey	45ª	7.7 <sup>e</sup>	59	350 <sup>g</sup>	30	5 <sup>1</sup> -25 <sup>n</sup>	31, 84, 107
5	1940	Imperial Valley, California	2.7 <sup>c,d</sup>	6.9 <sup>e</sup>	78	60 <sup>s</sup>	8, 9	18–23 <sup>1</sup>	32
7	1942	Erbaa Niksar, Turkey	2.5 <sup>a</sup>	6.9 <sup>e</sup>	59	50 <sup>8</sup>	30	5'-25 <sup>n</sup>	31, 84, 107
8	1944	Gerede-Bolu, Turkey	24 <sup><i>a</i></sup>	7.6 <sup>e</sup>	59	190 <sup>s</sup>	30	5 <sup>1</sup> -25 <sup>n</sup>	31, 84, 107
7	1952	Kern County, California	11 <sup>a</sup>	7.3 <sup>e</sup>	10	7 <u>5</u> '	10	3-8.5'	10
)	1 <b>95</b> 3	Golen-Yenice, Turkey	7.3ª	7.2 <sup>e</sup>	59	58 <sup>8</sup>	30	5 <sup>1</sup> -25 <sup>n</sup>	31, 84, 107
1	1954	Fairview Peak, Nevada	6.4 <sup><i>c</i>,<i>d</i></sup>	7.2 <sup>e</sup>	78	4664 <sup>8</sup>	64	0.01-11	103
2	1954	Dixie Valley, Nevada	2.9 <sup>c,d</sup>	6.9°	78	46 <sup>8</sup>	64	0.3–11	27, 28
3	1956	San Miguel, Mexico	1.0 <sup>c,d</sup>	6.6 <sup>e</sup>	78	22 <sup>h</sup>	78	0.1-0.5'	33
4	1959	Hebgen Lake, Montana	10.3°	7.3 <sup>e</sup>	58	26 <sup>8</sup>	20	0.8–2.5 <sup>1</sup>	34
5	1964	Niigata, Japan	32 <sup>d</sup>	7.6 <sup>e</sup>	48	80 <sup>4</sup>	40	0.01.1	
5	1966	Parkfield, California	$0.15^{d}$	6.1°	48 2	80° 378	48 . 3 .	0.01–1 <sup>7</sup> 29–39 <sup>7</sup>	21 6, 61
1	1967	Mudurnu Valley,	8.8 <sup>c</sup>	7.3 <sup>e</sup>	96	80 <sup>g</sup>	30	5 <sup>1</sup> -25 <sup>n</sup>	31, 84, 107
1	1968	Turkey Borrego Mtn, California	1.2 <sup>c</sup>	6.7 <sup>e</sup>	11	30-45 <sup>8.h</sup>	13, 14	1.4–5′	12, 106
)	1971	San Fernando,	1.0 <sup>c.d</sup>	6.6 <sup>e</sup>	78	16 <sup>s</sup> -17 <sup>h</sup>	78	2-7.5'	35, 41
)	1072	California	100		-	·			
•	1973	Luhuo, China	19°	7.5 <sup>e</sup>	72	89 <sup>8</sup> -110 <sup>4</sup>	78	5-10'	43
	1979	Coyote Lake, California	0.051 <sup>c.d</sup>	5.8°	78	14 <sup>k.j</sup>	95, 73	15–19 <sup>1</sup>	44
	1979	Imperial Valley, California	$0.6^{d}$	6.5°	52	30.5 <sup>8</sup>	15	18–23 <sup><i>i</i></sup>	32
	1981	Daofu, China	1.3 <sup>c</sup>	6.7 <sup>e</sup>	75	46 <sup>h</sup>	75	5-10'	

(continued)

No.	Year	Location	M <sub>0</sub> (×10 <sup>26</sup> dyne-cm)	M <sub>w</sub>	Refs*	Length (km)	Refs*	Slip Rate (mm/yr)	Refs*
4	1983	Coalinga, California	0.54 <sup>d</sup>	6.5 <sup>a</sup>	60	25 <sup>h</sup>	46	1-7°	45, 91
5	1983	Borah Peak, Idaho	$2.1^{c}-3.5^{d}$	6.8–7.0 <sup>e</sup>	56, 57	30 <sup>h</sup> -39.5 <sup>g</sup>	90, 74	0.070.3	34
6	1984	Morgan Hill, California	0.2 <sup>c,d</sup>	6.2°	78	30 <sup>4</sup>	67	36.4	47, 49
37	1986	N. Palm Springs, California	0.16 <sup>c,d</sup>	6.1°	78	9 <sup>8</sup> –16 <sup>h</sup>	78	14–25 <sup>′</sup>	50
8	1987	Edgecumbe, New Zealand	0.63 <sup>c,d</sup>	6.5 <sup>e</sup>	78	18 <sup>s</sup> 32 <sup>k</sup>	78	1.3–2.8'	51
9	1987	Superstition Hills, California	1.1 <sup>c</sup>	6.7 <sup>e</sup>	68.	27 <sup>8</sup>	69	2–6 <sup>1</sup>	12
0	1989	Loma Prieta, California	3.0 <sup>c</sup>	7.0 <sup>e</sup>	76	34 <sup>i</sup>	77	12-28 <sup>1,0</sup>	53, 24, 91
1	1990	Luzon, Philippines	39 <sup>c</sup>	7.7 <sup>e</sup>	65	110 <sup>s</sup> 120 <sup>h</sup>	66	1020 <sup>4</sup>	104
2	1992	Landers, California	6-11.5 <sup>c,d</sup>	7.1–7.3 <sup>e</sup>	97–101	70 <sup>s,h</sup>	71, 82	0.08–2'	12, 54
3	1994	Northridge, California	0.76–2.6 <sup>c.d</sup>	6.5–6.9° `	22, 63, 79, 85, 89, 102	816 <sup>h,i,k</sup>	80, 81, 22	1.4–1.7′	55

#### Table 1 (Continued) Historical Earthquake Data

Explanation of Data

The superscripts beside each of the estimates of  $M_0$ ,  $M_w$ , L, and slip rate represent the following:

 $M_{o}$  estimated from (a) geological observations, (b) intensity data, (c) body waves, and (d) surface waves.

 $M_{\rm w}$  estimated from (e)  $M_{\rm o}$ , using the equation log  $M_{\rm o} = 16.1 + 1.5M$  (Hanks and Kanamori, 1979). If a range of  $M_{\rm o}$  is given, then the equivalent range of  $M_{\rm w}$  is shown; (f) intensity data.

Length estimated from (g) geological observations, (h) aftershock distribution, (i) geodetic data, (j) broadband data, and (k) borehole-dilatational strainmeter data.

Slip rate estimated from (1) geological observations; (m) the equation  $U^8 = \dot{M}_0^8/\mu LW$ , in which  $U^8$  is the slip rate,  $\dot{M}_0^8$  is the seismic moment rate [New Madrid  $\dot{M}_0^8$  is calculated by estimating the  $M_0$  of the 1811 event from log  $M_0 = 16.1 + 1.5M$  (Hanks and Kanamori, 1979), and then dividing  $M_0$  by return times estimated from paleoliquefaction studies],  $\mu$  is the rigidity modulus, and L and W are the fault length and width; (n) geodetic data; and (o) slip partitioning studies.

\*The references for the data sources are as follows:

1. Sieh (1978). 2. Tsai and Aki (1969). 3. Brown and Vedder (1967). 4. Lienkaemper et al. (1991). 5. Knuepfer (1992). 6. Bakun and McEvilly (1984). 7. Wilson (1936). 8. Brune and Allen (1967). 9. Trifunac (1972). 10. Stein and Thatcher (1981). 11. Petersen et al. (1991). 12. Petersen and Wesnousky (1994), 13. Clark (1972). 14. Hamilton (1972). 15. Sharp et al. (1982). 16. Hanks and Kanamori (1979). 17. Page (1935). 18. Van Dissen and Yeats (1991). Cowan and McGlone (1991). 20. Witkind (1964). 21. Research Group for Active Faults of Japan (1992). 22. Hudnut et al. (1994). 23. Prentice (1989). 24. Sims (1991). 25. Niemi and Hall (1992). 26. Clahan et al. (1994). 27. Wallace and Whitney (1984). 28. Bell and Katzer (1990). 29. Okada and Ikeda (1991). 30. Ambraseys (1970). 31. Straub and Kahle (1994). 32. Thomas and Rockwell (1996). 33. Hirabayashi et al. (1995). 34. Doser (1985a). 35. Sharp (1981). 36. Matsuda (1974). 37. Mikumo and Ando (1976). 38. Matsuda et al. (1980). 39. Thatcher et al. (1980). 40. Kanamori (1973). 42. Abe (1978). 43. Teng et al. (1983). 44. Savage et al. (1979). 45. Trumm et al. (1986). 46. Urhammer et al. (1983). 47. Galehouse (1991). 48. Abe (1975). 49. Bird and Kong (1994). 50. Hardin and Matti (1989). 51. Nairn and Beanland (1989). 52. Kanamori and Regan (1982). 53. Weber and Anderson (1990). 54. Jennings (1975). 55. Yeats and Huftile (1995). 56. Doser and Smith (1985). 57. Tanimoto and Kanamori (1986). 58. Doser (1985b). 59. Sykes and Quittmeyer (1981). 60. Kanamori (1983). 61. Sieh and Jahns (1984). 62. Thatcher (1975). 63. Thio and Kanamori (1994a). 64. Caskey et al. (1995). 65. Romanowicz (1992). 66. Yoshida and Abe (1992). 67. Bakun et al. (1984). 68. Bent et al. (1989). 69. Sharp et al. (1989). 70. Nuttli (1983). 71. Ad Hoc Working Group on the Probabilities of Future Large Earthquakes in Southern California (1992). 72. Zhou et al. (1983b). 73. Reasenberg and Ellsworth (1982). 74. Crone et al. (1987). 75. Zhou et al. (1983a). 76. Hanks and Krawinkler (1991). 77. Marshall et al. (1991). 78. Wells and Coppersmith (1994). 79. Zhao (1994). 80. Dreger et al. (1994). 81. Johnston and Linde (1994). 82. Sieh et al. (1993). 83. Lensen (1978). 84. Oral et al. (1995). 85. Wald and Heaton (1994b). 86. Johnston and Kanter (1990). 87. Cowan (1990). 88. Eiby (1973). 89. Thio and Kanamori (1994b). 90. Kanamori and Allen (1986). 91. Jones and Wesnousky (1992). 92. Beanland and Clark (1995). 93. Wesnousky and Leffler (1992). 94. Cowan (1991). 95. Bouchon (1982). 96. Hanks and Wyss (1972). 97. Freymueller (1994). 98. Johnson et al. (1994). 99. Wald and Heaton (1994a). 100. Cohee and Beroza (1994). 101. Dreger (1994). 102. Song et al. (1994). 103. J. Caskey, personal comm. 104. T. Nakata, personal comm. 105. Berryman (1979). 106. Gurrolo and Rockwell (1996). 107. Barka and Gulen (1988). 108. Yu and Segall (1995).

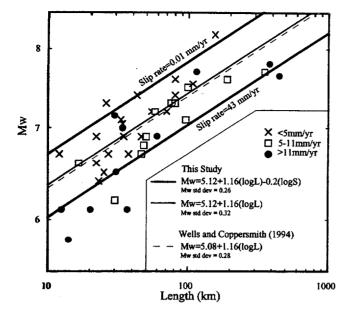


Figure 1. Relationship between magnitude, rupture length, and slip rate. Data are shown as points (mean values of length and  $M_w$ ), with different symbols depending on the range of fault slip rate. The heavy lines are from equation (2), which includes slip rate, and are shown for slip rates of 0.01 mm/yr and 43 mm/yr, as labeled on the graph. The light solid line is the prediction from equation (3) in which slip rate is not included as a parameter. The dashed line shows regression results of Wells and Coppersmith (1994) for magnitude as a function of surface rupture length.

**Predicted** magnitudes using equation (2) are shown in Figure 1. For comparison, we also determined the regression relationship between only magnitude and fault rupture length to equal

$$M_{w} = (5.12 \pm 0.12) + (1.16 \pm 0.07)\log L$$
 (3)

Equation (3) is shown by the thin line on Figure 1.

The sample standard deviation is defined by

$$\sigma = \left\{\frac{1}{N}\sum (M_i - \hat{M}_i)^2\right\}^{1/2},$$

where  $M_i$  is the observation and  $\hat{M}_i$  is the predicted magnitude, and the sum is over all observations. For equation (2), we found  $\sigma = 0.26$  magnitude units. For the predictions of equation (3),  $\sigma = 0.32$  magnitude units. Although the *F*-test (e.g., Mason *et al.*, 1989) indicates that this error reduction is significant at only 75% confidence, equation (2) is better than equation (3) with 95% confidence when an L1 norm (e.g., Menke, 1989) is used to measure the misfit. More importantly, the coefficient, *C*, on slip rate, in distribution on Figure 2, is never closer to zero than -0.05, indicating much less than I chance in 10,000 of finding a set of parameters, within the specified ranges, for which the coefficient on slip rate is zero. That is to say, the distribution on coefficient *C* 

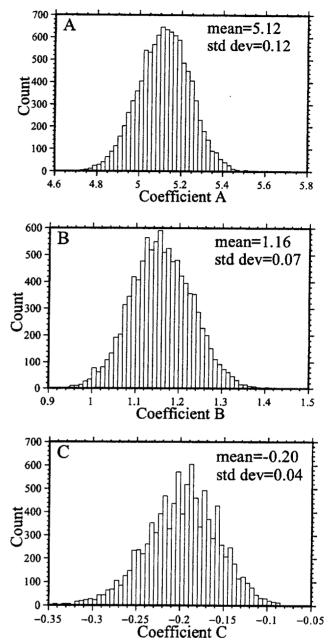


Figure 2. Distribution of coefficients A, B, and C (equation 1) in 10,000 runs in which the slip rate and rupture length on each fault and  $M_w$  are chosen at random from a uniform distribution within a range of allowed values, as discussed in the text. Specifically, log S and log L are given uniform distributions between their minimum and maximum values.

shows that a regression that does not include slip rate as a parameter will systematically overestimate the expected magnitude of earthquakes on the fastest slipping faults and, conversely, will systematically underestimate the expected magnitude of earthquakes on the slowest slipping faults. It is on these bases that we assert that inclusion of slip rate leads to meaningful improvement in the fit to the data.

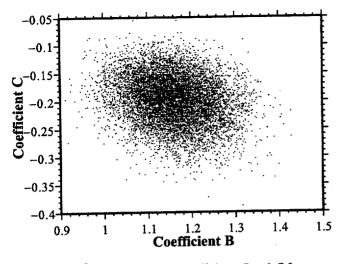


Figure 3. Scatter plot of coefficients B and C for 10,000 individual runs in the Monte Carlo calculations.

#### Discussion

Because we have considered only faults for which slip rate estimates exist, our data set is much smaller than used in the recent summary and regression analyses of Wells and Coppersmith (1994). Nonetheless, Figure 1 shows that equation (3) is virtually identical to the Wells and Coppersmith regression. It thus appears that our data are not obviously biased in any significant manner relative to the data used by Wells and Coppersmith.

For any given fault length, the curve for the slowest slip rate in Table 1 (S = 0.01 mm/yr) yields estimates of magnitude about 0.7 magnitude units greater than the curve for the fastest slip rate in Table 1 (S = 43 mm/yr curve), a difference twice the standard deviation of the curve fit. The regression of  $M_w$  on L that ignores slip rate (equation 3) would agree with the regression in equation (2) for S = 1mm/yr. The comparison of curves illustrates that simple regressions of  $M_w$  on L that ignore fault slip rate appear to underestimate the magnitude of earthquakes on the relatively slow slipping faults. That is to say, information useful to making accurate estimates of future earthquake size is being ignored when fault slip rate is not considered in estimating potential earthquake size on active faults.

It is also useful to briefly consider our results in the context of the definition of seismic moment. The seismic moment is defined as  $M_0 = \mu LWD$ , in which L is fault length, W is fault width, D is average slip, and  $\mu$  is the shear modulus, which is about  $3 \times 10^{11}$  dyne/cm<sup>2</sup>. The relationship between seismic moment and magnitude is  $M_w = (2/3) (\log M_0 - 16)$ , where  $M_0$  is in units of dyne-cm (Hanks and Kanamori, 1979). Combining the two relationships yields

$$M_{w} = \frac{2}{3} \log L + \frac{2}{3} \log D + \frac{2}{3} (\log \mu + \log W - 16).$$

We may consider W approximately constant because our data set is limited to earthquakes with moderate to high dip and in regions where the seismogenic depth is limited to the upper 15 to 20 km. Thus,  $M_w$  will be primarily dependent on L and D. If  $D \propto W$  (the W model), B should equal 2/3. If  $D \propto L$  (the L model), as suggested by Scholz (1982) and approximately confirmed by the data set of Wells and Coppersmith (1994), then  $M_w = 4/3 \log L + \text{const.}$  The value we obtain for B (equation 2) is between these two values. If only faults with L > 30 km are included in the regression to assure that L is greater than the fault width, the coefficient B is 1.18, which is about the same as the result with the full data set. Thus, B is much closer to the prediction of the L model than it is to the prediction of the W model, but it is significantly different from either one.

The reduction of magnitude with a higher slip rate is consistent with a physical model in which, as the time from the last earthquake increases, geological processes strengthen the fault (Kanamori and Allen, 1986; Scholz et al., 1986). Stated another way, a fault with a slow slip rate tends to have earthquakes with a greater static stress drop and greater average slip than a fault with a faster slip rate. The compilation of Wells and Coppersmith (1994) suggested that dip-slip faults tend to have a larger average slip per event (magnitude held constant) than strike-slip faults. To test this, the data were divided into faults with strike-slip mechanisms and faults with dip-slip mechanisms. The regression on strike-slip data gave similar coefficients to those in equation (2). The dip-slip data cover only a small range of slip rates, and consequently, the coefficient on slip rate is smaller. Nonetheless, the regression on dip-slip faults alone predicts similar magnitudes as equation (2) for the slip rates spanned by the data. Hence, fault mechanism does not appear to be as important a factor as the slip rate on the fault on which the earthquake occurs when trying to estimate the earthquake size or stress drop as a function of fault length.

In the context of the physical model, it is interesting to consider some of the events that are conspicuously below the prediction curves in Figure 1. Four events with L < 50 km fall between 0.2 and 0.5 magnitude units below the curve for 43 mm/yr. All are from central or northern California: 1934 Parkfield; 1966 Parkfield; 1984 Morgan Hill; 1979 Coyote Lake. An interesting feature of all of these events is that they occurred adjacent to creeping sections of the San Andreas system. Considering that fault strength is probably significantly below average on the creeping sections, it is plausible that strength for all of these segments is somewhat lower than average, contributing to the anomalies.

It is plausible that amplitudes of dynamic strong ground motions correlate with static stress drop. If so, our observations predict that strong ground motion amplitudes are inversely related to fault slip rate. Recently, Boore *et al.* (1995) observed that reverse faults have larger ground motions than strike-slip faults. The result is probably consistent with our result because most of the reverse faults in their data set are characterized by low slip rate. In other words, it is reasonable that fault slip rate has more influence on dynamic strong ground motion than does fault mechanism and that estimation techniques for the dynamic ground motions from earthquakes might be improved by incorporating slip rate.

#### Conclusions

We conclude that a regression for moment magnitude  $(M_w)$  as a function of surface rupture length (L) and fault slip rate (S) reduces the uncertainty in estimating the potential size of future earthquakes on mapped faults as compared to the standard regressions of  $M_w$  on L that are commonly used in seismic hazard analysis. The results of the regression indicate that faults with slower slip rates tend to fail in earthquakes with higher static stress drop.

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# **Expected Shape of Regressions for Ground Motion Parameters on Rock**

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## Introduction

This note discusses the expected shape of regressions for ground motion parameters on rock as a function of magnitude and distance. Most current regressions use an assumed magnitude and distance dependence that is dominantly ad hoc. Figure 1 illustrates two extremes. The regression by Boore et al (1993) assumes the distance dependence is independent of magnitude, while the regression by Idriss (1991) assumes the distance dependence varies with magnitude. The problem arises because of the scarcity of records from large earthquakes at short distances that are needed to difinitively resolve the problem. This paper compares predictions using synthetic seismograms to the models in Figure 1. It uses both empirical and theoretical Green's functions.

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This examination of the physical processes that are present at ideal rock sites gives an unambiguous answer to the question of whether the distance dependence of attenuation curves should be affected by the magnitude.

#### Method 1. A simple approach using synthetic Green's functions

Figure 2 illustrates the geometry used in a simple approach which illustrates the processes that are involved. For each of 4 sites, I generated synthetic Green's functions from a linear array of eleven sources. Figure 3 shows the transverse component of the synthetic contributions from the eleven points along the fault (Fig 2) for each of the four stations. Each contribution is convolved with a synthetic source time function, derived from the composite source model of Zeng et al (1994), appropriate for a square source with 5 km on a side, and thus has about a two second duration. Figure 3 also shows the effect of adding these contributions with proper time delays to allow for rupture propagation at 2.5 km/sec.

At the short distances (5 and 25 km), the synthetic Green's functions in Figure 3 have a short duration, consisting essentially of a single spike. However, at larger distances, the complexity of the crustal model becomes more important, causing the synthetics to have multiple impulses spread out over increasingly long durations. At 5 km and 25 km distances, because the Green's functions are brief, the separate sources on the fault cause motions at separated times, and there is little constructive interference. Consequently, the sum of the subevents has a peak amplitude that is about the same as the largest of the subevents. However at 50 km and 100 km distances, because of the multiple arrivals, energy from adjacent parts of the fault arrives simultaneously at the station. The first phases from a part of the fault that ruptures later arrive at the same time as

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the later phases from a part of the fault that ruptures earler, and there is the opportunity for constructive interference. The peak acceleration on the sum of the subevents is 14% larger than the largest subevent at 50 km, and 48% larger than the largest subevent at 100 km in this example. This constructive interference can be regarded as random, so that the increase in the amplitudes is related to the square root of the number of contributing Green's functions. Another way to describe the effect is that the multiple arrivals at large distances allow the distant station to "see" more of the fault rupturing at any one time. The net effect, shown in Figure 3, is that the peak amplitude of the sum of several subevent contributions decreases less rapidly with distance than the peak amplitude from any one of the subevents.

#### **Method 2: Empirical Green's Functions**

The tendencies observed in Figure 3 are repeated in a simple example of summation of empirical Green's functions. I selected empirical Green's functions from an earthquake in Mexico recorded on the Guerrero accelerograph network (Anderson et al, 1995). An earthquake on May 2, 1989 was recorded at 13 stations with epicentral distances from 17 to 220 km (Anderson et al, 1991). According to Humphrey and Anderson (1994), this event has seismic moment  $M_o = 8.9 \times 10^{23}$  dyne-cm (M<sub>w</sub>=5.3) and a source radius of 1.4 km. To generate a larger event, the accelerograms were assumed to represent empirical Green's functions for a line of eleven sources with the geometry in Figure 2. Seismograms were delayed according to the assumed rupture velocity and distance from the source to the station.

Figure 4 illustrates results using the seismograms from stations at 17, 33, 68, and 220 km distance. It shows some of the individual contributions, and the total sum which is taken to represent a synthetic seismogram for a larger earthquake with a nearest fault distance equal to the

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distance of the station from the original event. Subevent amplitudes from source locations larger than the original event distance could be adjusted before summing, but this was not done. Figure 4 shows that the ratios of pga for the composite seismogram to the contributing empirical Green's functions tends to increase with distance, although the percentage increase is scattered because of characteristics of the input data. For the 16 km station, because of the relatively short duration of the strongest part of the shaking from the small event, the synthetic main event has an amplitude that is only 18% larger than the empirical Green's function. At the station 33 km from the May 2 event, the peak acceleration on the synthetic seismogram is 50% larger than on the empirical Green's function, and at the station at 68 km, it is 97% larger. The station at 220 km does not continue the trend, as the sum is only 62% larger than the contributing traces. Considering other records, though, it seems that the 68 km record is more of the anomaly, perhaps because its seismogram has a longer duration due to a site effect, or perhaps because by chance several phases happened to interfere constructively. Considering these and the results of the same experiment using other seismograms recorded from the May 2 event, it is evident that even though the trend is more scattered in the presence of real data, the tendency persists for the peak acceleration of synthetic seismograms generated from these empirical Green's functions to decrease less rapidly than the peak values from the small event.

The anomaly at 68 km (Ocotito) calls attention to the point that at any distance, there will be some stations with local site effects that tend to increase the duration of that seismogram. When that occurs, regardless of distance, the ratio of the peak amplitudes of synthetics of large earthquakes to the amplitude of the empirical Green's function will be enhanced, compared to behavior at ideal rock sites.

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#### **Example 3: Complete synthetic seismograms**

The previous examples have been selected to illustrate the physical principles affecting the distance dependence of attenuation curves for large and small earthquakes. However, it is also appropriate to illustrate the results using full synthetic seismograms. For this, I used the composite source model approach (Zeng et al, 1994; Yu, 1994) to generate a profile of synthetics from four seismic sources. Figure 5 illustrates the extent of assumed faulting and the station locations for this example. The fault in this case is a thrust fault with a dip of about 60°. The assumed events have moment magnitudes of 5.0, 6.0, 7.0, and 7.5. Figure 6 shows representative profiles of synthetic accelerations, and Figure 7 shows the corresponding peak values.

In this synthetic model, the peak accelerations decrease more rapidly for the small earthquake than for the large earthquake. For instance, on the sets of traces on the lower half of these figures, the peak motions for the M=5 earthquake at site S025 are barely visible, on the scale of motions at site S010, while for the M=7.5 event they have about 50% the amplitude of the nearer site. Put another way, the attenuation of peak values for the synthetics between sites S010 and S025 for the M=5 earthquake is about the same as the attenuation between sites S010 and S100 for the M=7.5 earthquake.

#### Discussion

The results shown above give a clear indication of what should be expected from empirical regressions. The attenuation of ground motions on rock should have a shape that depends on the fault dimension. Earthquakes on large faults should have an attenuation function that decreases less rapidly with distance than earthquakes on small faults. Since there is a strong correlation

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The predicted shape is the result of an interaction of two effects. First, the Green's function becomes more complex, with multiple arrivals spread out over a longer time window, at larger distances. Second, the fault is larger with larger magnitude earthquakes. Consequently, more distant stations can receive signals from a larger area of fault rupture at any one time. This happens during large earthquakes, when the fault is large, explaining the less rapid attenuation in this circumstance.

This paper has concentrated on peak acceleration, but the synthetics in Figure 6 show similar behavior for peak velocity, peak displacement, and response spectral values. Obviously, the results will depend on the relationship between the size of the fault and the wavelength of the waves that are involved. When the wavelength is long compared to the fault dimension, the attenuation will resemble the attenuation of the Green's function. As the wavelength becomes shorter, the interactions illustrated in Figures 3 and 5 will become effective. Knowing the rupture duration, easily estimated from fault dimension, and characterizing the duration of the Green's function, it should be possible to develop a model which realistically describes the magnitude dependence of the shape of attenuation curves.

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## Acknowledgements

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# Tables

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# Table 1

# Velocity model used for synthetic seismograms

Layer	Thickness	P-wave	Q <sub>P</sub>	S-wave	Qs	Density
	(km)	velocity		velocity		(gm/cm <sup>3</sup> )
		(km/sec)		(km/sec)		
1	2.0	2.90	200	1.60	100	2.28
2	2.3	4.90	200	2.85	100	2.68
3	4.7	5.82	400	3.38	200	2.86
4	36.0	6.55	400	3.81	200	3.03
5	1000.0	8.10	800	4.70	400	3.32

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# Table 2

Characteristics of seismograms used as empirical Green's functions

# (from Anderson et al, 1991)

Earthquake parameters:

Date: May 2, 1989 Origin Time: 09:30:16.72 GMT Latitude: 16.637°N Longitude: 99.513°W Hypocentral Depth: 13.4 km Magnitudes:  $m_b$ =5.4,  $M_s$ =4.9,  $M_{coda}$ =5.1

### Station parameters

Station	Epicentral
	Distance
	(km)
San Marcos	16.9
Las Vigas	33.0
Ocotito	67.7
Teacalco	219.7

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# **Figure Captions**

Figure 1. Predicted values of peak accelerations on as a function of distance, from the regressions of a) Boore et al (1993) and b) Idriss (1991).

Figure 2. Geometry used to consider expected attenuation. The goal is to examine distance effects on a profile perpendicular to a 50 km long fault. Sources used to compute Green's functions are placed at 5 km intervals along the fault (circles). The receivers are at a distances of 5, 25, 50, and 100 km along the perpendicular bisector.

Figure 3. Synthetic seismograms from eleven point sources, located as in Figure 2, and the sum of these synthetics (shown at the top). Green's functions are all convolved with the same composite source time function with duration of about 2 seconds. To illustrate the concepts with maximum clarity, the SH component of the synthetic seismograms has been used for each point source. Numerical values give peak acceleration of the composite seismograms and the largest subevent.

Figure 4. Empirical Green's functions and resulting synthetic seismogram. The empirical seismograms are from a magnitude MW=5.3 earthquake recorded in Guerrero, Mexico. The sum of eleven of the seismograms, shifted as explained in the text, is shown at the top. (Only four of the eleven seismograms are shown in this figure.) Notice how at the two closer stations the main contributions to the composite seismogram come from only one or two of the contributing subevents, while for the two farther stations three or four are contributing at once.

Figure 5. Geometry for profiles of synthetic seismograms.

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Figure 6. Profiles of synthetic seismograms for the magnitude 5 and 6 (6A) and 7 and 7.5 (6B) earthquakes described in Figure 5. In the upper half of this figure, the profiles are normalized by the peak value of each trace. In the lower half, the profiles are all on a common scale determined by the peak value of station S010. Note that for the magnitude 5 and 6 earthquake, the peak values at station S010 are near the largest anyplace in the model, but for the magnitude 7 and 7.5 earthquakes, stations nearer the fault outcrop would give much larger peak values.

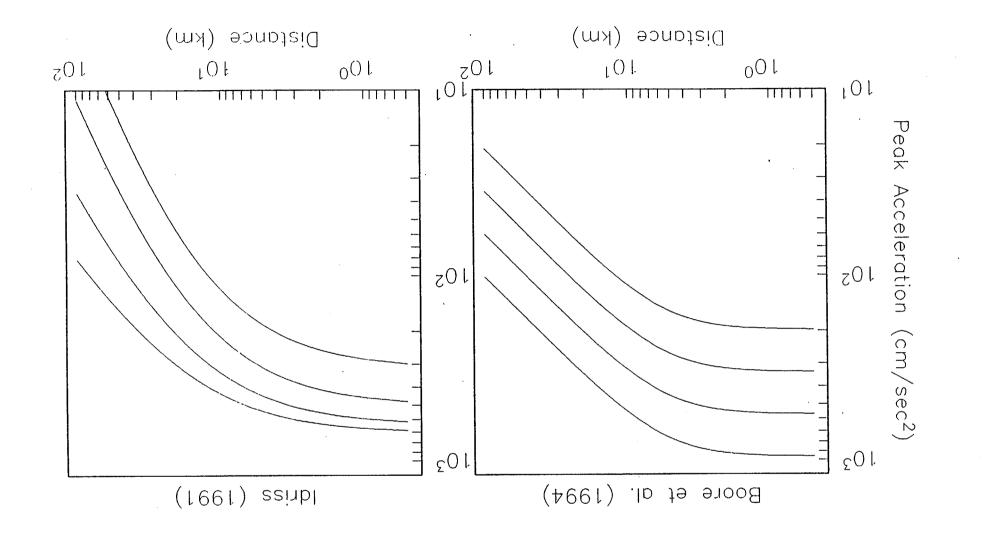
Figure 7. Peak accelerations corresponding to Figure 6, as a function of fault distance.

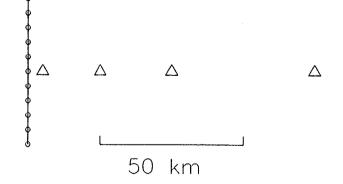
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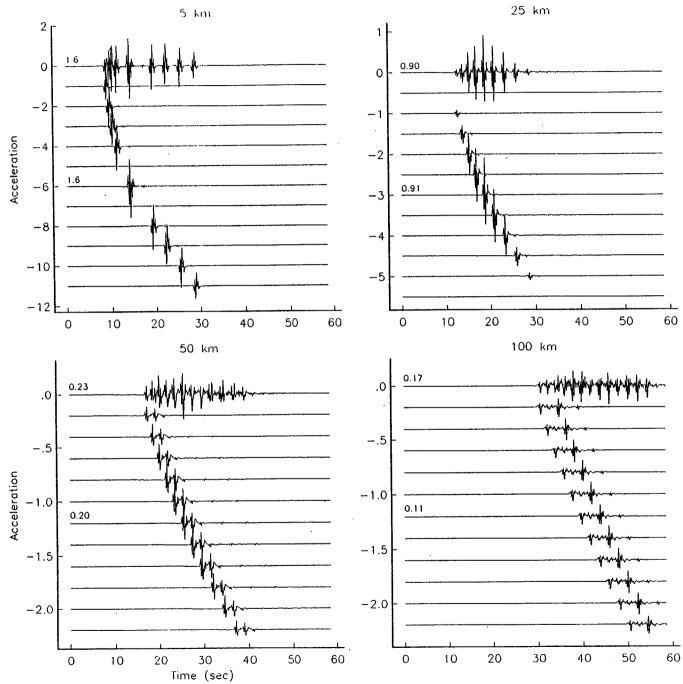
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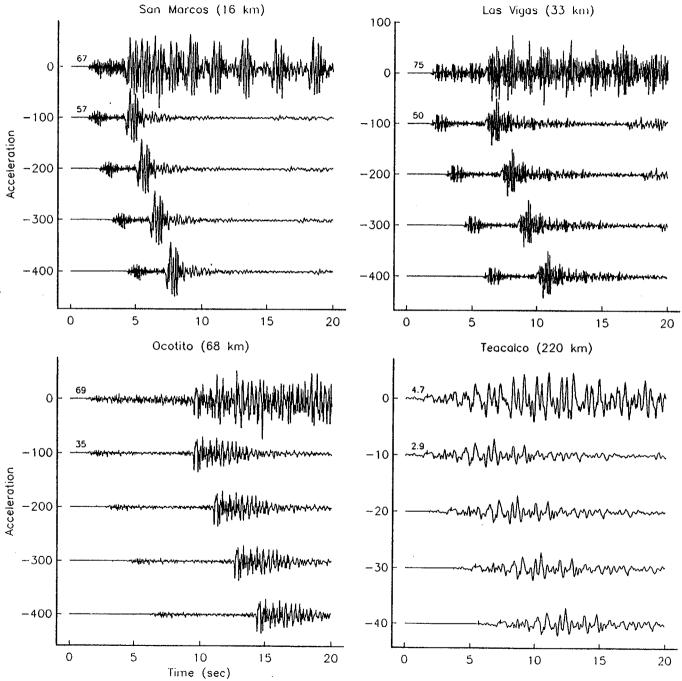
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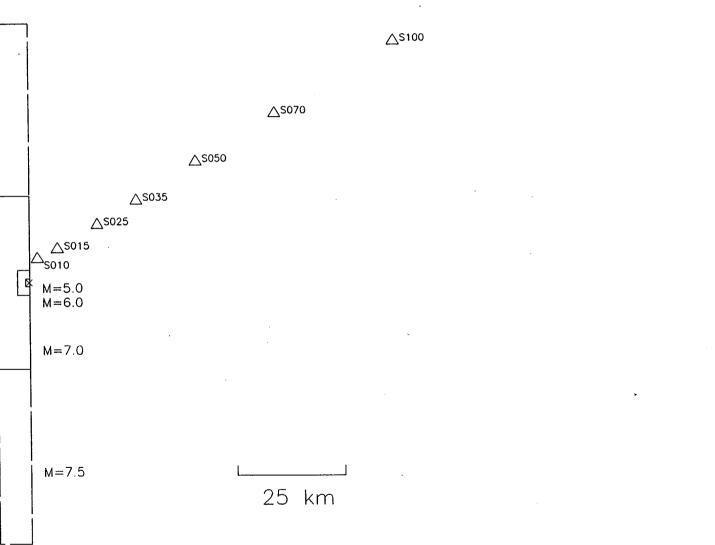


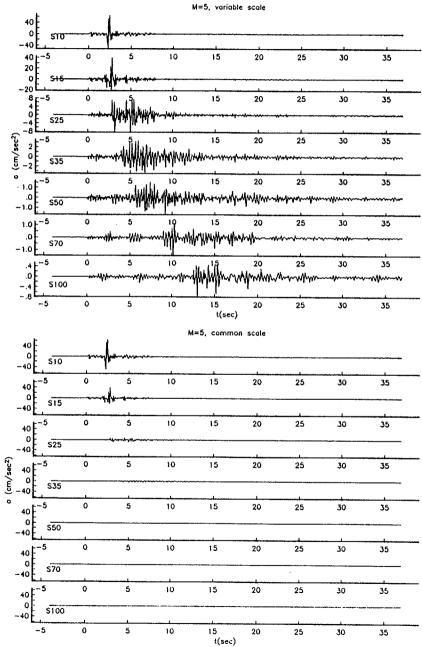


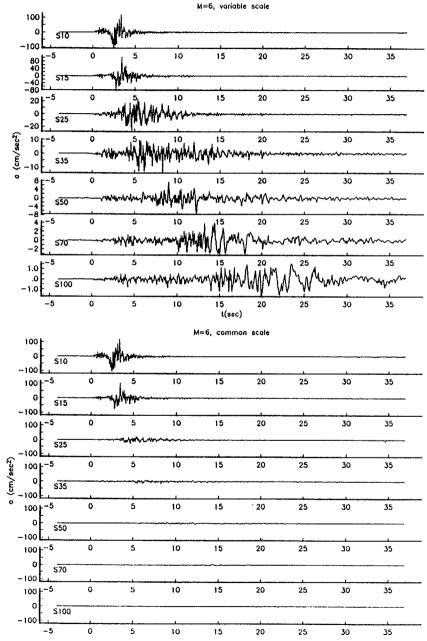


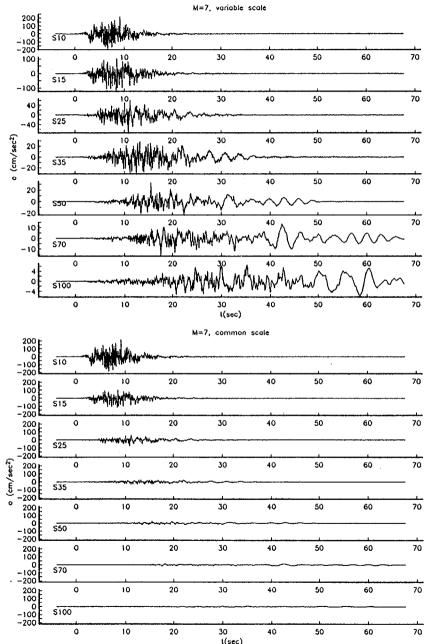


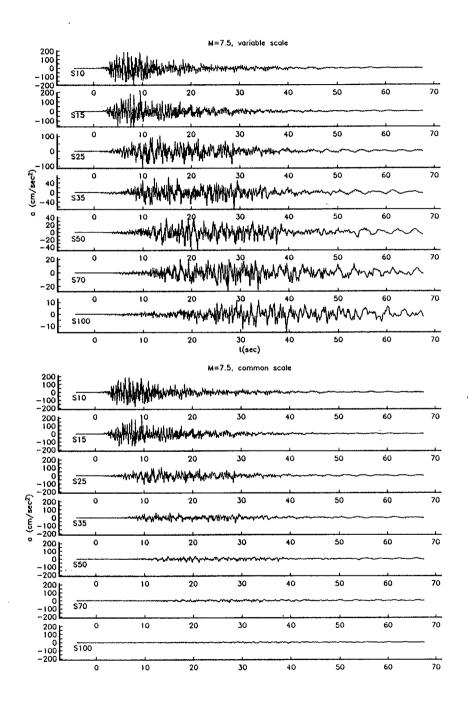




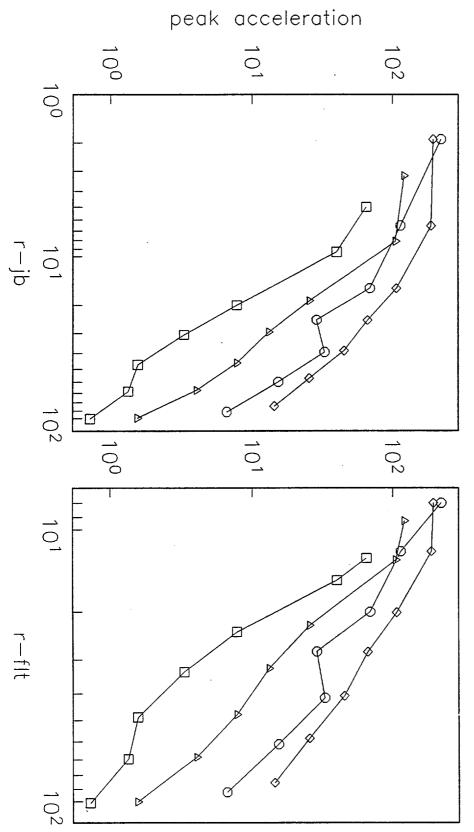








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# ENGINEERING EVALUATION OF THE 1 OCTOBER 1995 DİNAR EARTHQUAKE (M<sub>L</sub>=5.9)

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In 1995, a swarm of earthquakes affected the city of Dinar, Turkey, which is located in Southwest Anatolia and has a population of 35 000. The mainshock having a local magnitude of 5.9 occurred on 1 October 1995. It was preceded by foreshocks for four days, the largest one having a magnitude of 4.7. These foreshocks initiated structural damage in many buildings, which was then severely aggravated by the mainshock and a strong aftershock two hours later, with a magnitude of 5.0. Numerous aftershocks were recorded in the following three months. Strong ground motions were recorded within the city where the mainshock produced horizontal peak accelerations of 0.28gand 0.29g. The Dinar earthquake caused a death toll of 90, and more than 200 injuries. The economic losses due to structural damage alone are estimated at 250 million USD.

Keywords: Dinar earthquake, Anatolian block, Dinar-Çivril fault, foreshock, earthquake damage.

## 1. Introduction

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Following a quiescent period of seventy years, a damaging earthquake of magnitude  $M_L$ =5.9 occurred in Dinar, Turkey on 1 October 1995 at 17.57 local time (3:57 PM, GMT). An intriguing aspect of this earthquake was the arrival of a series of foreshocks of varying magnitudes between  $M_L$ =3.5 and 4.7 within the preceding four days. More than 70 aftershocks with magnitudes between 3.5 and 5.0 were recorded in the following days. Aftershocks were still continuing after three months with decreasing magnitudes.

The earthquake caused 90 deaths and injured more than 200. Eventually, the essential life-lines were affected by the earthquake particularly at their connections to the collapsed buildings: the electricity was cut, the water supply and sewerage systems were seriously influenced. The communication system failed for a short period. The structural damage perspective of the earthquake was also drastic. Out of 24 000 households in the affected region, sheltering a population of 100 000, 4340 were heavily damaged, 3712 experienced moderate damage and 6140 experienced light damage. The Dinar earthquake caused the collapse of about 200 buildings. The replacement and repair costs of the collapsed and damaged buildings totals 250 million US Dollars. Indirect losses due to interruption of business and temporary resettlement expenses are not accounted for in this cost. Since the earthquake occurred in early winter which is severe in Dinar, reconstruction and rehabilitation works could not have been initiated until March 1996. This inevitable delay led to a sudden drop in the city population in the days following the earthquake. Citizens of Dinar who left the city started moving back in summer 1996 with resumption of the construction activity.

The ground motion events were recorded by a digital SMA-1 Kinemetrics accelerograph which is installed in the Dinar Meteorolgical Station. A brief engineering assessment of the nature and consequences of the Dinar earthquake is presented in this paper.

## 2. Seismotectonics of the Region

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The region where Dinar is located has been troubled by earthquakes for centuries. In the Phrygian period (1200-600 BC), the region was called Celainai. In the 8th century BC, Celainai was destroyed by a major earthquake. It is stated in the ancient Anhoros myths that, during the earthquake, water sprang out from the ground. The Hellenistic town Apameia, which was settled in the same region, was devastated by a strong earthquake in 84 BC. During the Roman period (72 BC-395 AD), Apameia was resettled. However, a major earthquake occurred around 225-235 AD and the town was again destroyed. During this last event, some lakes were formed in the region. Apameia was given the name of Geyikler during the Ottoman period. In 1853 and 1875 two major earthquakes struck Geyikler again, the latter caused 1300 deaths. The last major earthquake that Dinar -the name the town bears in the Turkish Republic period- experienced was of magnitude 6.0 in 1925. The epicentral coordinates<sup>1</sup> of this earthquake indicate a location 60 km west of Dinar and the damage it caused was scattered in the rural areas. No one in Dinar today bears the memories of this earthquake.

Anatolia lies at the junction of three major converging plates: the Eurasian, African and Arabian plates as shown in Fig.1. The Arabian plate converges to the Eurasian plate which results in compression along the Bitlis-Zagros thrust and fold belt. This compression is compensated by the westward escape of the Anatolian block along the right-lateral North Anatolian fault and the left-lateral East Anatolian fault, also with the Eastward movement of the North-East Anatolian block. On the other hand, with the hindrance of this movement by the Hellenic arc on the West, the Anatolian block is redirected towards Southwest. Besides, the African plate subducts under the Anatolian block at the Northeast side of the Rhodes Island via the Hellenic arc. Under-these complex effects, Dinar and its surrounding region experience extensional faulting in the Northeast-Southwest and compressional faulting in the Northwest-Southeast directions. Accordingly, this region covering the Aegean graben system and Hellenic arc produces very high seismic activity with respect to the surrounding

regions. Detailed information on the seismotectonics and seismicity of West Anatolia and the Aegean system can be found in References 1-4.

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The earthquakes which occurred in this century in the Aegean region exhibited a spatial migration Northward, from the Hellenic arc to the Aegean graben system. A remarkable increase in seismic activity had been observed in two time cycles<sup>2</sup>, first from 1900 to 1920 and the second from 1920 to 1960. Seismic activity has decreased from 1960 to the present day. The epicenters of the earthquakes that occurred in the period 1900-1994 are plotted in Fig.2. There are four major identified active faults in the vicinity of Dinar. On the East there are Tatarlı and Kumdanlı faults. The Burdur and the Acıgöl faults are to the South and Southwest of Dinar, respectively. All of these faults have left lateral slip. However, the causative fault of the October 1 Dinar earthquake was the previously unrecognized 50 km long Dinar-Çivril fault. This is a normal fault with a slight right lateral strike slip. During the last 70 years, there were no moderate to major earthquakes which affected the Dinar region. Hence, this resulted in significant accumulation of strain energy in the active fault system over the ensuing years. A spot panchromatic satellite view of Dinar and vicinity pictured after the last earthquake is shown in Fig.3. Local faults have been traced on the picture after an extensive field survey in the region, by matching the pictorial information with the field observations. The fault scarp is indicated with the light line on the figure. Dinar is in the lower middle part of the picture, to the South of the ruptured faults end. A close-up picture of the fault scarp is shown in Fig.4.

The first fault rupture occurred on September 26 which resulted in minor earthquakes  $(M_L < 4.7)$ . The mainshock took place at 17:57 local time on October 1  $(M_L=5.9, M_w=6.1)$ , which was followed by a strong aftershock  $(M_L=5.0)$  two hours later. The mainshock was produced by the 25 seconds rupture of the Dinar-Çivril fault at a focal depth of 24 km. Epicenters of the recorded earthquakes after the first rupture are depicted in Fig.5. The epicentral coordinates of the mainshock are 38.13 N-30.08 E. The distribution of the magnitudes of earthquakes during 21 days are presented in Fig.6.

The surface rupturing and fault plane solutions have indicated normal faulting with a slight right-lateral component. The vertical displacements along the fault scarp ranged from 20 cm to 50 cm whereas the horizontal displacements were between 5 and 10 cm.

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The Dinar earthquake has been assigned a local magnitude  $M_L=5.9$ , a moment magnitude  $M_w=6.1$  and a seismic moment of  $1.68 \times 10^{25}$  dyne.cm by the Earthquake Research Department of the General Directorate of Disaster Affairs. The faulting surface area is estimated as  $15 \times 16 \text{ km}^2$  and the first nodal plane has a Strike= $144^\circ$ , Dip= $48^\circ$  and Slip= $-125^\circ$ .

#### 3. Ground Motion Intensity and Strong Motion Characteristics

The isoseismal contours constructed to reveal the intensity distribution of the Dinar earthquake exhibit circular shapes where the inner circle for an MKS<sup>6</sup> intensity of VIII has an approximate diameter of 20 km, and the next circle with intensity VII has a diameter of 30 km. Dinar town is divided into two by the intensity VIII contour along the slope border indicated in Fig.7. The Western part of the town located on alluvial deposits is in the intensity zone VIII whereas the eastern part settled along the hillside remains in the intensity zone VII. According to MKS intensity scale, VIII corresponds to 5% heavy and 75% medium damage in reinforced concrete structures.

The strong ground motions of the Dinar earthquakes were recorded by an analog Kinemetrics SMA-1 accelerograph installed in the Dinar Meteorological Station (Fig.7). The station is located in the Southwest end of the city which is underlain by alluvial deposits. Hence, there is considerable damage in the vicinity. The location of concentrated building damage within the city is given in Fig.7.

During a time span of ten days, the number of earthquakes which occurred in Dinar with magnitudes  $M_L \ge 4.5$  is seven, as indicated in Fig.6. Three of them are foreshocks,

one is the mainshock and three are aftershocks. The strong ground motions induced by these earthquakes are all recorded by the Dinar SMA-1 station. Their basic properties are listed in Table 1, and the time variations of the respective horizontal ground acceleration components are presented in Fig.8.

Date	Time	Depth	Distance	ML	Peak Acceleration (g)			Peak Velocity (cm/s)		
	(GMT)	(km)	(km)		NS	EW	v	NS	EW	v
26.09.1995	14:58	20	6	4.7	0.106	0.174	0.056	4.9	8.6	2.5
27.09.1995	14:16	30	8	4.7	0.077	0.163	0.040	5.6	13.1	2.5
01.10.1995	15:57	24	13	5.9	0.294	0.275	0.111	17.7	21.1	5.7
0110.1995	18:03	20	18	5.0	0.208	0.118	0.038	16.4	10.6	2.1
05.10.1995	16:15	20	2	4.6	0.089	0.151	0.057	<u> </u>		
06.10.1995	16:16	24	24	4.5	0.093	0.152	0.042	2.9	8.9	1.7

Table 1. Strong Motion Data for Dinar Shocks with  $M_L \ge 4.5$ 

The Dinar earthquake mainshock is also recorded by three distant strong motion accelerograph stations. These station locations, their epicentral distances and larger horizontal peak accelerations are as follows: Çardak, 54 km, 0.070*g*; Burdur, 70 km, 0.0519*g*; and Denizli, 87 km, 0.013*g*. Burdur and Denizli are indicated on Fig.5, whereas Çardak is on the midway between Dinar and Denizli.

Dinar is located in earthquake Zone-1 (most severe) of the Turkish Seismic Zones Map which was substantially revised in 1996 in view of an extensive study<sup>7</sup>, summarized in Reference 8. Dinar was always in Zone-1 in the previous versions of the seismic zones maps as well. According to Reference 7, the peak ground acceleration expected in Dinar with a 10% probability of exceedance in 50 years, i.e. with a return period of 475 years, is 0.486g. The effective peak acceleration assigned to Zone-1 in the Turkish Seismic Design Code<sup>9</sup> is 0.40g. This value appears rational for Dinar concerning the difference between the effective and actual peak ground accelerations. In the same study<sup>7</sup>, peak ground acceleration with 40% probability of exceedance in 50 years (return period of 100 years) is calculated as 0.336g. Since the recorded peak ground acceleration in Dinar is 0.294g (Table 1), the 1 October 1996 earthquake falls into an event category with a return period close to, but less than 100 years. This is in conformance with the seismicity of the region discussed above.

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The elastic acceleration response spectra for Dinar earthquakes calculated for 5% damping are shown in Fig.9. It is observed from the figure that the effective period range of the lateral forces resulting from the earthquakes is not broad. The main shock is observed to have no significant effect on very short period structures. Although the forces acting on intermediate period structures are higher, these forces decay quickly beyond the period of 1 second.

The smaller earthquakes recorded in Dinar have no appreciable horizontal force contribution on the existing buildings. However, these forces may increase the damage that a structure experienced earlier. A softened, and consequently increased period structure may undergo large displacements under the effect of the mainshock and aftershocks.

The correlation between the intensity of the earthquake ground motions and the damage experienced by structures can be expressed by the dissipated energy spectrum. This is because the energy which is dissipated by the structural system during the ground motion duration is directly related to the structural damage. Dissipated energy spectrum is sensitive to the peak acceleration, effective duration and the frequency content of the earthquake excitation, which are the dominant characteristics of the intensity of shaking. The accumulated and the mainshock's individual dissipated energy spectra are presented in Fig.10. Although it is not possible to supply a cumulative elastic acceleration response spectrum for sequential shocks, a cumulative energy spectrum can be provided. It can be observed from Fig.10 that foreshocks and aftershocks have contributed significantly to the probable damage of medium period structures.

## 4. Influence of Soil Properties on the Observed Damage

It is evident in Fig.7 that the slope border defines a sharp boundary to the section of the city where damage is concentrated. Most of the damaged buildings are located on loose alluvial deposits. Surprisingly however, the foundations of the damaged buildings did not exhibit any signs of failure or settlement. This decision is based on the observations of footings from 35 damaged buildings unearthed randomly by digging pits around them. There were no failures also to underground service mains due to any soil deformation. Although water was cut after the earthquake for several days, this had resulted from broken pipe connections at the service entrances of collapsed buildings.

A general distribution of damage density in Dinar is shown in Fig.11, where the city center is mapped on to the satellite view indicating close faults, global topography and soil conditions. Alluvial deposits are marked with light plain color along the valleys. It can be observed that the districts which sustained damage are located on the alluvial plain deposits. It is difficult however to propose a significant correlation between the intensity of damage and the thickness or bearing capacity of alluvial soil. Damage distribution on the alluvial region is fairly irregular although the construction quality is uniformly poor throughout the entire city.

Five shallow borehole logs of 30 m depth have been taken from the heavily damaged part of the city, circled in Fig.7. The boring data indicate that the water table depth varies between 3-5 m. Similar soil composition is observed from all five boring logs, which is mainly constituted of sand and gravel with small amounts of clay and silt. A loose filler material covers the surface with a thickness varying between 0.2-4.2 m. Standard penetration (SPT) blow counts are between 4-20 in the first fifteen meters, and between 20-50 in the second fifteen meters. Accordingly, sand and gravel series can be classified as loose and medium dense in the two consecutive surface layers. Saturated sand and gravel layers with low SPT blow counts increase liquefaction potential substantially during an earthquake. However there was no evidence of liquefaction during the Dinar earthquake, except for isolated sand mounds along an irrigation canal. Grain size and the duration of strong motion did not perhaps provide necessary conditions for liquefaction.

Since Dinar is still vulnerable to future earthquakes, the seismic response characteristics of the alluvial basin should be determined through detailed studies. A number of research studies have already been initiated; however, the insufficiency of strong motion data handicaps the accuracy of these studies.

#### 5. Evaluation of Structural Damage

The total population affected from the earthquake in the region is 100,000 and the number of households is about 24,000. The damage survey conducted in the affected region after the earthquake revealed that, out of 24,000 households 4340 (18%) were heavily damaged, 3712 (15%) were moderately damaged, 6104 (25%) were lightly damaged and the remaining 9844 (41%) were undamaged. In the city center (Fig.7), heavy damage in residential units increases to 31%. Two hundred buildings were completely collapsed. According to these figures, a death toll of 90 might be considered less than expected. The foreshocks in the preceding four days of the mainshock considerably reduced the death toll because many residents had already left the city before October 1 by fear and expectation of a big quake.

The building stock in the city mainly consists of 3-6 story reinforced concrete and 2-4 story masonry buildings at the city center where damage was concentrated, and 1-2 story adobe, stone and brick masonry buildings on the slopes and outskirts of the city. Considering that seismic energy is intensified within the period range of 0.3-1 seconds (Fig.10), buildings having three or more stories which were already damaged

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to some extent and softened due to foreshocks possibly received high seismic forces during the mainshock.

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An independent survey had been conducted by the Chamber of Civil Engineers on 103 public buildings in Dinar after the earthquake. According to their quick expert evaluation, 20 of these buildings were heavily damaged or collapsed, 10 were medium damaged, 20 were lightly damaged and the remaining 53 were undamaged. Fourteen of the twenty heavily damaged buildings were 3-5 story reinforced concrete framed buildings, which constitute the most vulnerable building class in Turkey.

Damage evaluation is presented in two parts here, seperately for heavily damaged or collapsed buildings and moderately damaged buildings. The reasons leading to building collapses are usually very obvious and not informative other than repeating the well known mistakes. Moderately damaged buildings on the other hand manifest relatively less obvious facts on structural weaknesses, hence their evaluation may contribute to improving our current knowledge.

# 5.1. Heavily Damaged and Collapsed Buildings

A structural classification of collapsed buildings is given in Table 2. Single story buildings did not experience partial or total collapse, including adobe dwellings. There were no steel or precast concrete structures in Dinar during the earthquake.

Structural	Number of	Number of Collapsed Buildings			
System	Stories	Single Story Collapse	Total Collapse		
R/C Frame	≥4	33	28		
R/C Frame	3	29	18		
Brick Masonry	4	32	41		
Brick Masonry	3	10	4		
Composite Masonry	2	6	-		

Table 2. Classification of 200 Collapsed Buildings in Dinar

It is revealed in Table 2 that soft story formation is responsible for many reinforced concrete building collapses. A weak ground story is usually created with the intention of reserving open space for commercial use. Since this story does not benefit from the presence of infill masonry walls, as shown in Fig.12, damage accumulates in this story and eventually leads to failure. It should be noted that the entire framing systems of such buildings are weak, as the three story building in Fig.12, but the contribution of infills to overstrength masks these weaknesses in the other stories. Another example of weak concrete frame is shown in Fig.13, in which one of the three identical buildings under construction had collapsed before receiving its full vertical load. None of the joints satisfied strong column-weak beam criteria, no shearwalls were employed, and orientation of strong column axes had led to an even weaker frame in one direction.

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An extraordinary failure is shown in Fig.14, where the standing building was constructed with four stories originally. The collapsed building on the left had later been constructed as five storied by the same owner and contractor, during which a fifth story was added to the building on the right, and a common roof was shared. The hanging roof fell down due to an aftershock a few days later. The standing building was heavily damaged due to several reasons, soft story, weak frame, and pounding by the short adjacent building. It was demolished later.

A middle story failure is presented in Fig.15 due to pounding. The brick masonry building on the right served as a lateral support in one direction, resulting in accumulation of shear forces at the intermediate story. Seismic joints are never taken into consideration in Turkey, although it is mandatory due to the seismic code<sup>9</sup>.

Low concrete quality also plays an important role in the failure of buildings discussed above. A material quality survey conducted in Dinar on 35 buildings by performing both destructive and non-destructive testing revealed an average concrete compressive strength of 10 MPa. The concrete in these buildings were prepared at the site by ordinary workers, which is a common practice in many small towns as Dinar. It is

very difficult to obtain a 28 day concrete strength of 15 MPa under these conditions, which is a minimum requirement in the seismic Zone 1 according to Turkish code.

The number of stories in brick masonry buildings is limited to two in Zone 1 by the Turkish seismic code. The masonry buildings shown in Figs.16 and 17 were constructed originally as single storied by using solid bricks. Several years later, with a permission from the municipality, two more stories were added despite violating the code. Hollow, non-load bearing bricks were used to construct these additional stories in order to reduce both the weight and the cost. No damage occured in the original stories while the poor performance of added stories have severely punished code violation. Unfortunately non-load bearing hole bricks with hollow ratios exceeding 50%, actually produced for infill wall construction, are being widely used in bearing wall construction in the recent years. Future earthquakes will definitely be brutal against this practice.

## 5.2. Medium damaged buildings

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Structural irregularities are the main cause of medium damage in buildings which otherwise possess code specified lateral resistance. The building shown in Fig.18 has both plan and elevation irregularity which is not accounted for in its seismic design. A sudden change in story plan and height above the ground story (Figs.19, 20) has again resulted in soft story formation, displayed by broken storefront windows.

Many buildings with poor lateral resistance remained in the medium damage level due to the overstrength provided by masonry infill walls (Figs.21, 22). The extent of damage would be more dramatic without the presence of infill walls in most of the concrete framed buildings. They had acted as passive energy dissipation devices as long as they maintained their integrity within the enlosing frame. However such a positive performance should not be expected during a longer ground excitation.

Reinforced concrete connections which do not satisfy strong colum-weak beam requirement experienced damage at the column ends (Fig.23). If this condition prevails in all connections, heavy damage becomes inevitable. Another case of joint failure was due to the formation of cold joints at the top of columns (Fig.24). This is a result of casting slab and girder concrete several days after casting the column concrete below. Hence, the associated joint behaves as a semi-rigid connection.

Inadequate frame configurations may lead to premature failure of certain elements under seismic effects. The columns in a small industry complex in Dinar, shown in Fig.25, received systematic damage in all frames although they support a very light roof. However total frame action could not have been developed since the individual frames were not connected to each other transversally. Accordingly, these columns were forced to restrain the transverse drift of longitudinal frames, similar to the fixed support of a lever arm.

It can be concluded finally that the predominant reason for structural damage in Dinar was the violation of the basic seismic code requirements. Those buildings which satisfy the 1975 seismic code<sup>9</sup> (which was valid in 1995 and updated in 1996) did not sustain any serious damage during the 1995 Dinar earthquake.

# 6. References

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9. Requirements for Buildings in Disaster Regions (Ministry of Public Works and Settlement, Ankara, 1975).

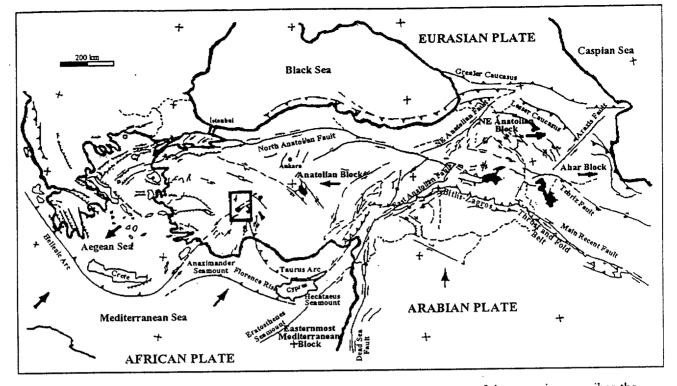


Fig.1. A general neo-tectonic map of Turkey. The rectangle to the Southwest of the map circumscribes the region affected by the 1 October 1995 earthquake and is enlarged in Figs.2 and 5.

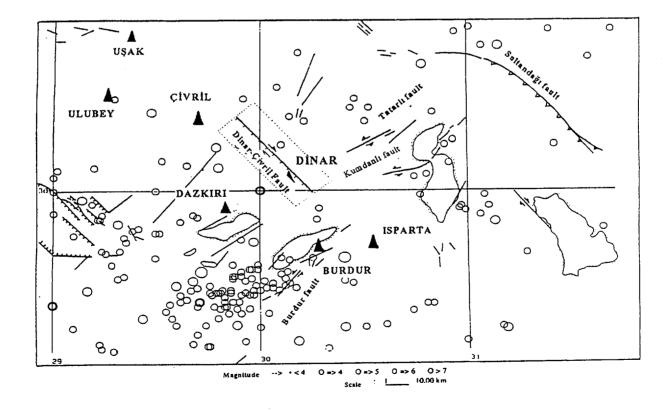


Fig. 2. Major faults around Dinar and epicenters of the earthquakes between 1900-1994.

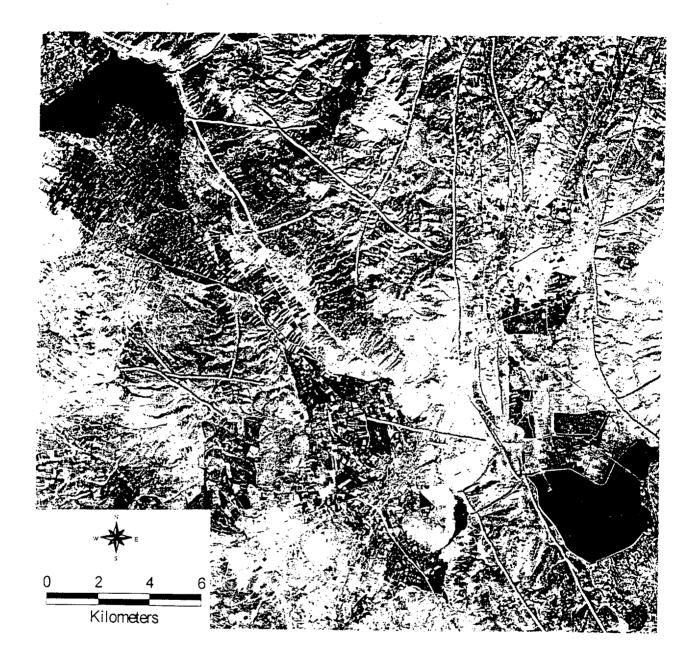
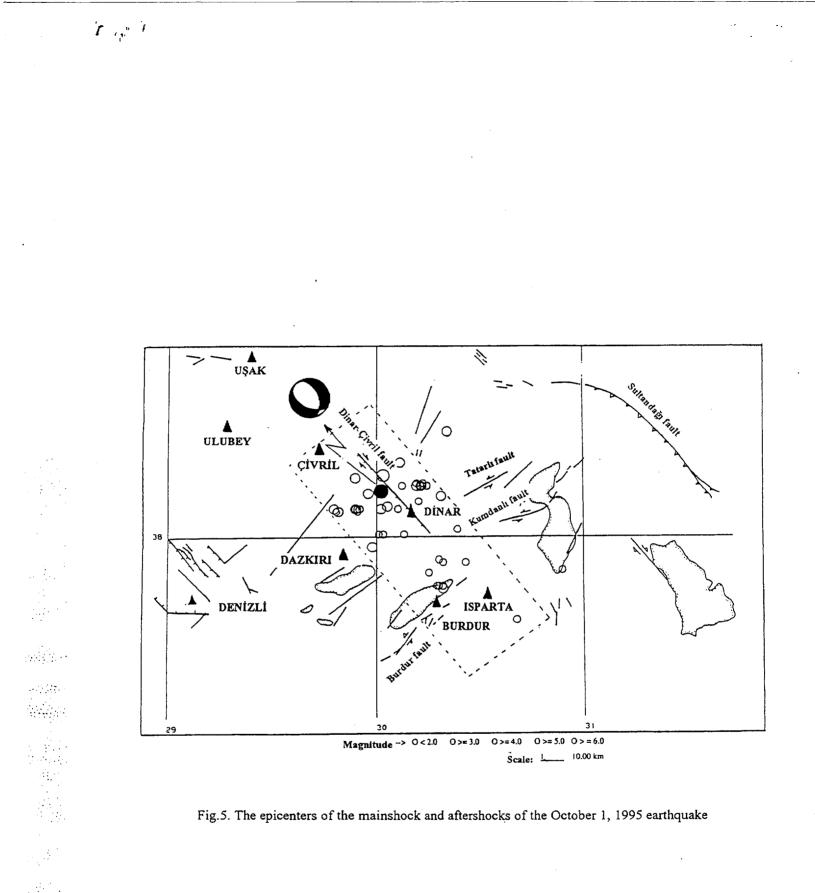


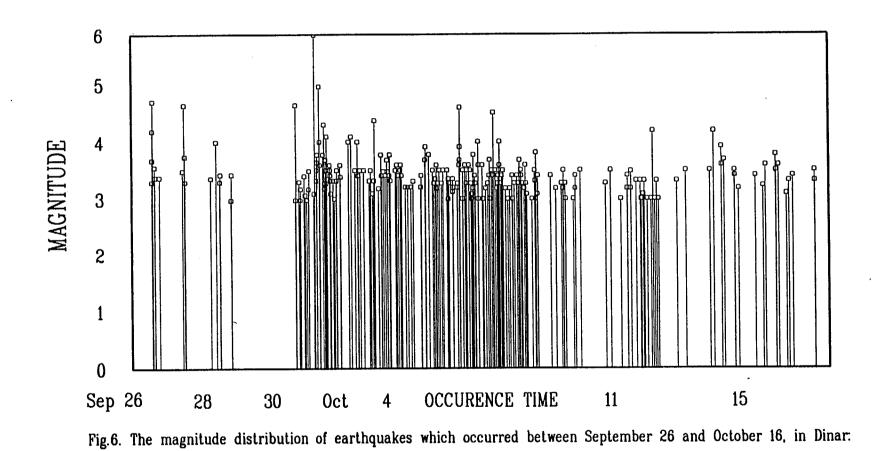
Fig.3. Satellite view of Dinar and vicinity. Local faults are marked with dark lines and the ruptured fault is marked with a light line.



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Fig.4. Fault rupture during the Dinar earthquake.





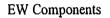
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Fig.7. Dinar settlement plan.

# NS Components

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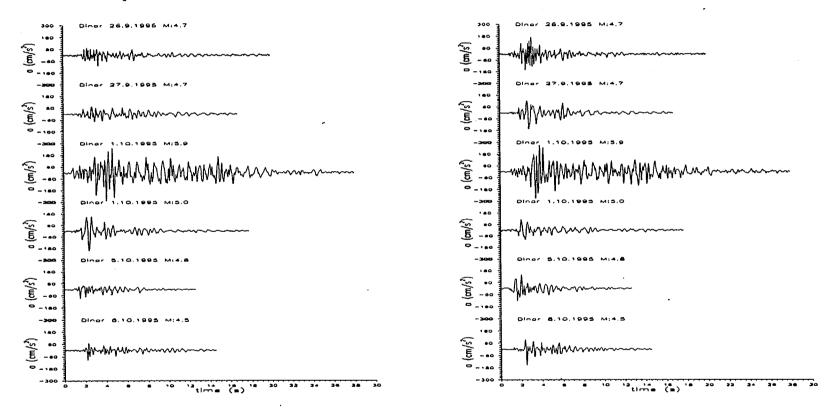
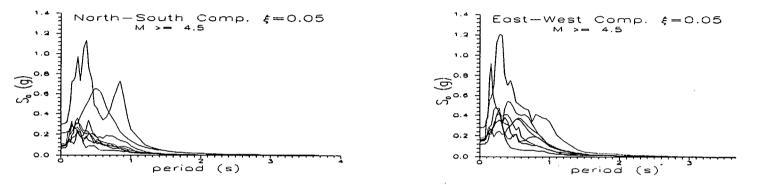
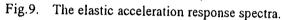
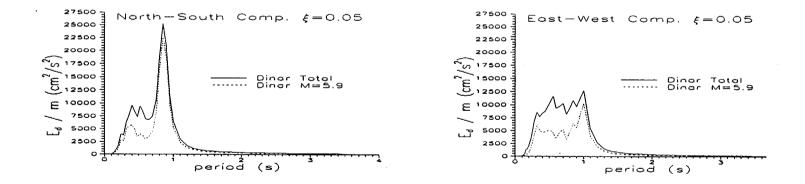
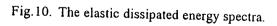


Fig.8. Time variations of the horizontal ground motion acceleration components which have magnitudes greater than 4.5.









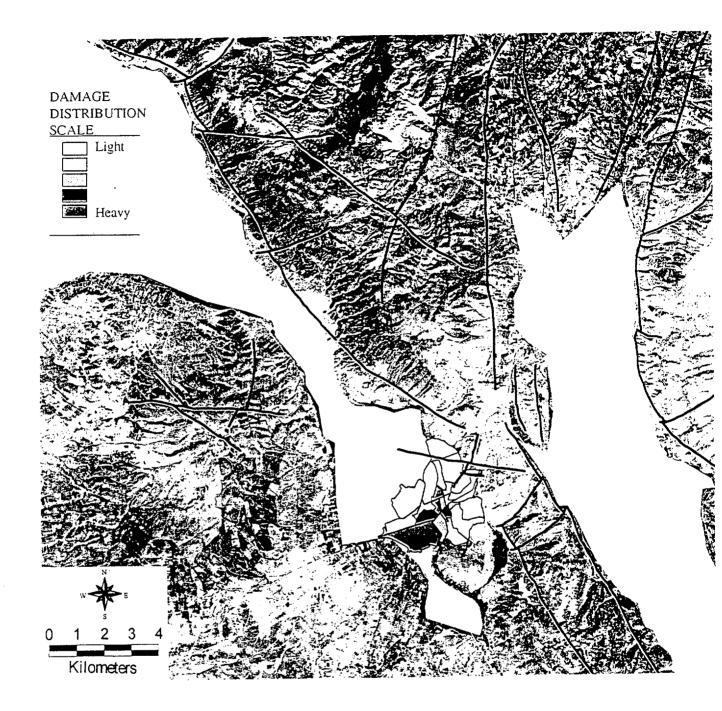


Fig.11. A general distribution of damage density in Dinar, mapped onto the satellite view. Alluvial deposits along the valleys are indicated with light plain color.

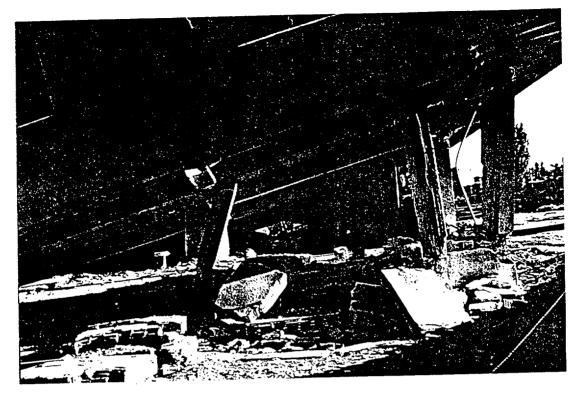


Fig.12. Soft story failure in a three story building



Fig.13. Three identical reinforced concrete building frames under construction. Notice that the strong column axes oriented in the same direction.

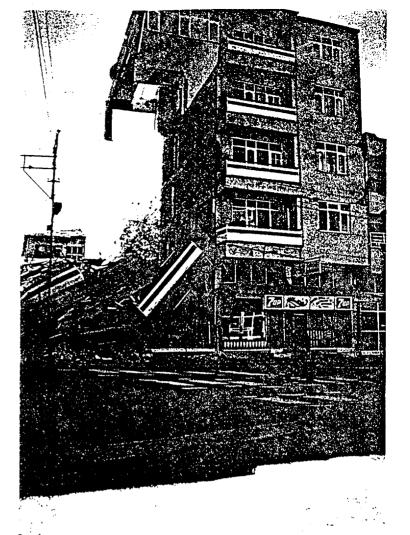


Fig.14. Adjacent collapsed and heavily damaged buildings sharing the same roof.



Fig.15. Middle story failure due to pounding.

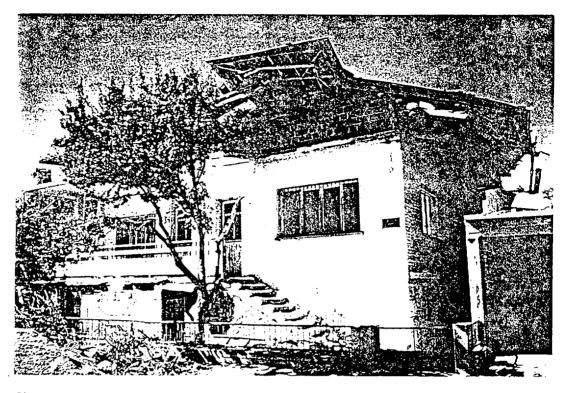


Fig.16. Three story masonry building. Top two stories constructed with hollow bricks collapsed onto the first story with solid brick walls.



Fig.17. Three story masonry building having identical failure pattern with the building in Fig.16. The original first stories sustained light damage in both buildings.

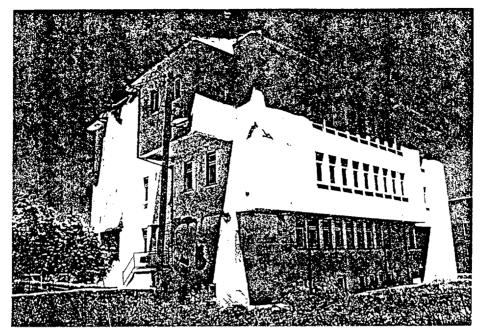


Fig. 18. Irregular building with medium damage.

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Fig. 19. Medium damage in a five story reinforced concrete frame due to soft ground story.

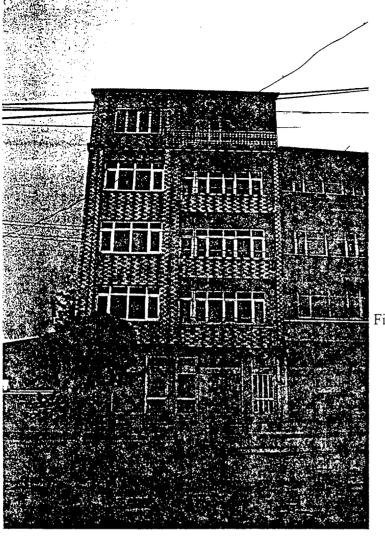


Fig.20. Medium damage in a five story reinforced concrete frame. Structural configuration and story plan changes above the ground story.

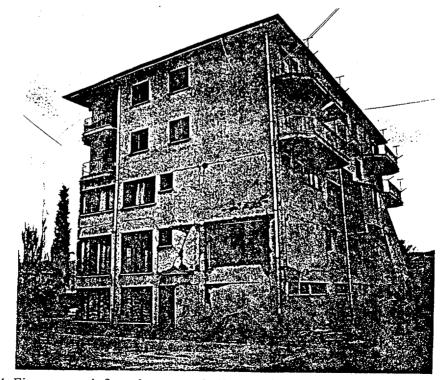


Fig.21. Five story reinforced concrete building where lateral stiffness increases with height. Infill walls resist excessive drift demands at the lower stories.

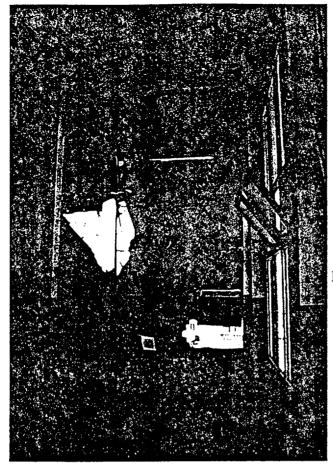


Fig.22. Infills walls providing lateral resistance in a weak frame.

Fig.23. Shear-flexure failure in a weak column connecting to stronger beams. Notice inadequate spacing of stirrups.

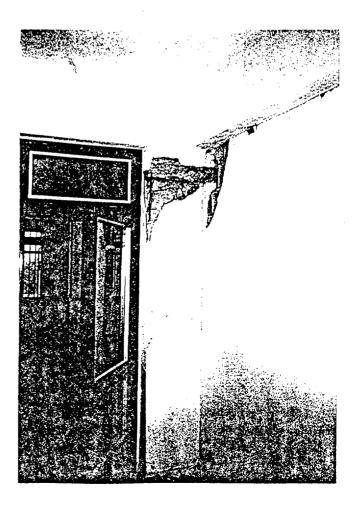




Fig.24. Cold joint at the top of a column.

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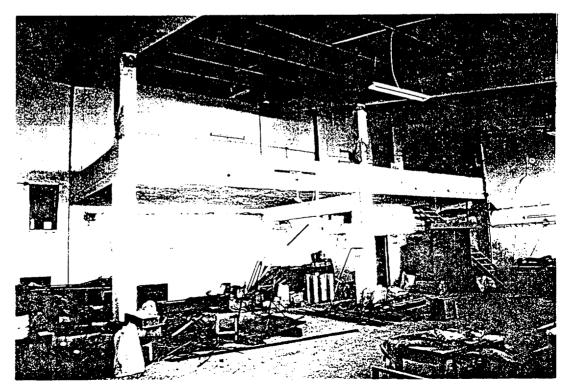


Fig. 25. Transversally unconnected frames in a small industry complex.

## **Evaluation of Linear and Nonlinear Dynamic Rock Properties: Yucca Mountain Samples**

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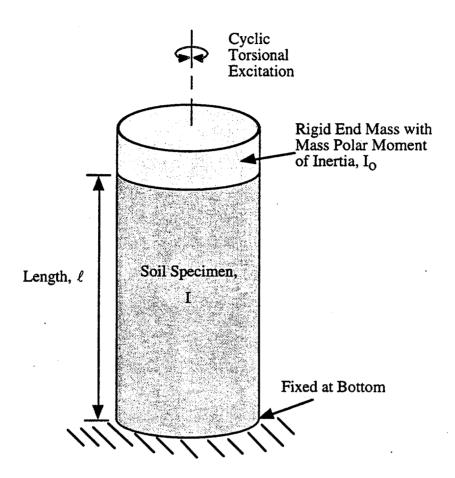


Fig. 1 Idealized Test Configuration of the Fixed-Free Resonant Column/Torsional Shear (RCTS) Device

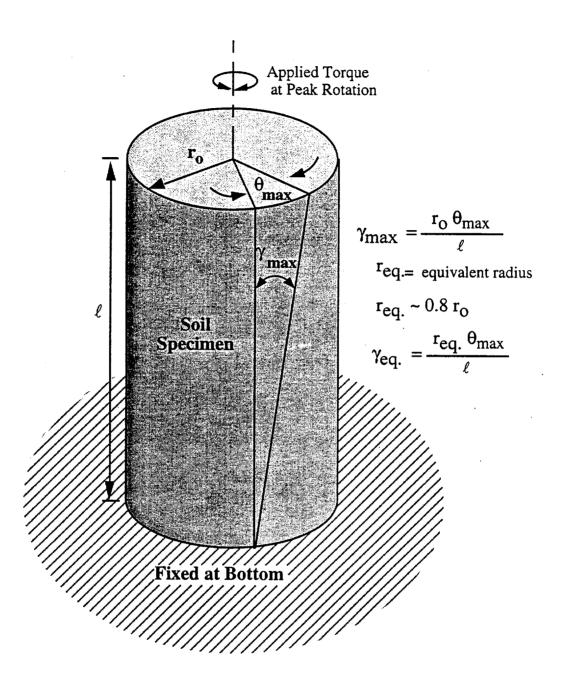


Fig. 2 Illustration of "Equivalent" Shearing Strain in a RCTS Specimen

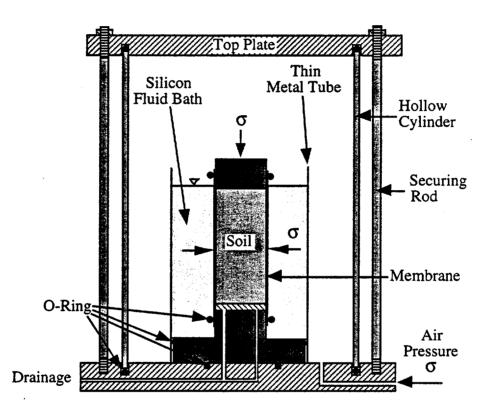
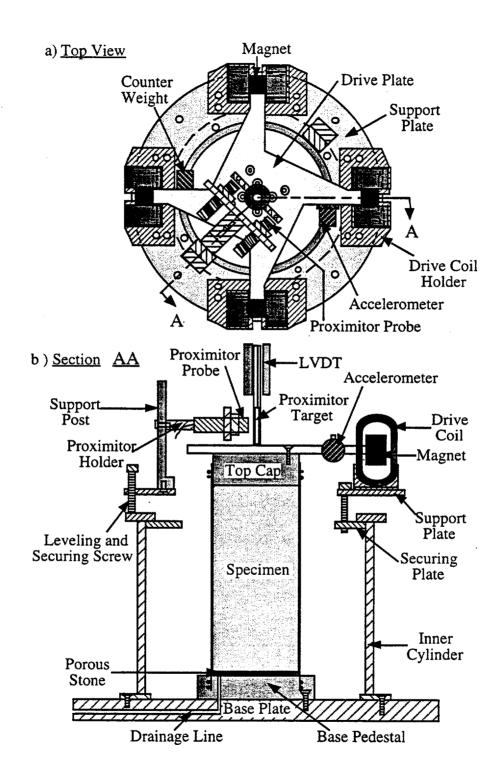


Fig. 3 Simplified Cross-Sectional View of RCTS Confinement System



## Fig. 4 General Configuration of RCTS Equipment

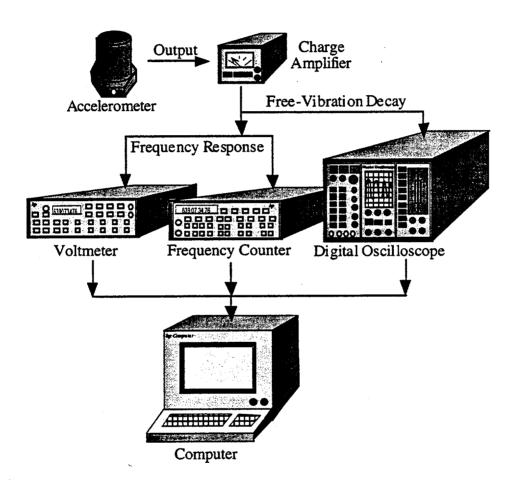


Fig. 5 Schematic Diagram of The Motion Monitoring System in The Resonant Column Test

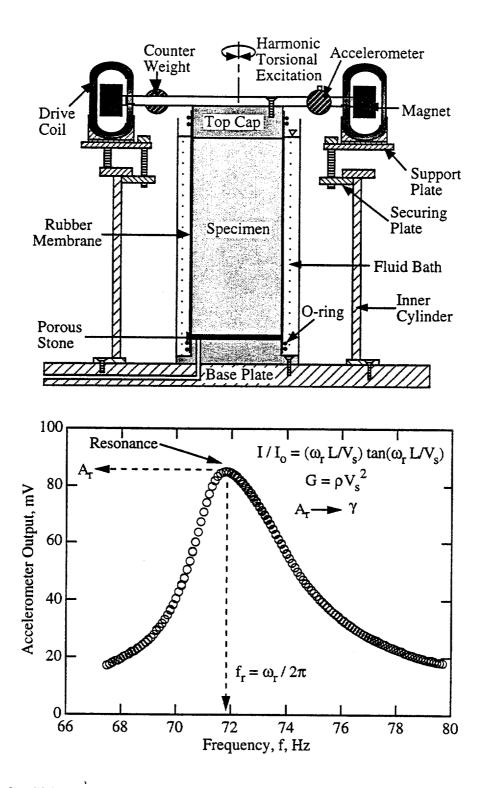


Fig. 6 Side View of a Fixed-Free Resonant Column Test Set-up and a Typical Frequency Response Curve

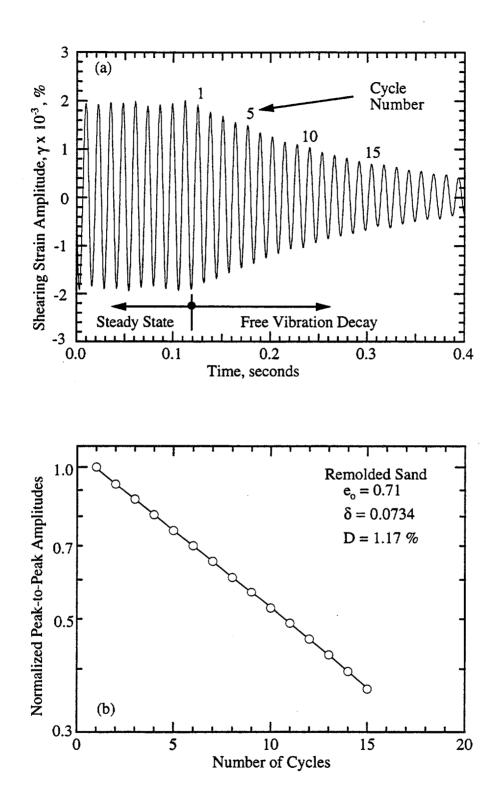


Fig. 7 Typical Free-Vibration Decay Curve (a) and Material Damping Measurement (b) in the Resonant Column Test Using Remolded Sand

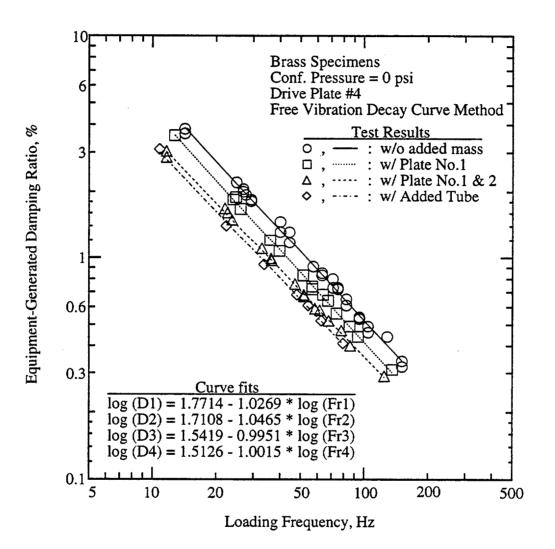


Fig. 8 Variation of the Equipment-Generated Damping Ratio Measured by Free-Vibration Decay Curve Method with Three Different Masses Added on Top of the Drive Plate No. 4

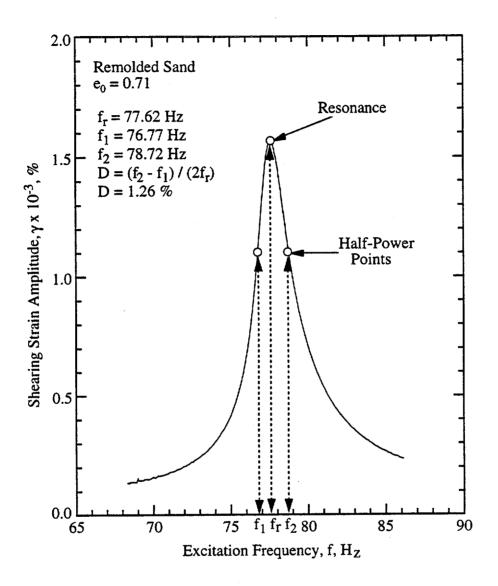


Fig. 9 Typical Material Damping Measurement from the Frequency Response Curve in the Resonant Column Test Using the Half-Power Bandwidth Method Using Remolded Sand

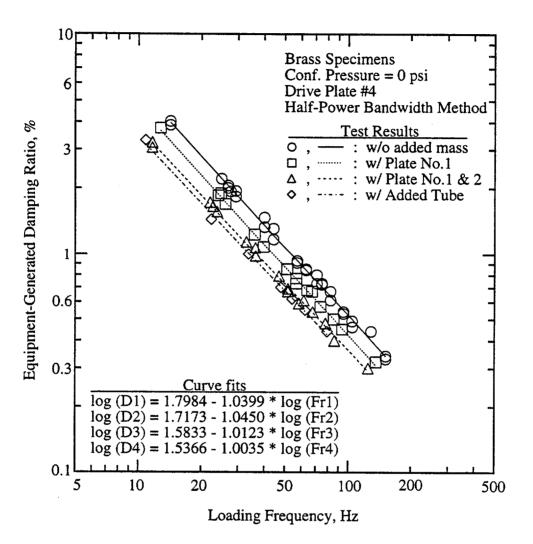
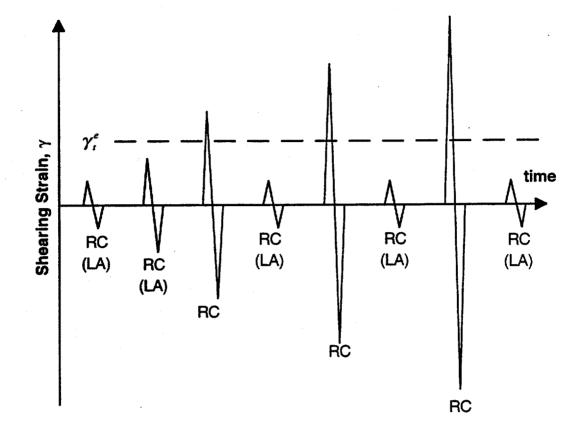


Fig. 10 Variation of the Equipment-Generated Damping Ratio Measured by Half-Power Bandwidth Method with Three Different Masses Added on top of the Drive Plate No. 4



 $\gamma_t^e$  = elastic threshold strain; below  $\gamma_t^e$ , G is constant and equal to G<sub>max</sub>

RC (LA) = resonant column test at low-amplitude strain

- RC = resonant column test in which 500 to 1000 cycles of loading is applied during each measurement
- Fig. 11 Testing Procedure Used in the Resonant Column Test to Investigate the Effects of Strain Amplitude on Shear Modulus (G) and Material Damping Ratio (D)

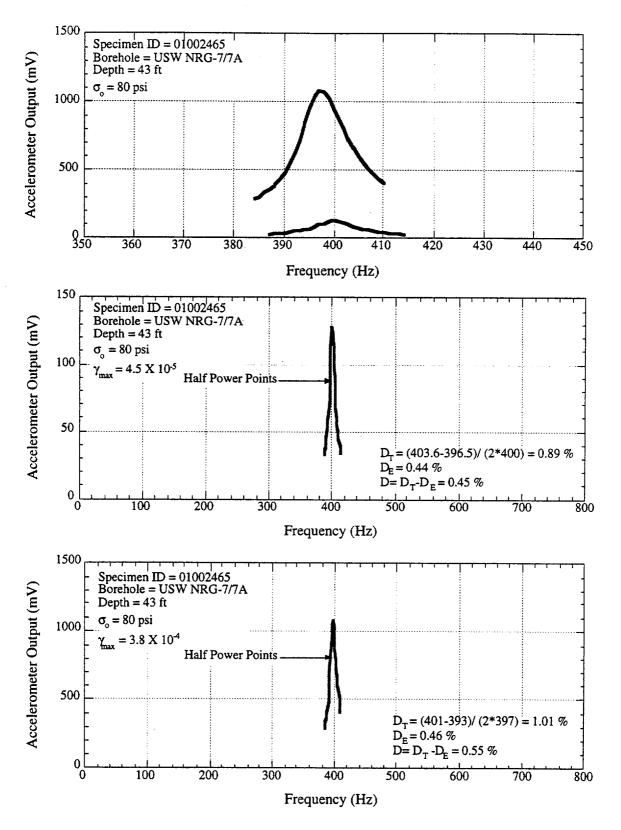


Fig. 12 Determination of Material Damping Ratio from the Half-Power Bandwidth Method

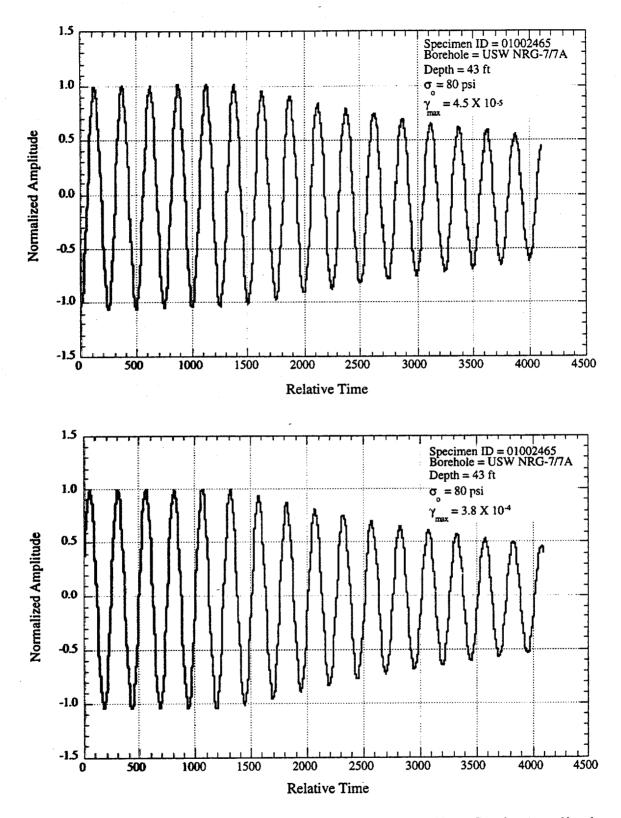


Fig. 13 Typical Free-Vibration Decay Curves at Two Strain Amplitudes

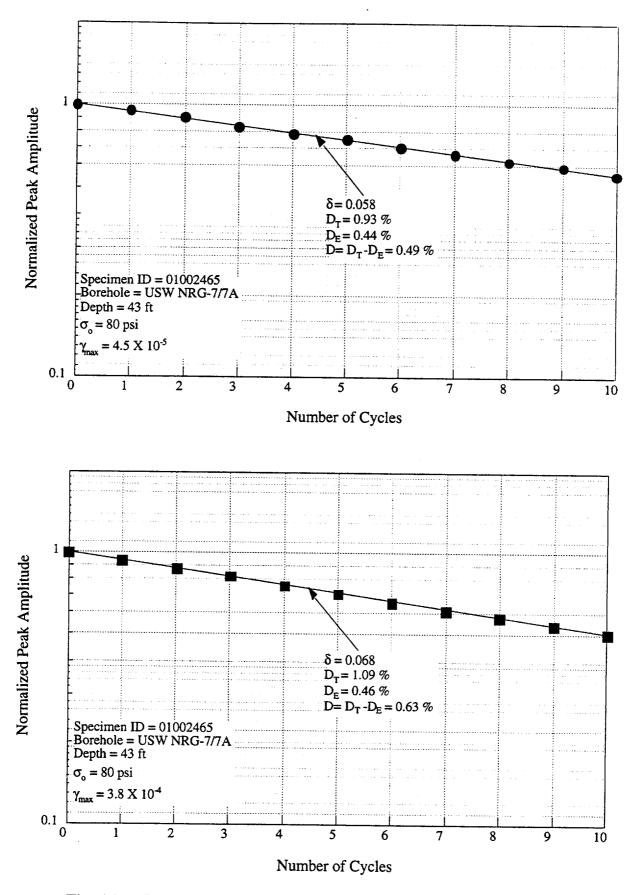


Fig. 14 Determination of Material Damping Ratio from Free-Vibration Decay Curves

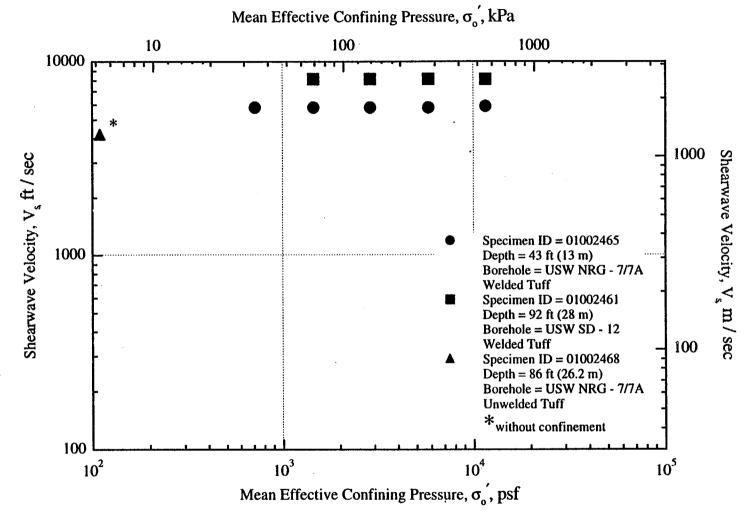


Fig. 19 Variation in Shearwave Velocity with Effective Confining Pressure from Resonant Column Tests of Intact Specimens from Yucca Mountain

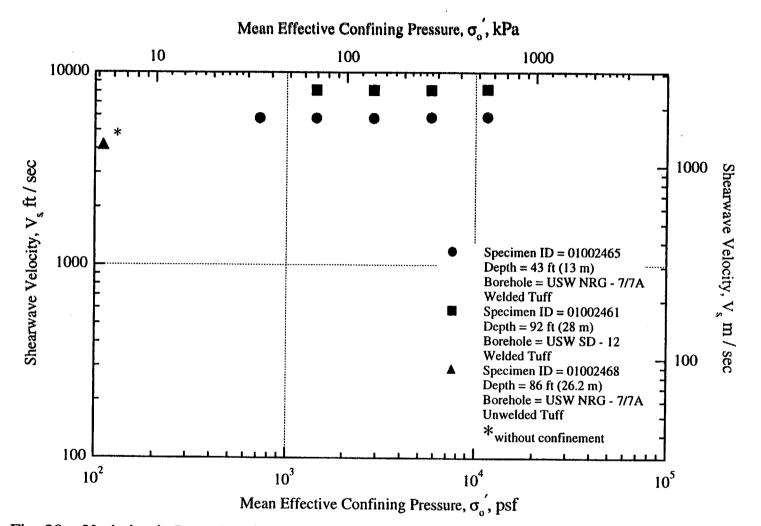


Fig. 20 Variation in Low-Amplitude Material Damping Ratio with Effective Confining Pressure from Resonant Column Tests of Intact Specimens from Yucca Mountain

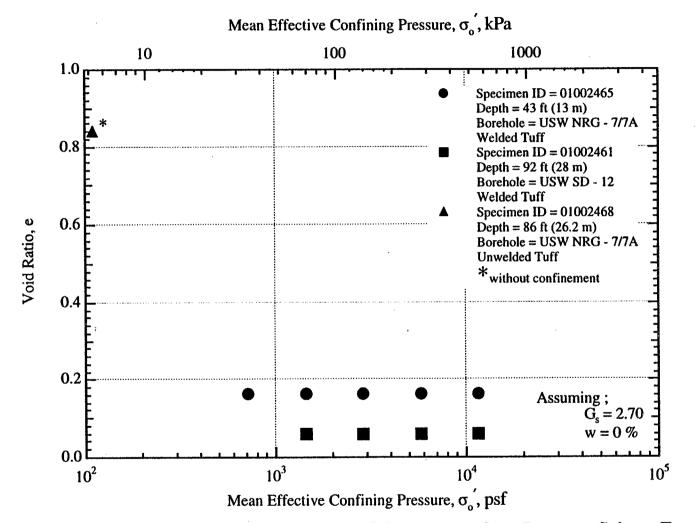


Fig. 21 Variation in Void Ratio with Effective Confining Pressure from Resonant Column Tests of Intact Specimens from Yucca Mountain

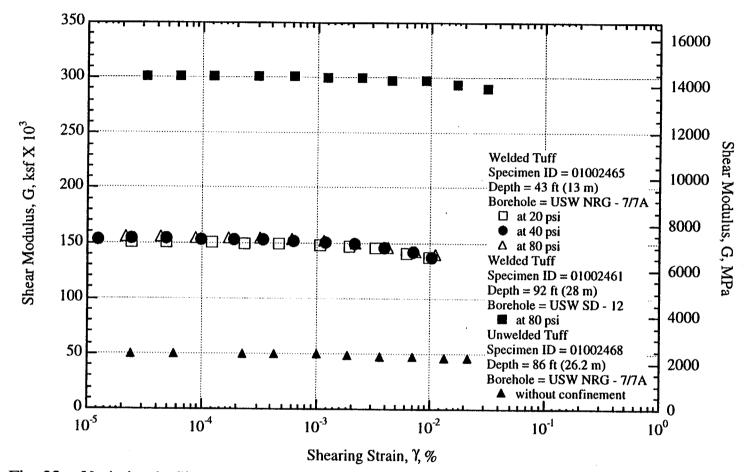


Fig. 22 Variation in Shear Modulus with Shearing Strain from Resonant Column and Torsional Shear Tests of Intact Specimens from Yucca Mountain

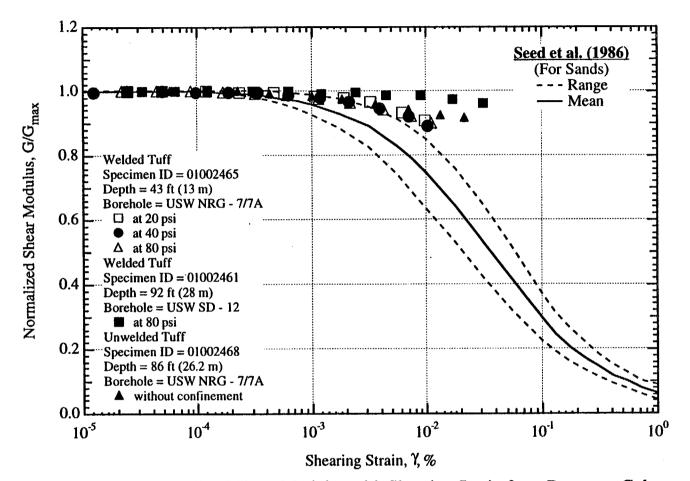


Fig. 23 Variation in Normalized Shear Modulus with Shearing Strain from Resonant Column Tests of Intact Specimens from Yucca Mountain

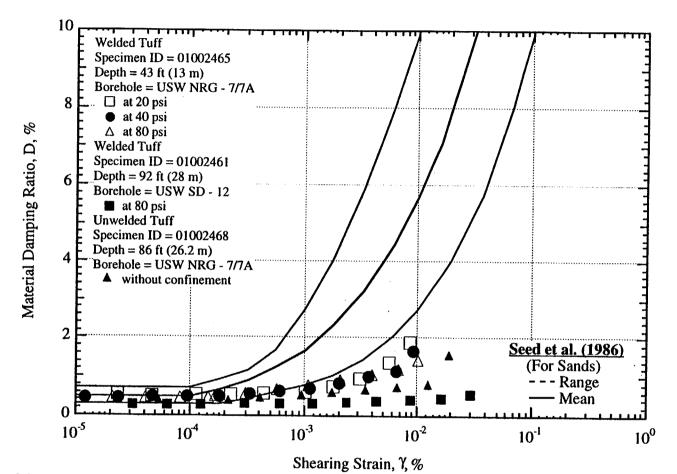


Fig. 24 Variation in Material Damping Ratio with Shearing Strain from Resonant Column Tests of Intact Specimens from Yucca Mountain

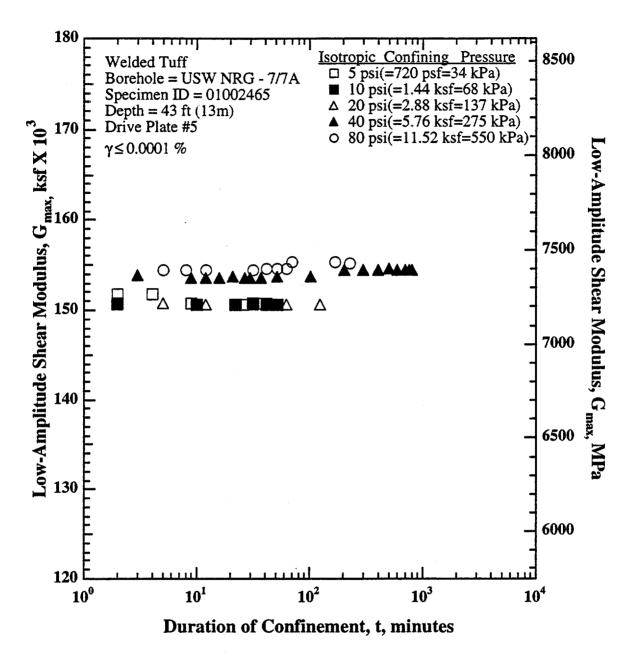


Fig. A.1 Variation in Low-Amplitude Shear Modulus with Magnitude and Duration of Isotropic Confining Pressure from Resonant Column Testing of Specimen 01002465 from Borehole USW NRG - 7/7A; Depth = 43 ft (13 m)

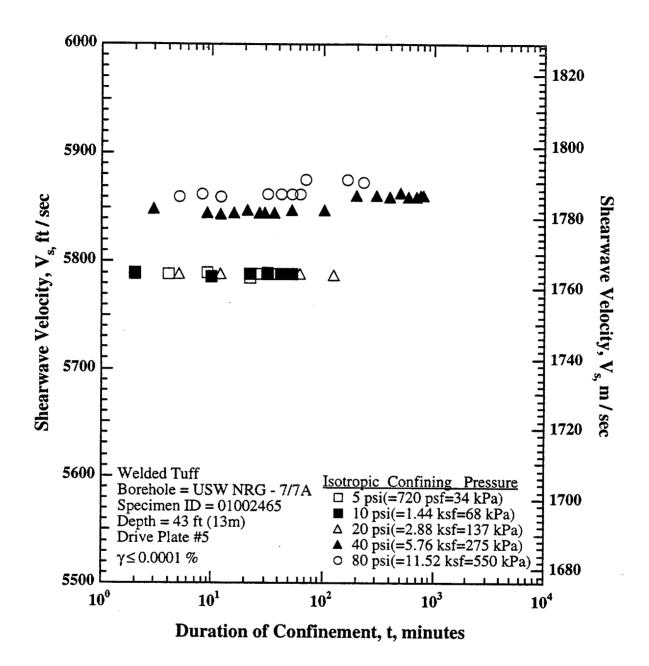


Fig. A.2 Variation in Shear Wave Velocity with Magnitude and Duration of Isotropic Confining Pressure from Resonant Column Testing of Specimen 01002465 from Borehole USW NRG - 7/7A; Depth = 43 ft (13 m)

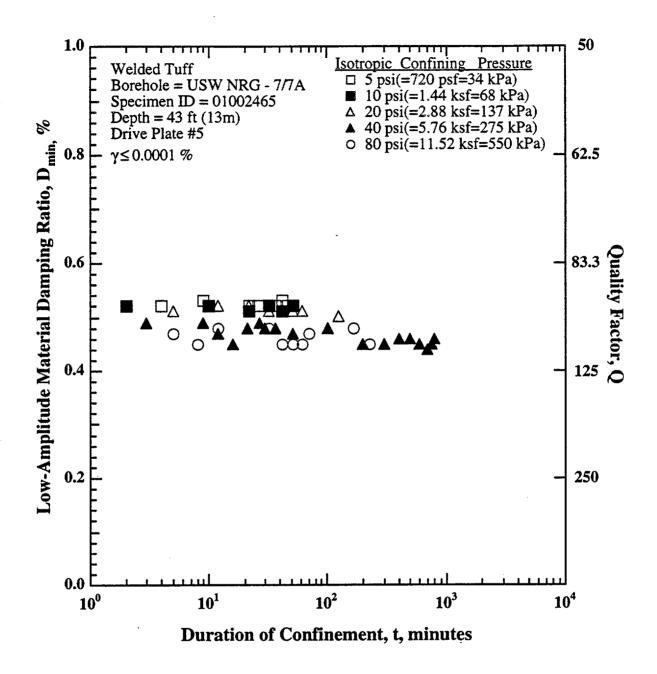


Fig. A.3 Variation in Low-Amplitude Material Damping Ratio with Magnitude and Duration of Isotropic Confining Pressure from Resonant Column Testing of Specimen 01002465 from Borehole USW NRG - 7/7A; Depth = 43 ft (13 m)

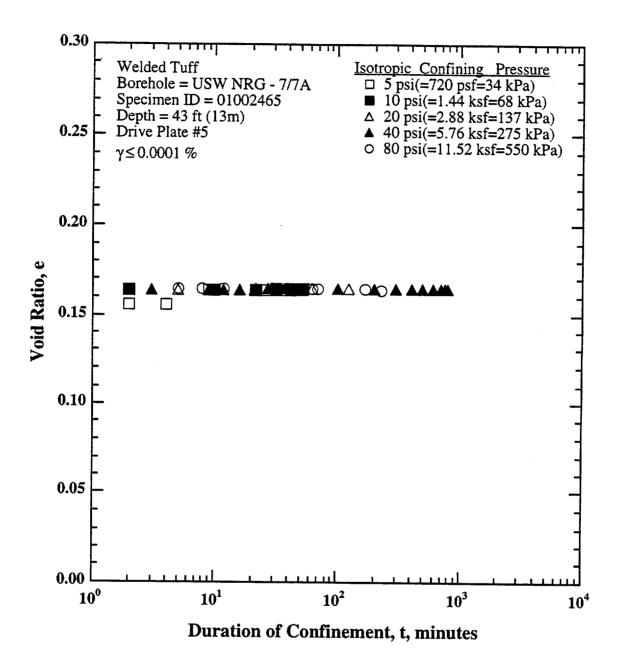


Fig. A.4 Variation in Void Ratio with Magnitude and Duration of Isotropic Confining Pressure from Resonant Column Testing of Specimen 01002465 from Borehole USW NRG - 7/7A; Depth = 43 ft (13 m)

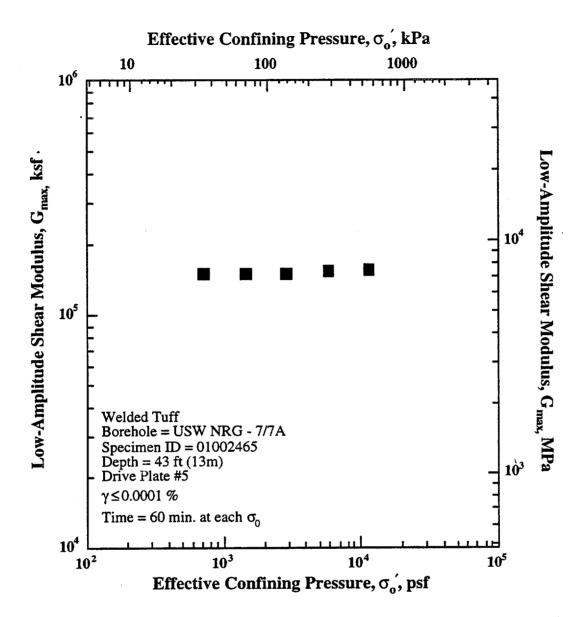


Fig. A.5 Variation in Low-Amplitude Shear Modulus with Effective Confining Pressure from Resonant Column Testing of Specimen 01002465 from Borehole USW NRG - 7/7A; Depth = 43 ft (13 m)

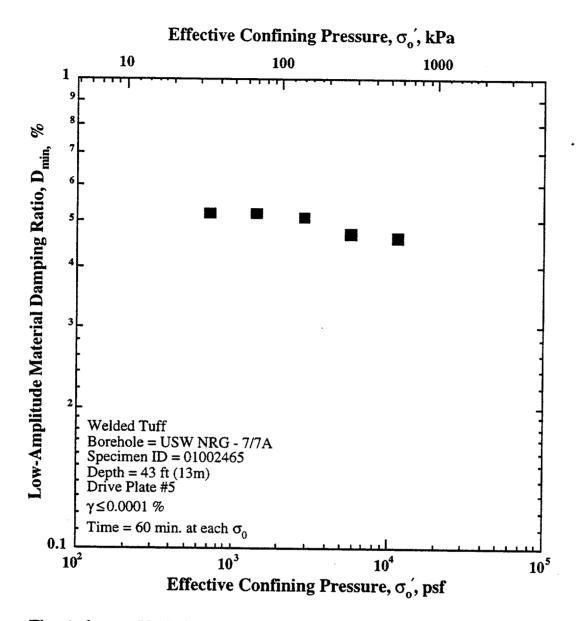


Fig. A.6 Variation in Low-Amplitude Material Damping Ratio with Effective Confining Pressure from Resonant Column Testing of Specimen 01002465 from Borehole USW NRG - 7/7A; Depth = 43 ft (13 m)

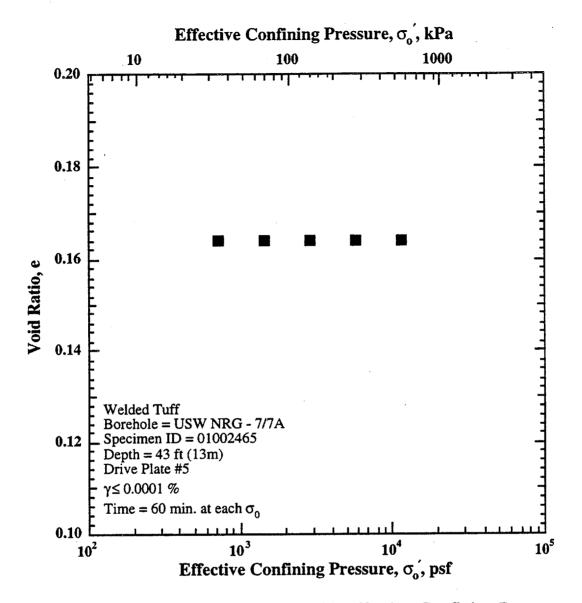


Fig. A.7 Variation in Void Ratio with Effective Confining Pressure from Resonant Column Testing of Specimen 01002465 from Borehole USW NRG - 7/7A; Depth = 43 ft (13 m)

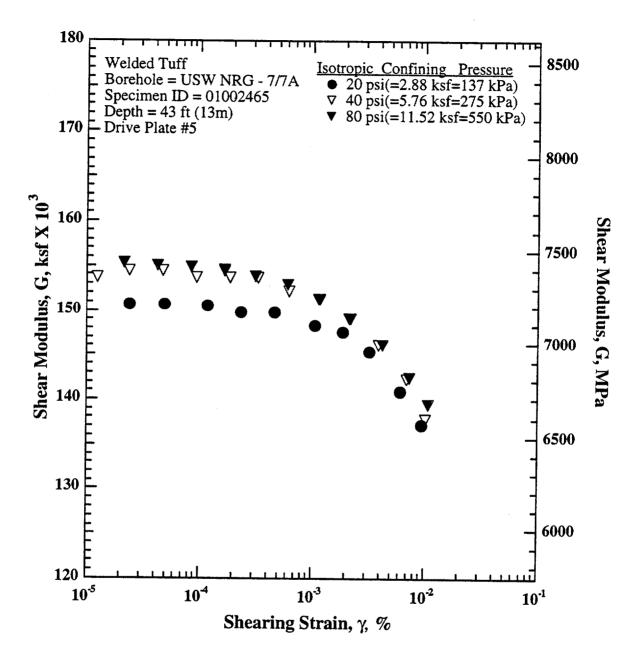


Fig. A.8 Variation in Shear Modulus with Shearing Strain and Effective Confining Pressure from Resonant Column Testing of Specimen 01002465 from Borehole USW NRG - 7/7A; Depth = 43 ft (13 m)

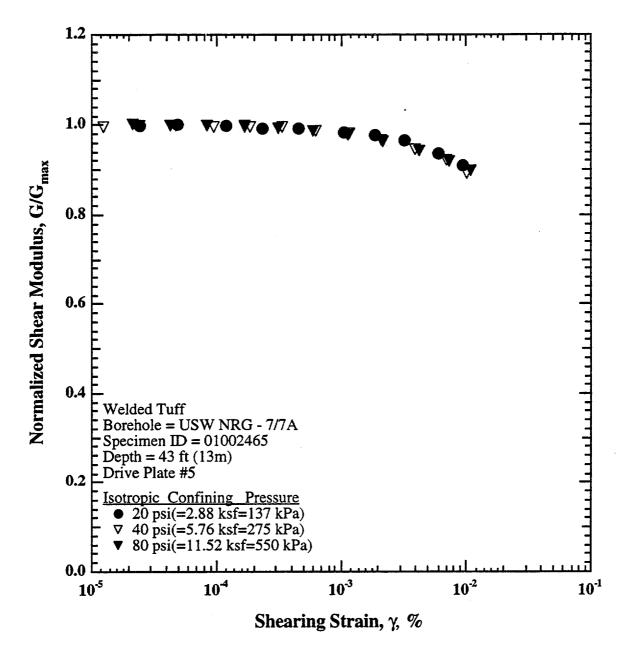


Fig. A.9 Variation in Normalized Shear Modulus with Shearing Strain and Effective Confining Pressure from Resonant Column Testing of Specimen 01002465 from Borehole USW NRG - 7/7A; Depth = 43 ft (13 m)

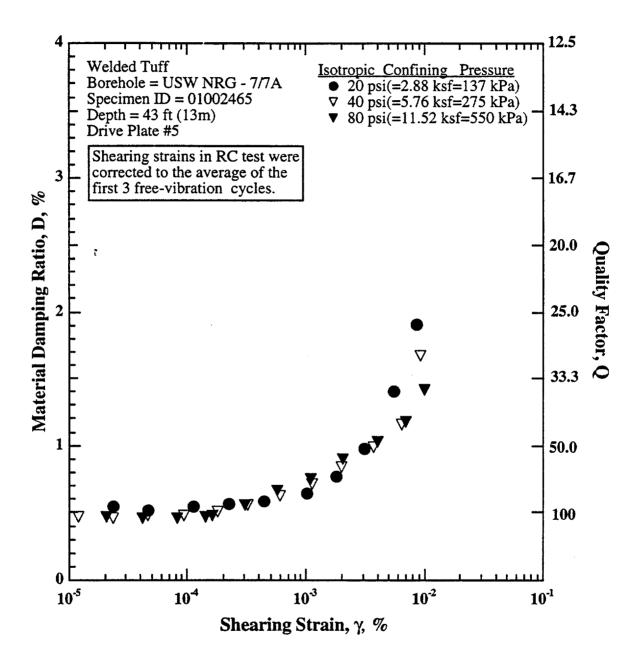


Fig. A.10 Variation in Material Damping Ratio with Shearing Strain and Effective Confining Pressure from Resonant Column Testing of Specimen 01002465 from Borehole USW NRG - 7/7A; Depth = 43 ft (13 m)

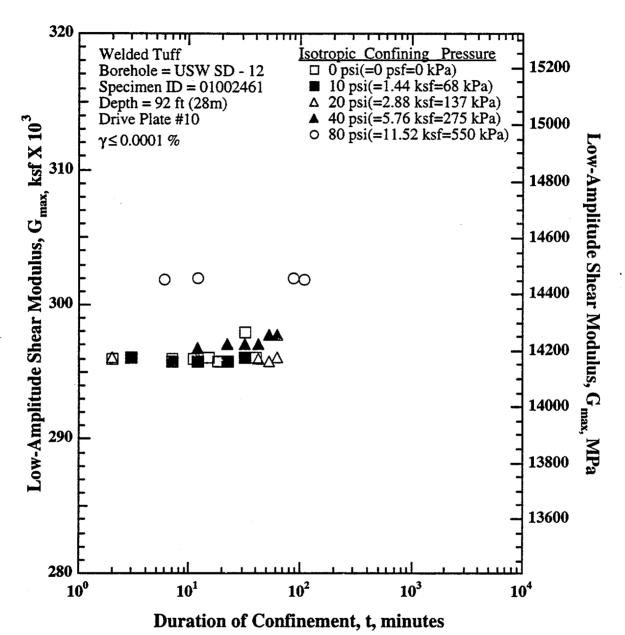


Fig. B.1 Variation in Low-Amplitude Shear Modulus with Magnitude

and Duration of Isotropic Confining Pressure from Resonant Column Testing of Specimen 01002461 from Borehole USW SD - 12; Depth = 92 ft (28 m)

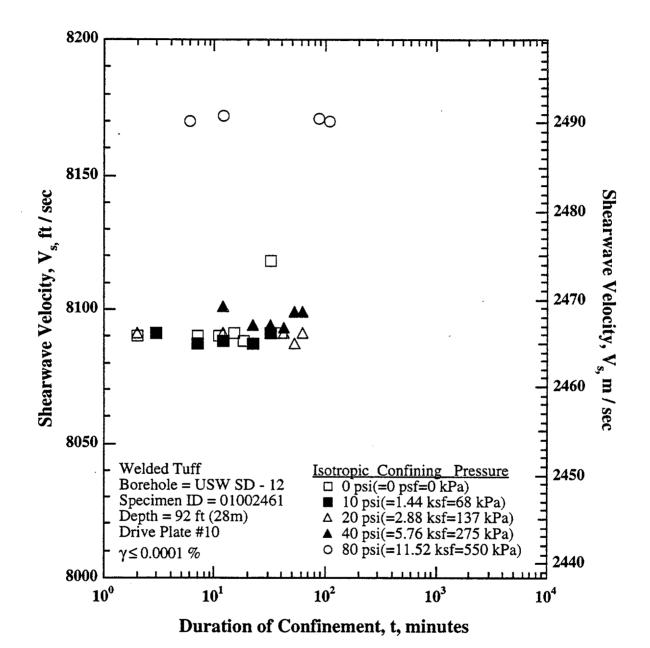


Fig. B.2 Variation in Shear Wave Velocity with Magnitude and Duration of Isotropic Confining Pressure from Resonant Column Testing of Specimen 01002461 from Borehole USW SD - 12; Depth = 92 ft (28 m)

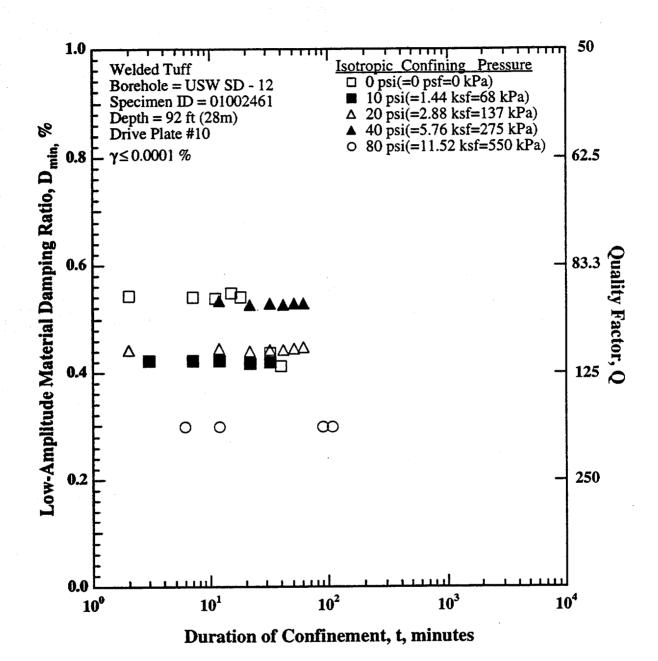


Fig. B.3 Variation in Low-Amplitude Material Damping Ratio with Magnitude and Duration of Isotropic Confining Pressure from Resonant Column Testing of Specimen 01002461 from Borehole USW SD - 12; Depth = 92 ft (28 m)

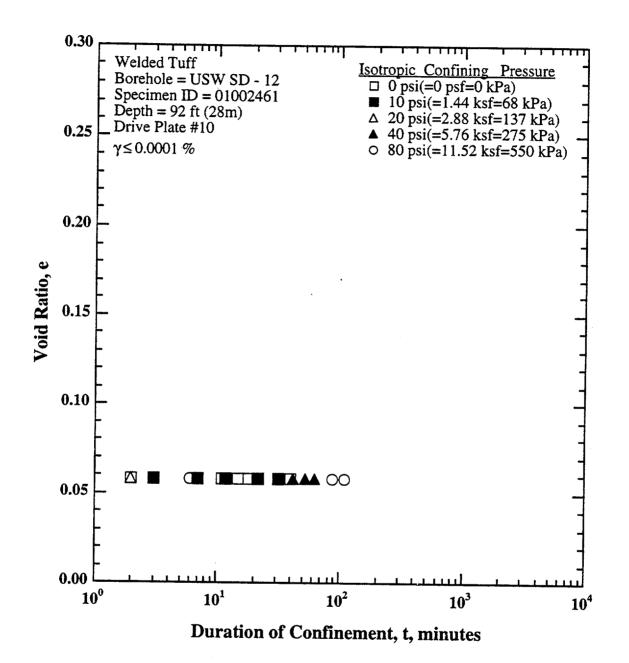
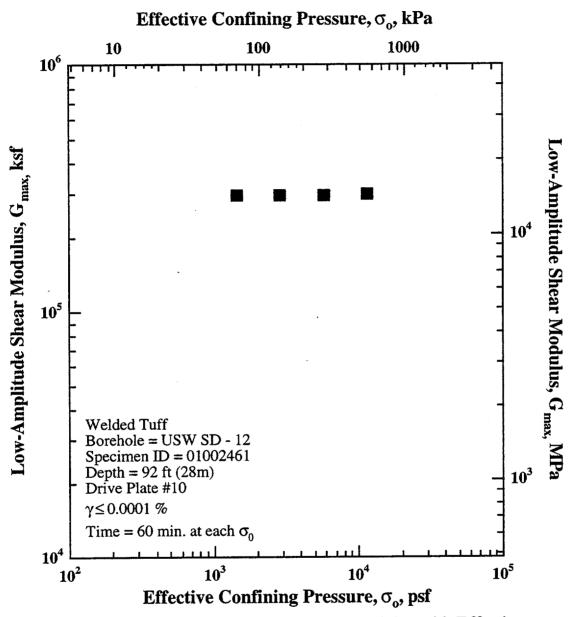
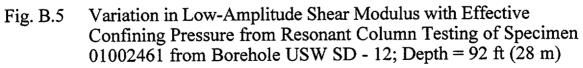


Fig. B.4 Variation in Void Ratio with Magnitude and Duration of Isotropic Confining Pressure from Resonant Column Testing of Specimen 01002461 from Borehole USW SD - 12; Depth = 92 ft (28 m)





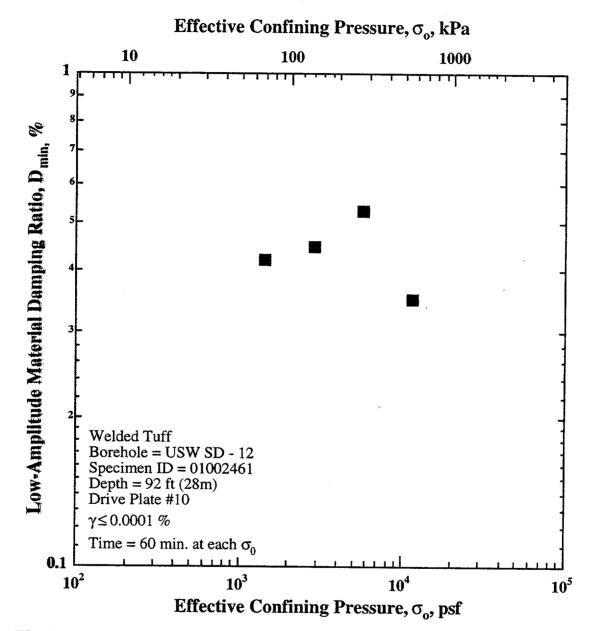


Fig. B.6 Variation in Low-Amplitude Material Damping Ratio with Effective Confining Pressure from Resonant Column Testing of Specimen 01002461 from Borehole USW SD - 12; Depth = 92 ft (28 m)

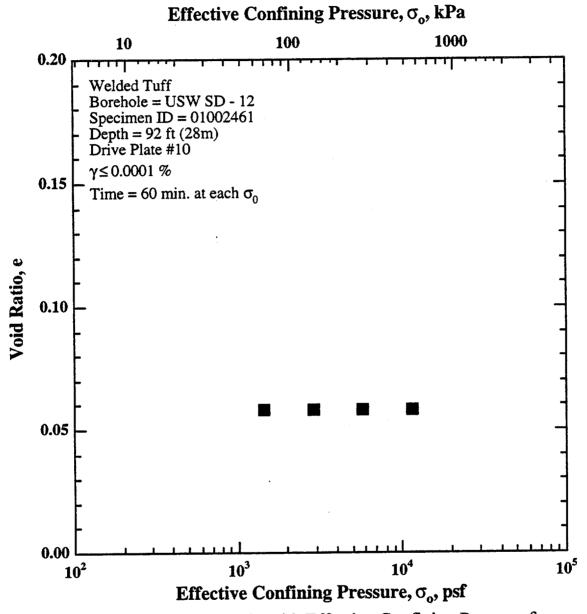


Fig. B.7 Variation in Void Ratio with Effective Confining Pressure from Resonant Column Testing of Specimen 01002461 from Borehole USW SD - 12; Depth = 92 ft (28 m)

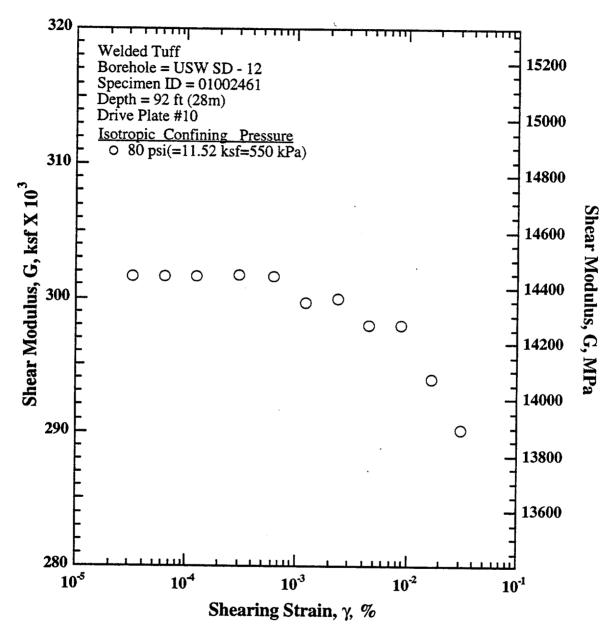
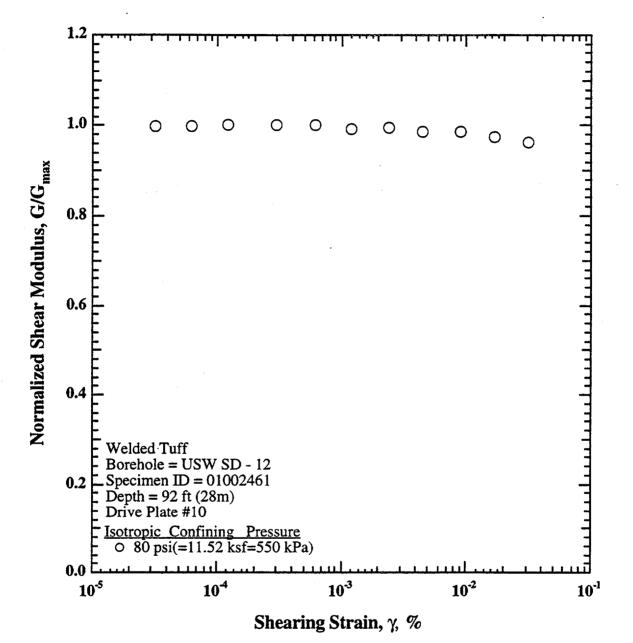
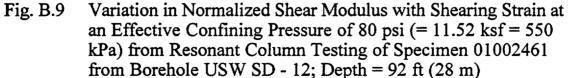


Fig. B.8 Variation in Shear Modulus with Shearing Strain at an Effective Confining Pressure of 80 psi (= 11.52 ksf = 550 kPa) from Resonant Column Testing of Specimen 01002461 from Borehole USW SD - 12; Depth = 92 ft (28 m)





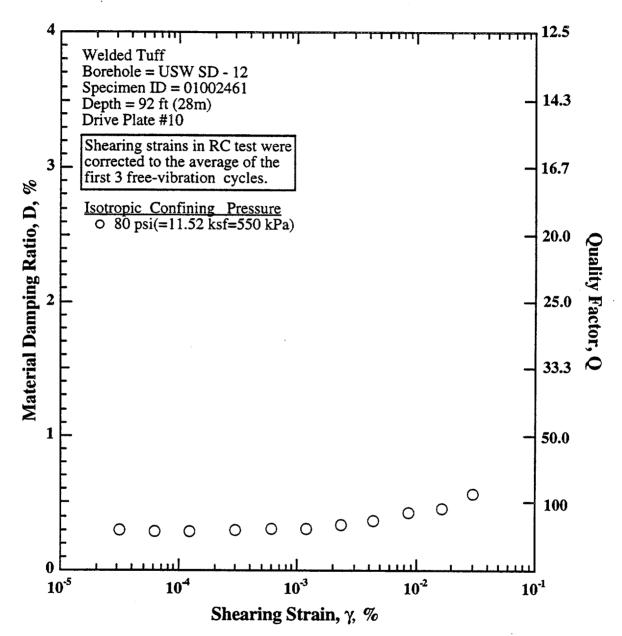


Fig. B.10 Variation in Material Damping Ratio with Shearing Strain at an Effective Confining Pressure of 80 psi (= 11.52 ksf = 550 kPa) from Resonant Column Testing of Specimen 01002461 from Borehole USW SD - 12; Depth = 43 ft (28 m)

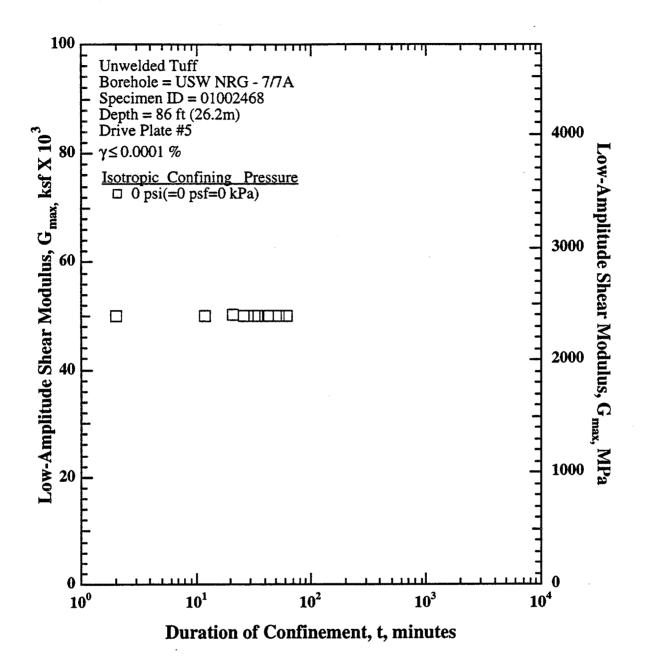


Fig. C.1 Variation in Low-Amplitude Shear Modulus with Magnitude and Duration of Isotropic Confining Pressure from Resonant Column Testing of Specimen 01002468 from Borehole USW NRG - 7/7A; Depth = 86 ft (26.2 m)

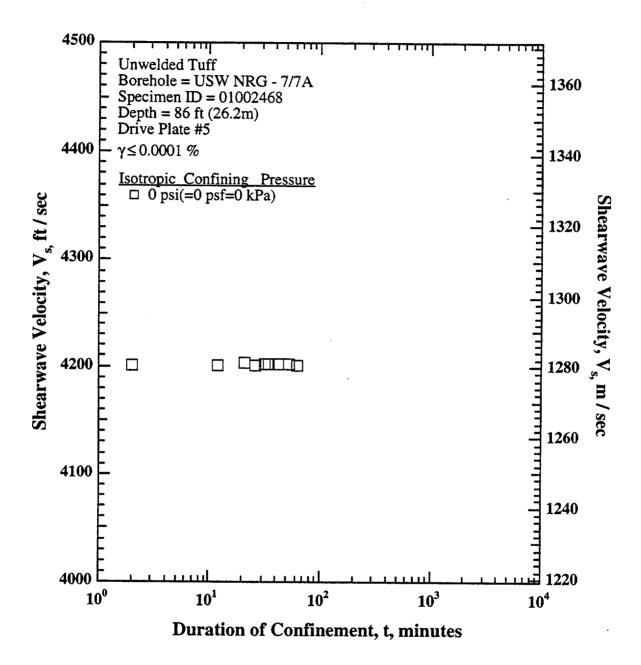


Fig. C.2 Variation in Shear Wave Velocity with Magnitude and Duration of Isotropic Confining Pressure from Resonant Column Testing of Specimen 01002468 from Borehole USW NRG - 7/7A; Depth = 86 ft (26.2 m)

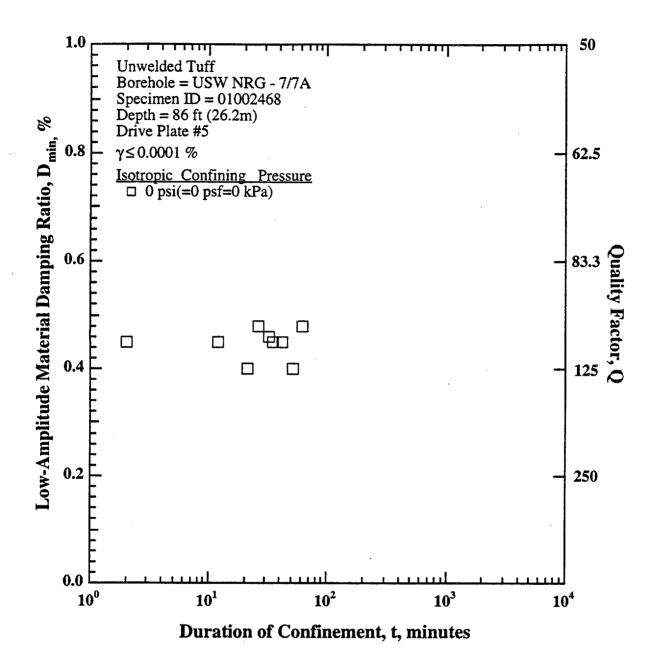


Fig. C.3 Variation in Low-Amplitude Material Damping Ratio with Magnitude and Duration of Isotropic Confining Pressure from Resonant Column Testing of Specimen 01002468 from Borehole USW NRG - 7/7A; Depth = 86 ft (26.2 m)

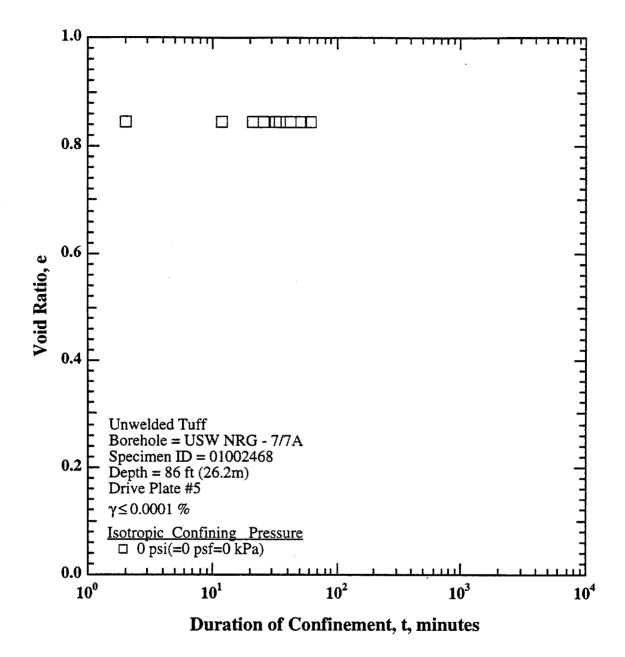


Fig. C.4 Variation in Void Ratio with Magnitude and Duration of Isotropic Confining Pressure from Resonant Column Testing of Specimen 01002468 from Borehole USW NRG - 7/7A; Depth = 86 ft (26.2 m)

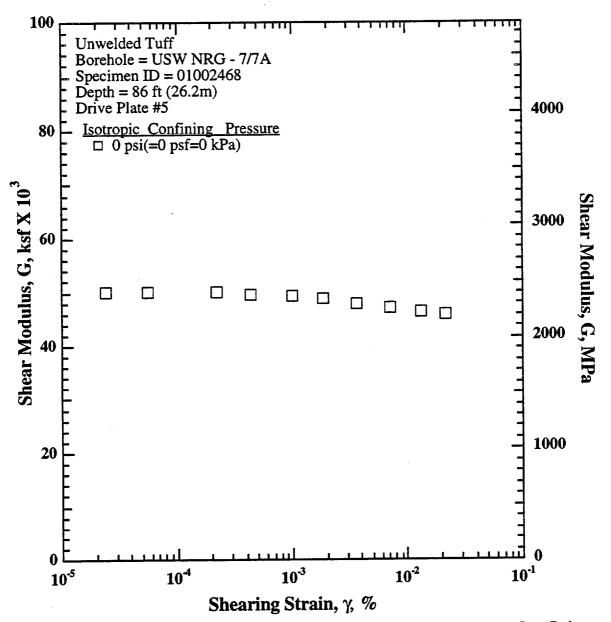


Fig. C.5 Variation in Shear Modulus with Shearing Strain at Zero Confining Pressure from Resonant Column Testing of Specimen 01002468 from Borehole USW NRG - 7/7A; Depth = 86 ft (26.2 m)

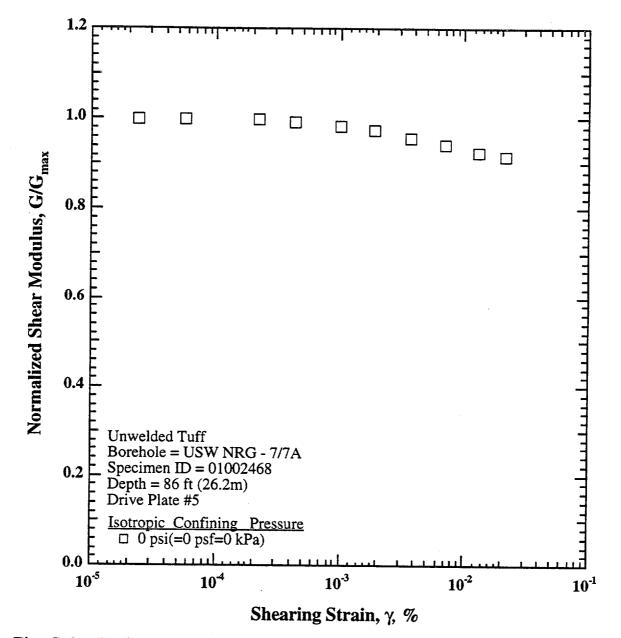


Fig. C.6 Variation in Normalized Shear Modulus with Shearing Strain at Zero Confining Pressure from Resonant Column Testing of Specimen 01002468 from Borehole USW NRG - 7/7A; Depth = 86 ft (26.2 m)

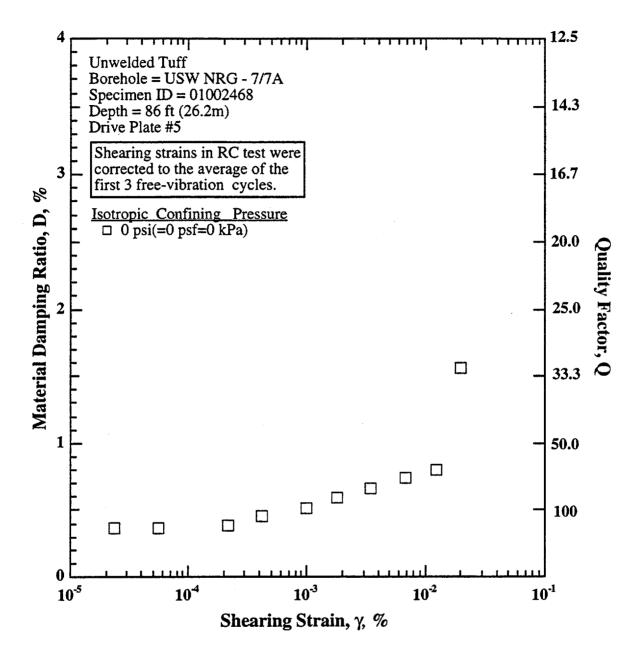


Fig. C.7 Variation in Material Damping Ratio with Shearing Strain at Zero Confining Pressure of from Resonant Column Testing of Specimen 01002468 from Borehole USW NRG - 7/7A; Depth = 86 ft (26.2 m)

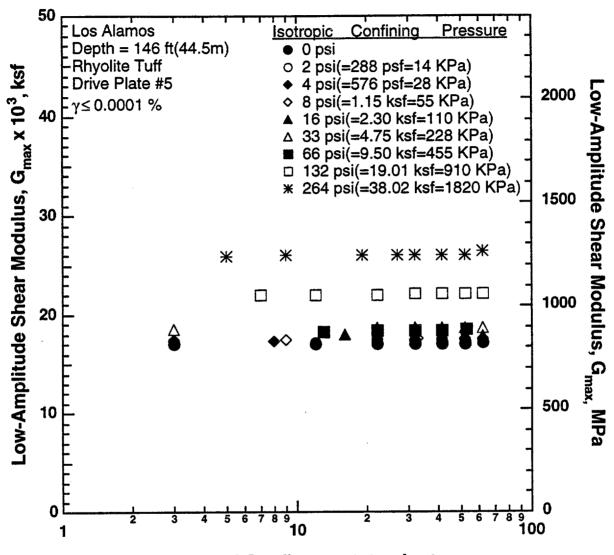




Fig. D.1 Variation in Low-Amplitude Shear Modulus with Magnitude and Duration of Isotropic Confining Pressure from Resonant Column Testing of Sample HQ30 from Borehole TA55

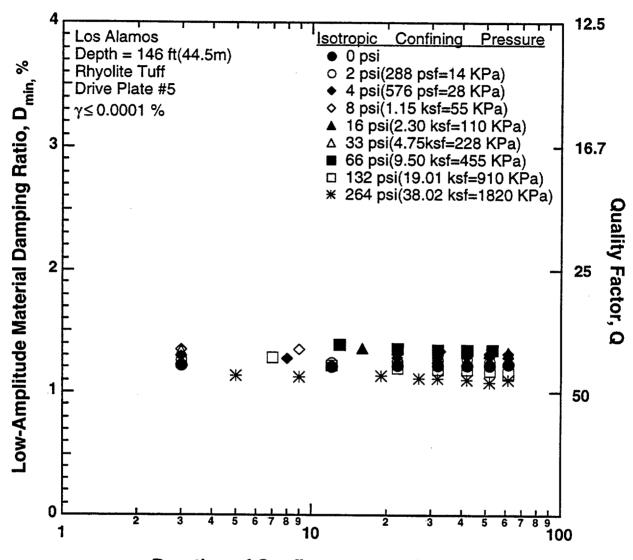




Fig. D.2 Variation in Low-Amplitude Material Damping Ratio with Magnitude and Duration of Isotropic Confining Pressure from Resonant Column Testing of Sample HQ30 from Borehole TA55

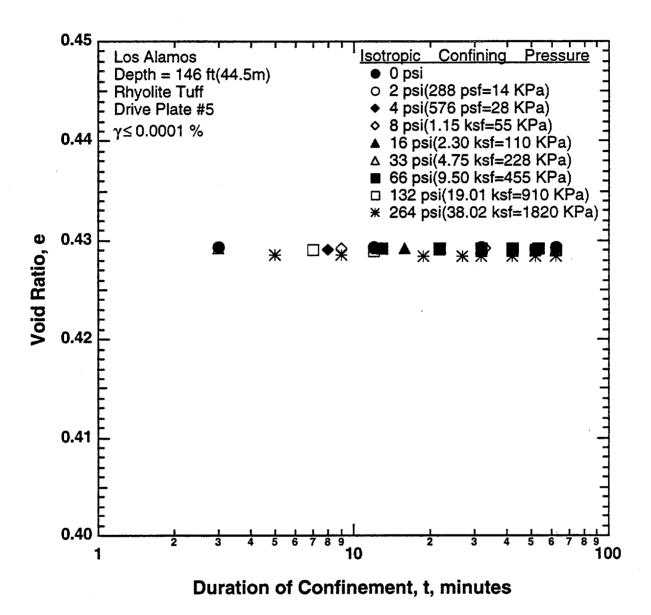


Fig. D.3 Variation in Void Ratio with Magnitude and Duration of Isotropic Confining Pressure from Resonant Column Testing of Sample HQ30 from Borehole TA55

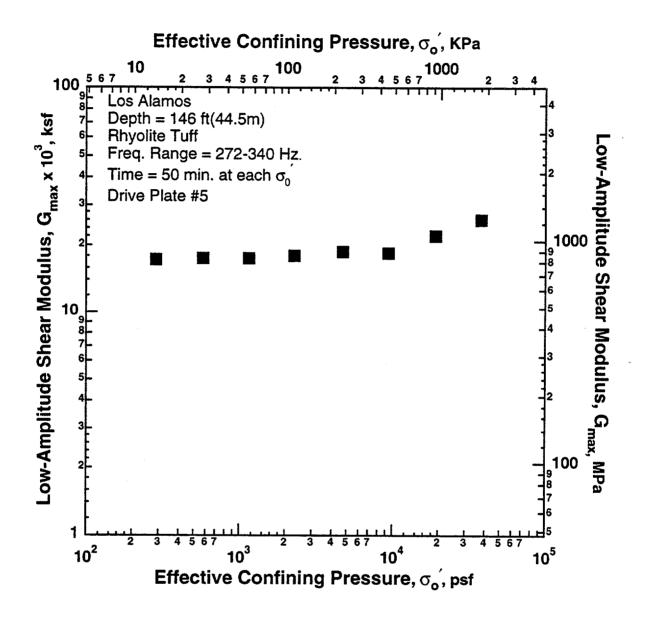


Fig. D.4 Variation in Low-Amplitude Shear Modulus with Effective Confining Pressure from Resonant Column Testing of Sample HQ30 from Borehole TA55

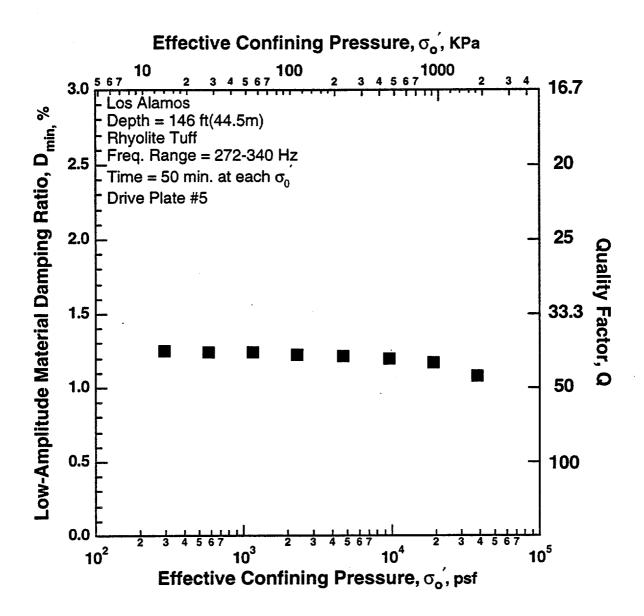


Fig. D.5 Variation in Low-Amplitude Material Damping Ratio with Effective Confining Pressure from Resonant Column Testing of Sample HQ30 from Borehole TA55

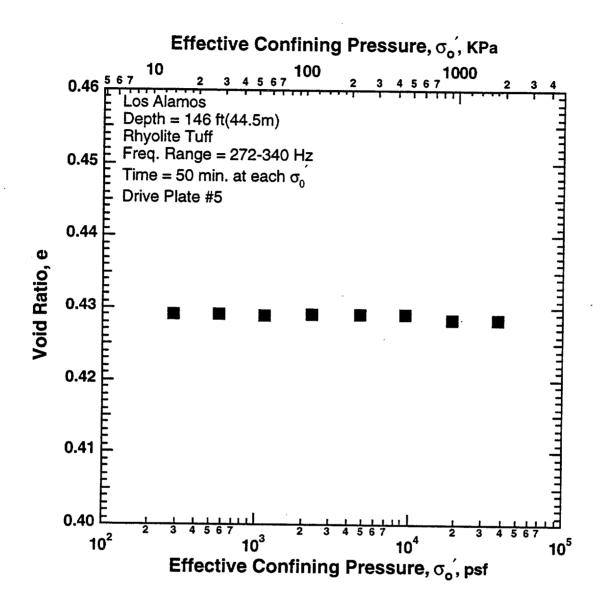


Fig. D.6 Variation in Void Ratio with Effective Confining Pressure from Resonant Column Testing of Sample HQ30 from Borehole TA55

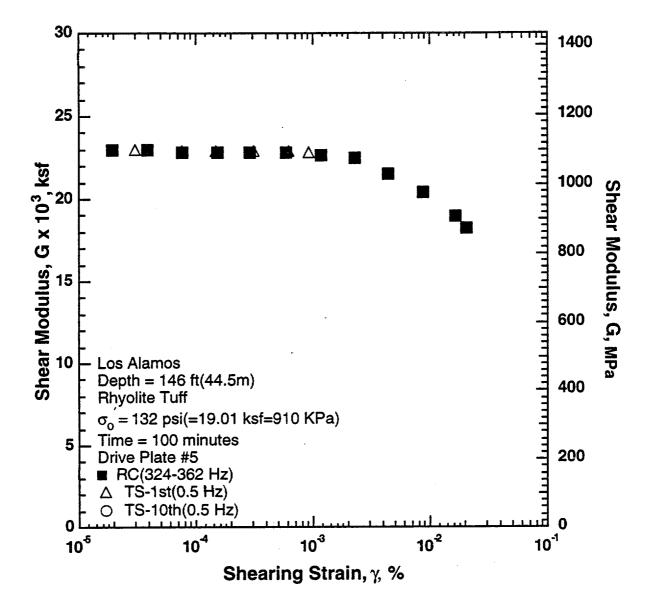


Fig. D.7 Variation in Shear Modulus with Shearing Strain at an Effective Confining Pressure of 132 psi (=19.01 ksf=910 KPa) from RCTS Tests of Sample HQ30 from Borehole TA55

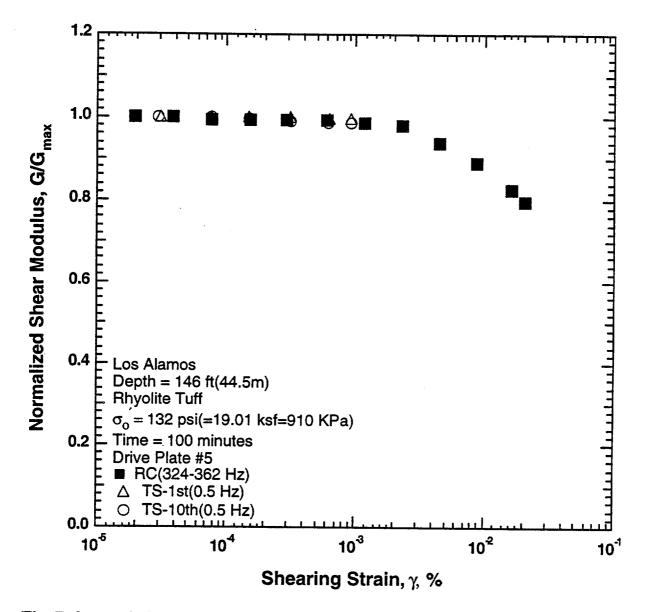


Fig. D.8 Variation in Normalized Shear Modulus with Shearing Strain at an Effective Confining Pressure of 132 psi (=19.01 ksf=910 KPa) from RCTS Tests of Sample HQ30 from Borehole TA55

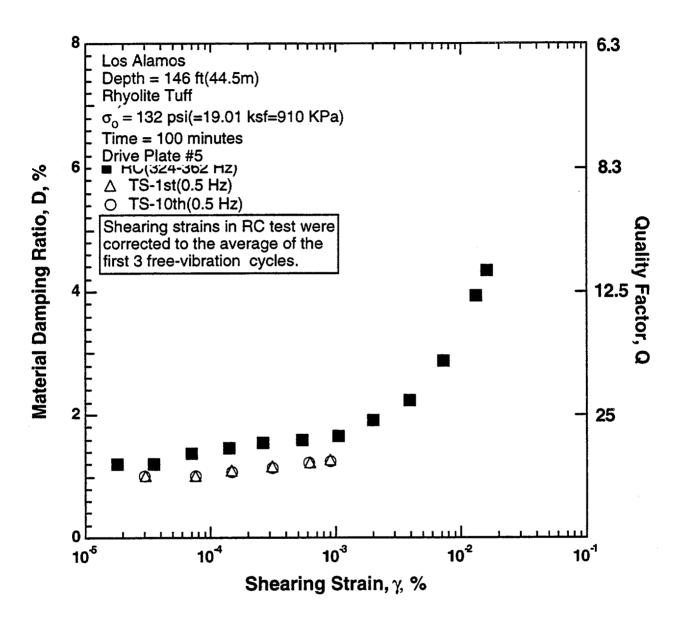


Fig. D.9 Variation in Material Damping Ratio with Shearing Strain at an Effective Confining Pressure of 132 psi (=19.01 ksf=910 KPa) from RCTS Tests of Sample HQ30 from Borehole TA55

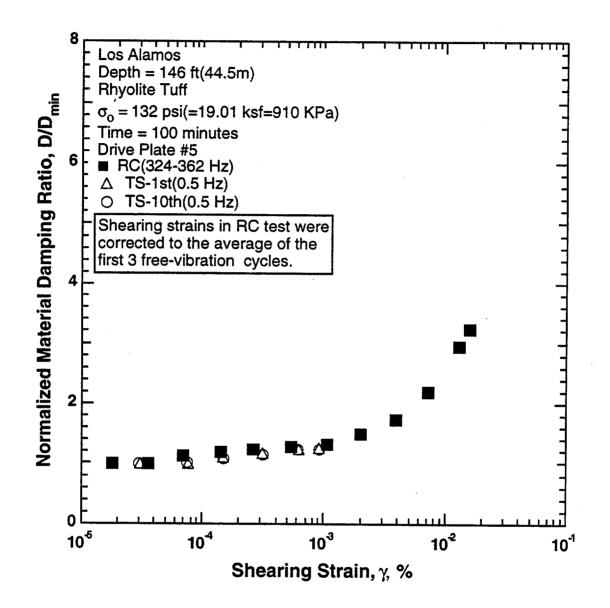


Fig. D.10 Variation in Normalized Material Damping Ratio with Shearing Strain at an Effective Confining Pressure of 132 psi(=19.01 ksf=910 KPa) from RCTS Tests of Sample HQ30 from Borehole TA55

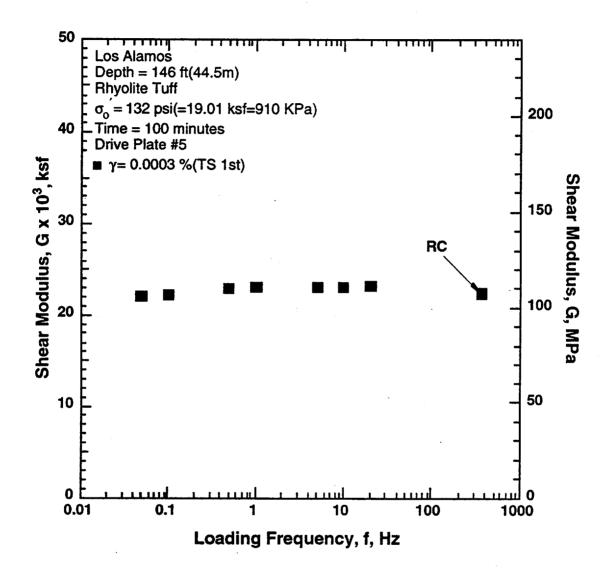


Fig. D.11 Variation in Shear Modulus with Loading Frequency and Shearing Strain at an Effective Confining Pressure of 132 psi(=19.01 ksf=910 KPa) from RCTS Tests of Sample HQ30 from Borehole TA55

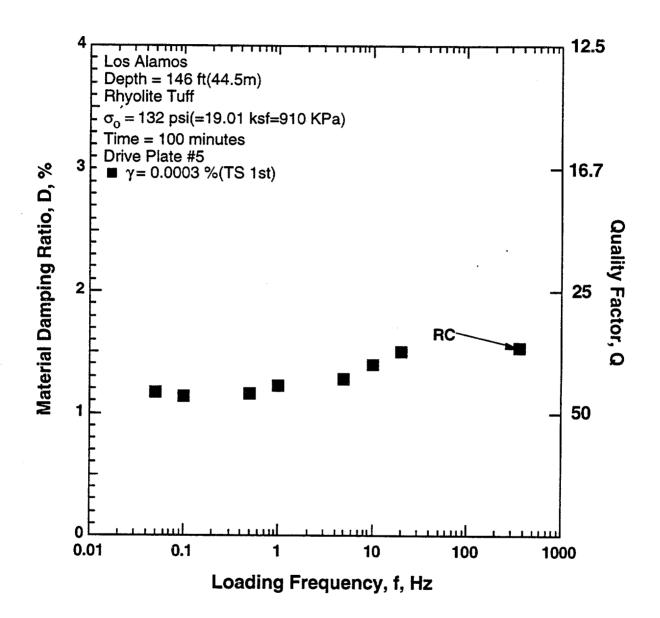


Fig. D.12 Variation in Material Damping Ratio with Loading Frequency and Shearing Strain at an Effective Confining Pressure of 132 psi(=19.01 ksf=910 Kpa) from RCTS Tests of Sample HQ30 from Borehole TA55

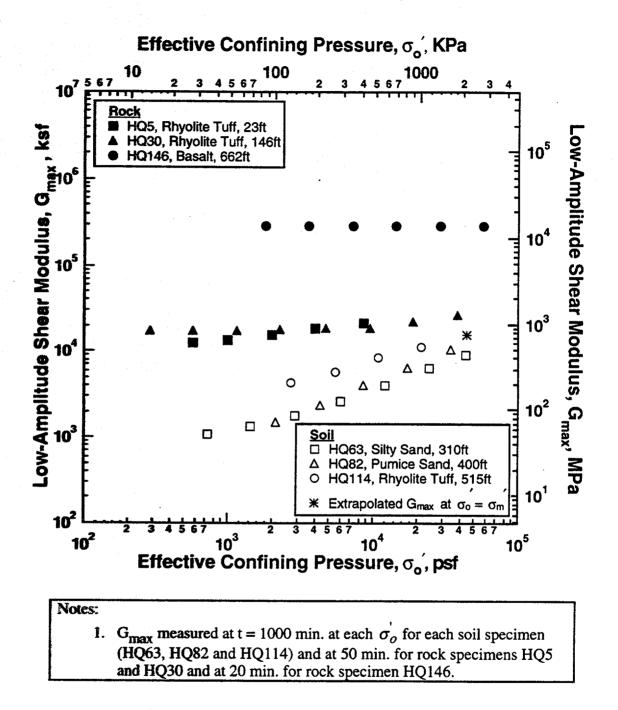


Fig. E.1 Variation in Low-Amplitude Shear Modulus with Effective Confining Pressure from Resonant Column Tests of Undisturbed Soil and Rock Samples from Los Alamos

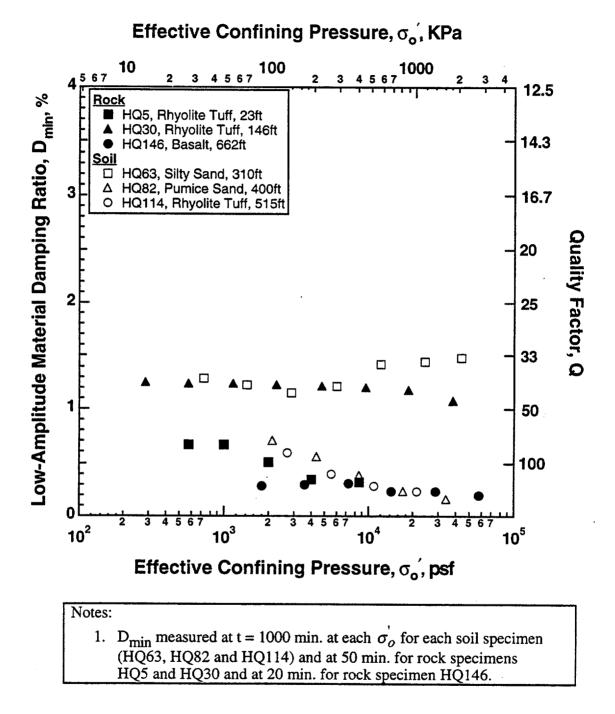


Fig. E.2 Variation in Low-Amplitude Material Damping Ratio with Effective Confining Pressure from Resonant Column Tests of Undisturbed Soil and Rock Samples from Los Alamos

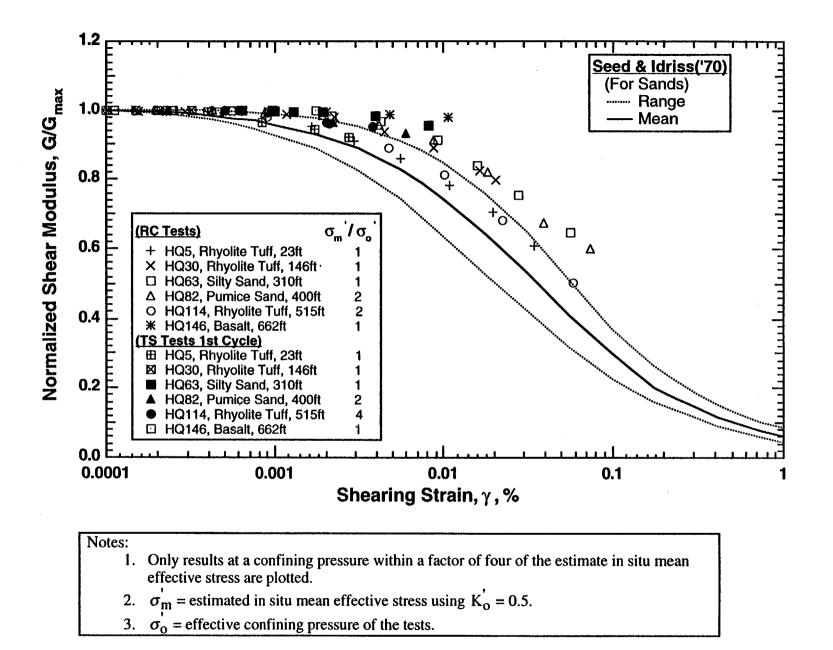
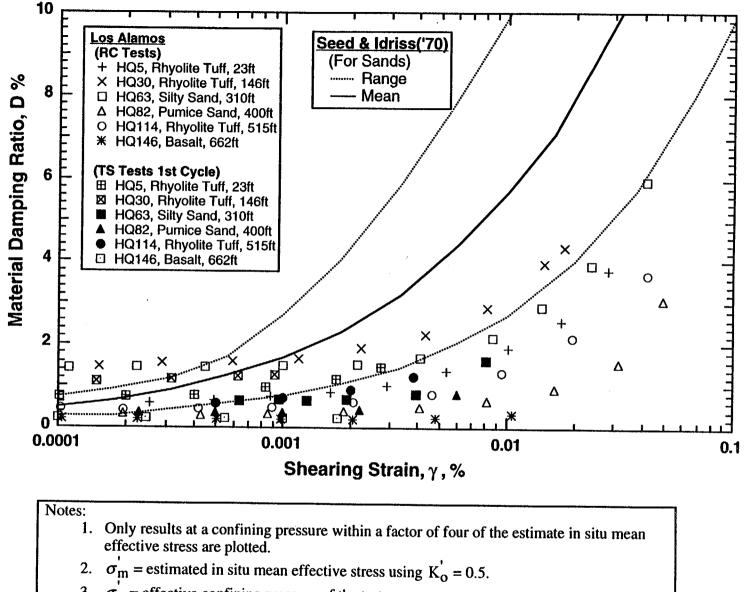


Fig. E.3 Variation in Normalized Shear Modulus with Shearing Strain from Resonant Column and Torsional Shear Tests of Undisturbed Samples from Los Alamos



- 3.  $\sigma'_0$  = effective confining pressure of the tests.
- 4. Shearing strains were corrected to the average of the first 3 free-vibration cycles.

Fig. E.4 Variation in Material Damping Ratio with Shearing Strain for g, 0.1 % from Resonant Column and Torsional Shear Tests of Undisturbed Soil and Rock Samples from Los Alamos

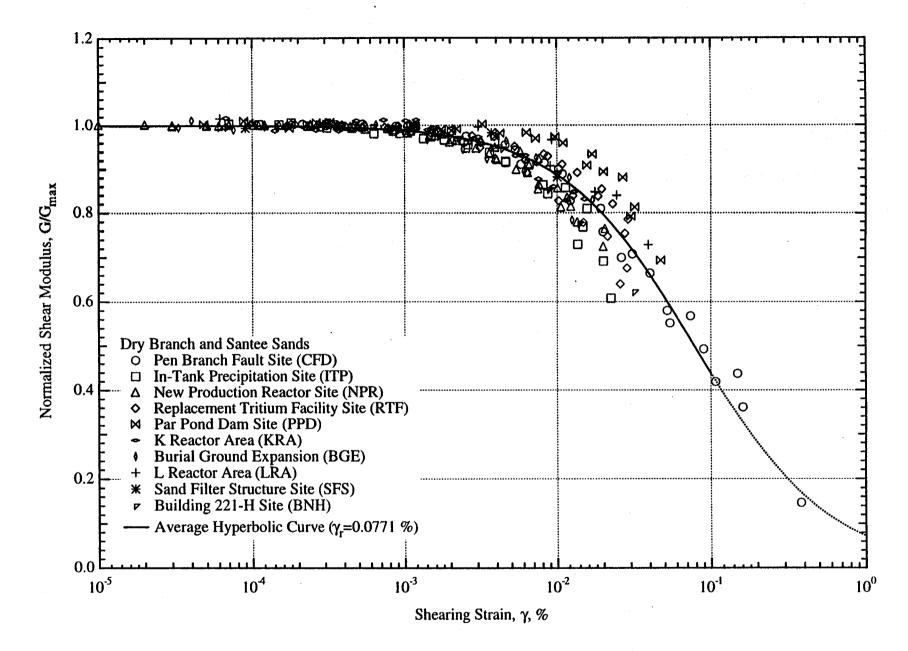


Fig. F.1 Summary Plot of All G/G<sub>max</sub> - log γ Relationships Determined by Resonant Column Testing with the Specimens Confined At or Near the In-Situ Mean Effective Stress for the Dry Branch and Santee Sands

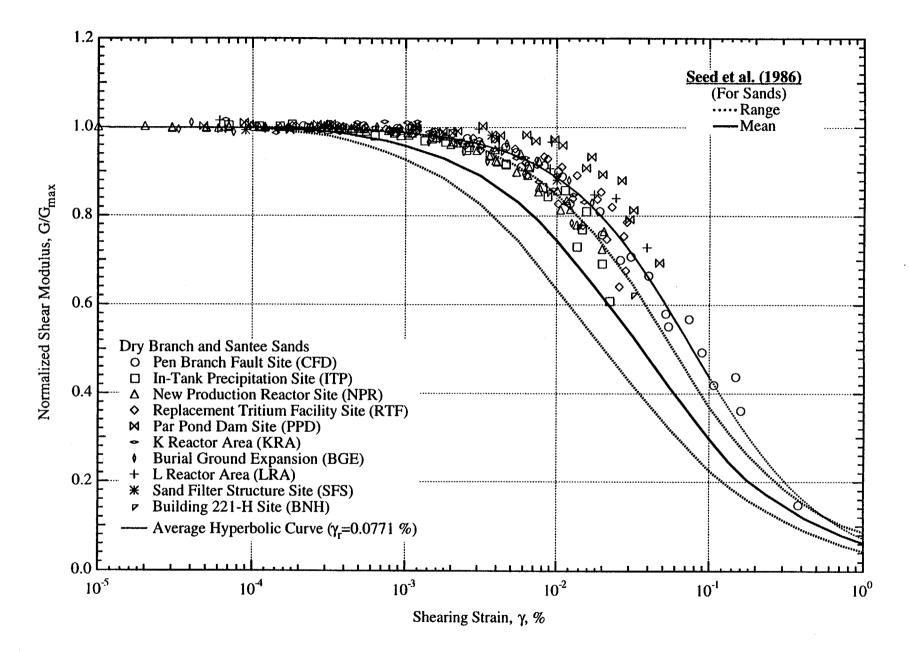


Fig. F.2 Comparison of the  $G/G_{max}$  - log  $\gamma$  Relationships Determined by Resonant Column Testing of Sands from the Dry Branch and Santee Formations with the Relationship Recommended by Seed et al. (1986) for Sands

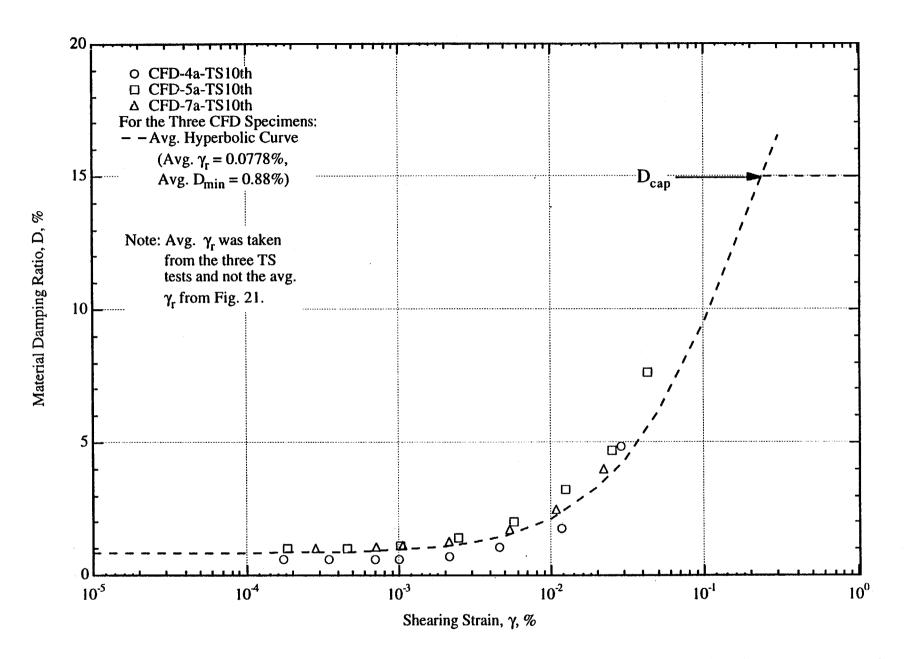


Fig. F.3 Comparison of the D -  $\log \gamma$  Relationships Measured in the Tenth Cycle of TS Testing with an Average Hyperbolic Relationship and Material Damping Cap for the Dry Branch and Santee Sands

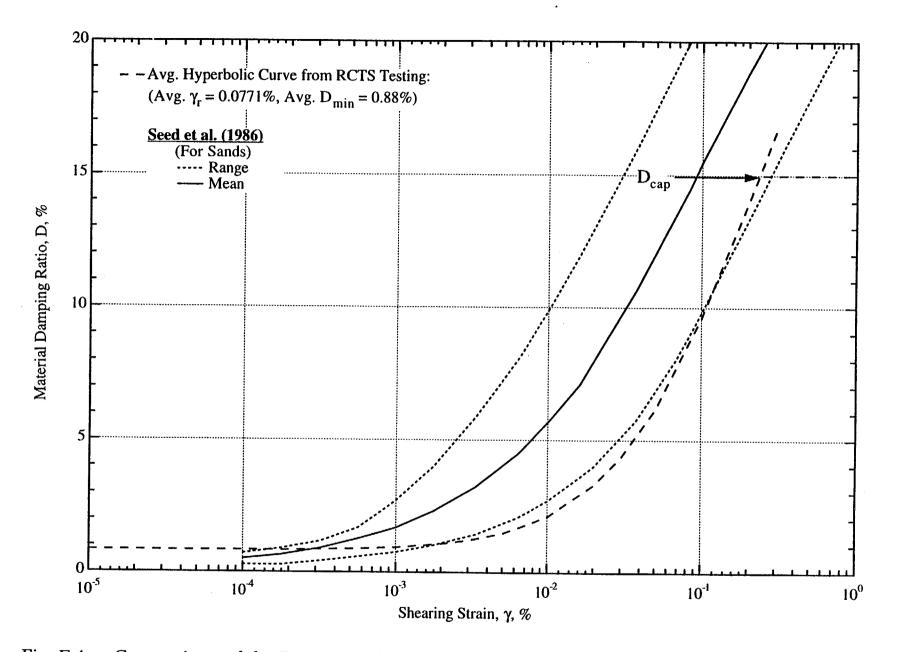


Fig. F.4 Comparison of the Recommended Average Hyperbolic D -  $\log \gamma$  Relationship for the Dry Branch and Santee Sands with the D-log  $\gamma$  Relationship Recommended by Seed et al. (1986) for Sands

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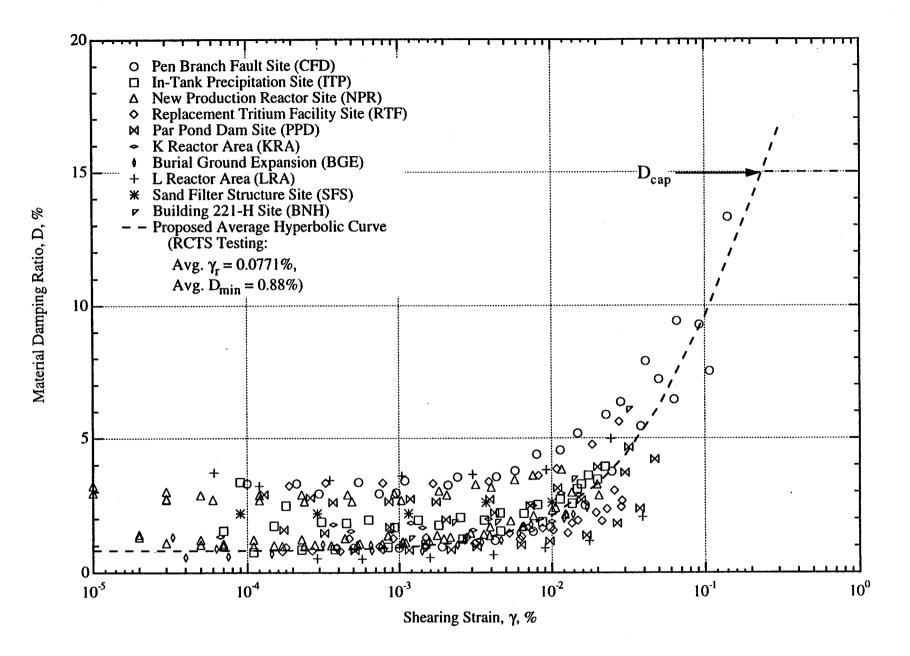


Fig. F.5 Comparison of the Recommended Average Hyperbolic D -  $\log \gamma$  Relationship Determined from RCTS Testing with the Resonant Column Results for the Dry Branch and Santee Sands

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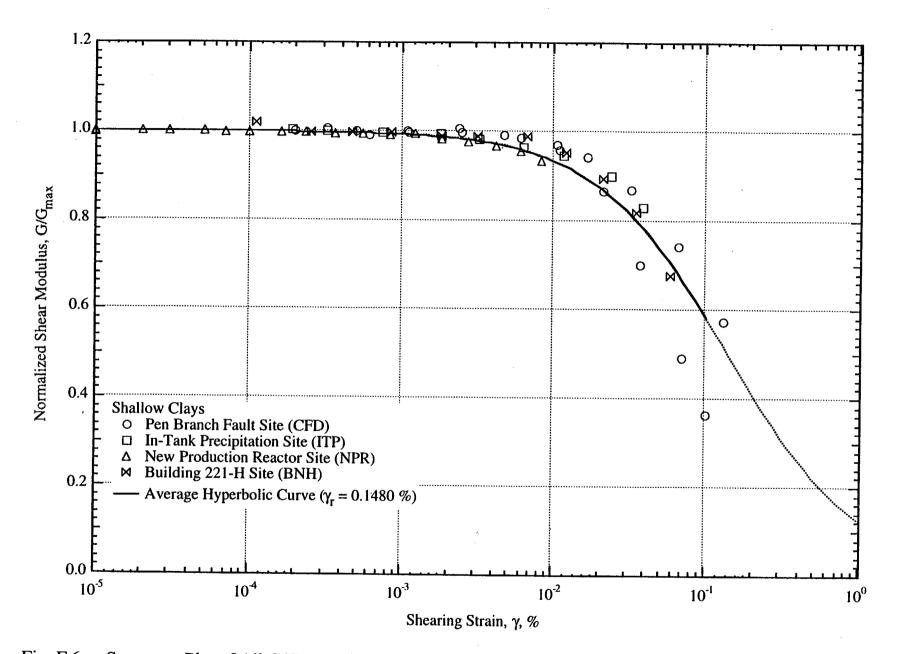


Fig. F.6 Summary Plot of All G/G<sub>max</sub> - log γ Relationships Determined by Resonant Column Testing with the Specimens Confined At or Near the In-Situ Mean Effective Stress for the Shallow Clays

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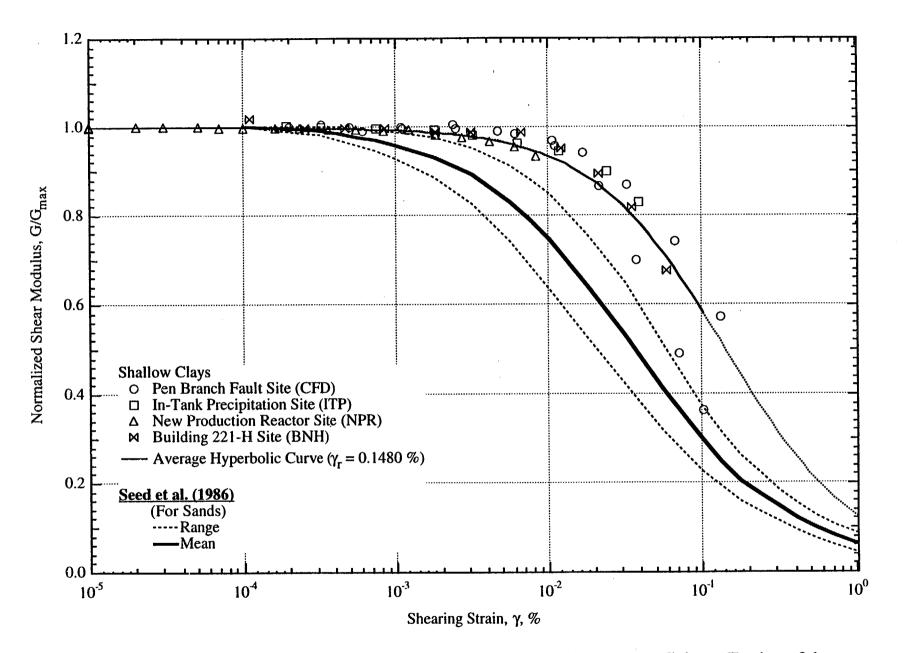


Fig. F.7 Comparison of the  $G/G_{max}$  - log  $\gamma$  Relationships Determined by Resonant Column Testing of the Shallow Clays with the Relationship Recommended by Seed et al. (1986) for Sands

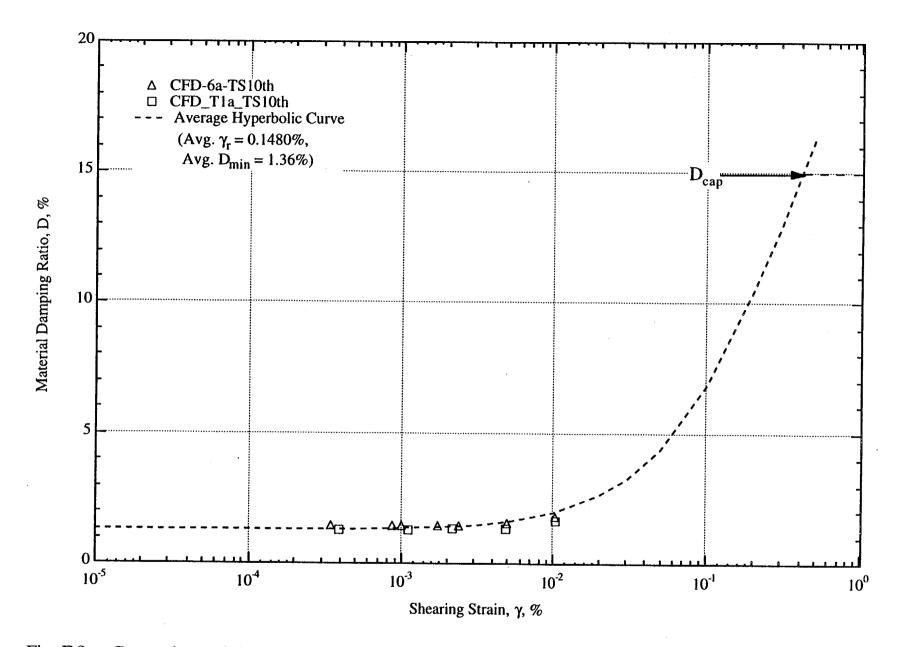


Fig. F.8 Comparison of the D - log γ Relationships Measured in the Tenth Cycle of TS Testing with the Recommended Average Hyperbolic Relationship and Material Damping Cap for the Shallow Clays

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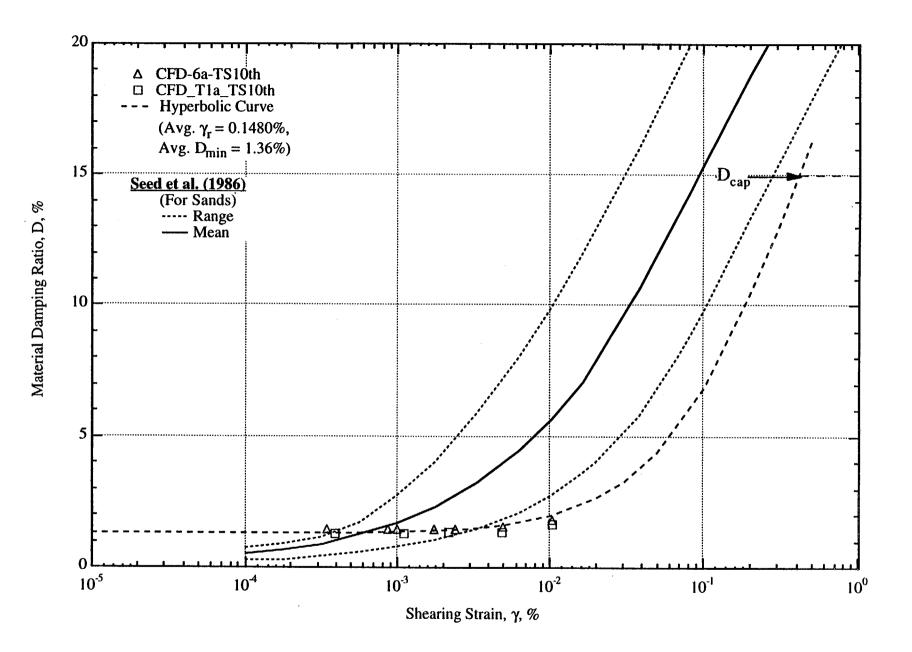


Fig. F.9 Comparison of the Recommended Average Hyperbolic D - log γ Relationship for the Shallow Clays with the Relationship Recommended by Seed et al. (1986) for Sands

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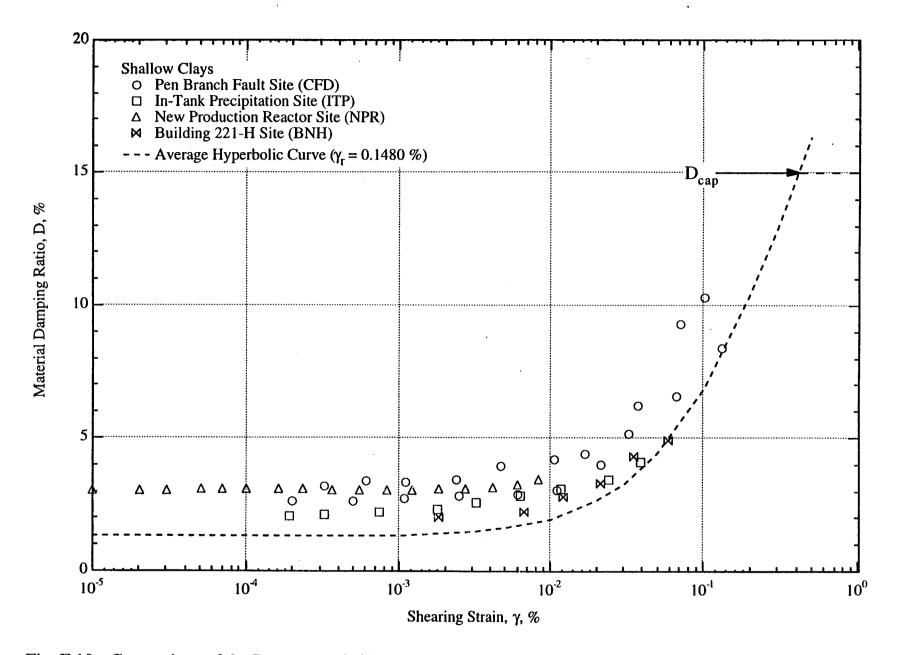


Fig. F.10 Comparison of the Recommended Average Hyperbolic D - log γ Relationship Determined from RCTS Testing with the Resonant Column Results for the Shallow Clays

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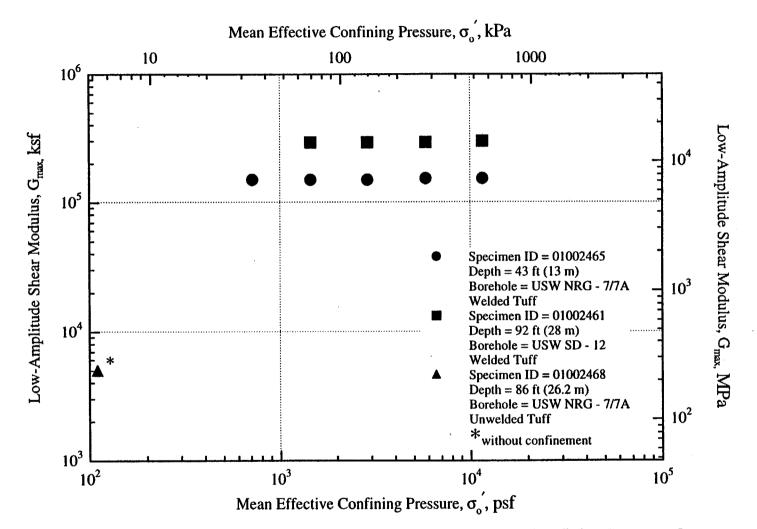
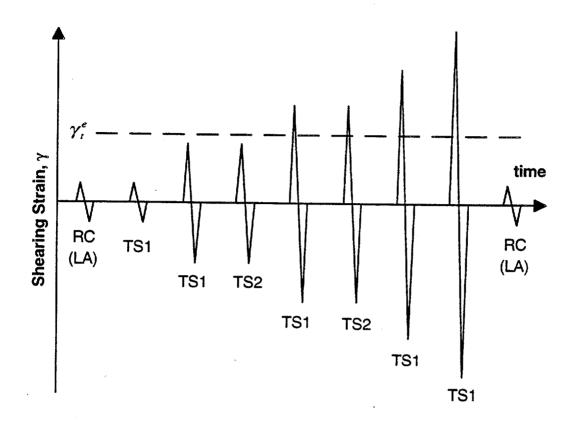


Fig. 18 Variation in Low-Amplitude Shear Modulus with Effective Confining Pressure from Resonant Column Tests of Intact Specimens from Yucca Mountain



 $\gamma_t^e$  = elastic threshold strain; below  $\gamma_t^e$ , G is constant and equal to G<sub>max</sub>

RC (LA) = resonant column test at low-amplitude strain

TS1 = torsional shear test in which 1 to 10 cycles are applied at 0.5 Hz

- TS2 = torsional shear test in which 4 cycles are applied at each of approximately 5 frequencies between 0.1 and 10 Hz
- Fig. 17 Testing Procedure Used in the Torsional Shear Test to Investigate the Effects of Strain Amplitude, Number of Loading Cycles and Excitation Frequency on Shear Modulus (G) and Material Damping Ratio (D)

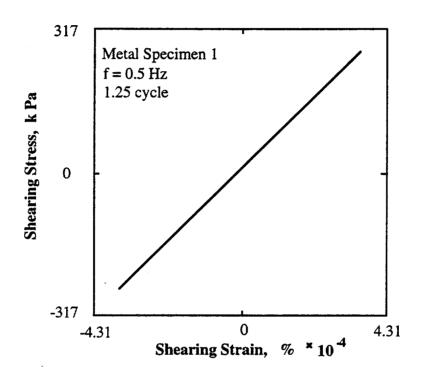


Fig. 16 Hysteresis Loops of Metal Specimen Determined by Torsional Shear Testing at a Frequency of 0.5 Hz

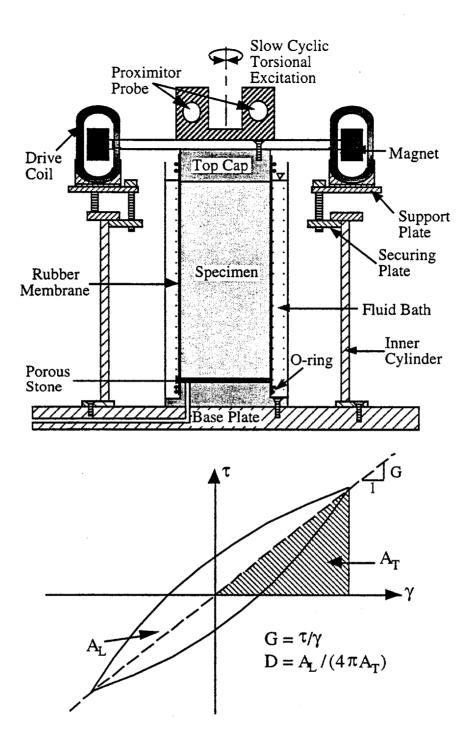


Fig. 15 Side View of a Fixed-Free Torsional Shear Test Set-Up and a Typical Hysteretic Loop for Shear Modulus and Material Damping Measurements

# YUCCA MOUNTAIN/CALIFORNIA **SCALING RELATIONS** Kenneth W. Campbell Yucca Mountain Ground Motion Workshop #2 Salt Lake City, Utah January 9-10, 1997 EQE

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# **Regional Scaling Characteristics**

- Regional differences included in this study:
  - Crustal structure ( $\beta$ ,  $\rho$ )
  - Crustal attenuation (Q)
  - Site attenuation ( $\kappa_0$ )
  - Stress drop ( $\Delta\sigma$ )
- Regional differences excluded in this study:
  - Source scaling relation
  - Magnitude measure
  - Distance measure

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# Methodology

- Point-source BLWN model
- Regional Earthquake, Crustal, and Site Characteristics
- **RVT Estimate of Ground Motion Parameters**
- Ratio of Ground Motions California/Yucca Mountain

# **Regional Characteristics**

• California:

EQE

- Crustal structure (Boore & Joyner, 1996)
- Crustal attenuation ( $Q = 150 f^{0.6}$ )
- Site attenuation ( $\kappa_0 = 0.04$  sec)
- Stress drop ( $\Delta \sigma = 100$  bars)
- Yucca Mountain:
  - Crustal structure (Yucca Mtn. Scenario Report)

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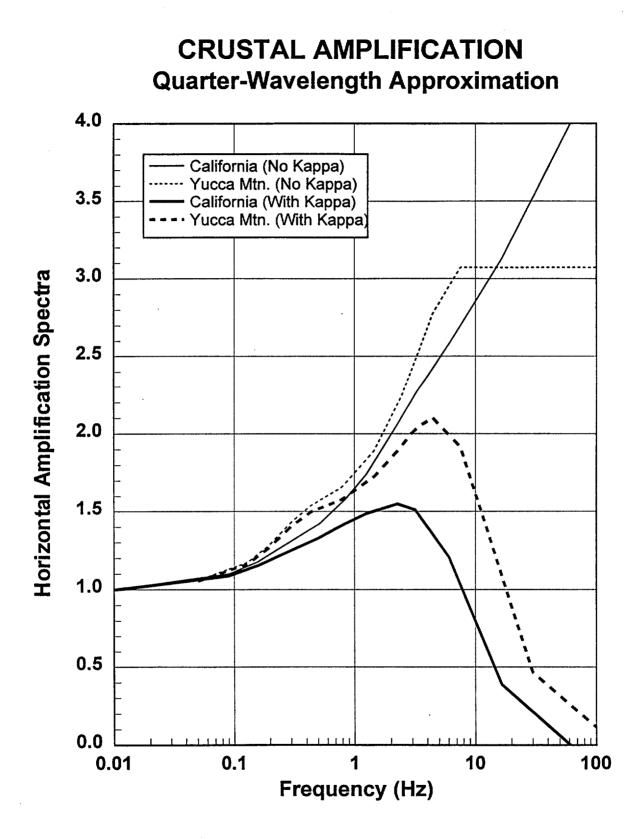
- Crustal attenuation ( $Q = 250 f^{0.4}$ )
- Site attenuation ( $\kappa_0 = 0.02$  sec)
- Stress drop ( $\Delta \sigma = 50, 75, 100$  bars)

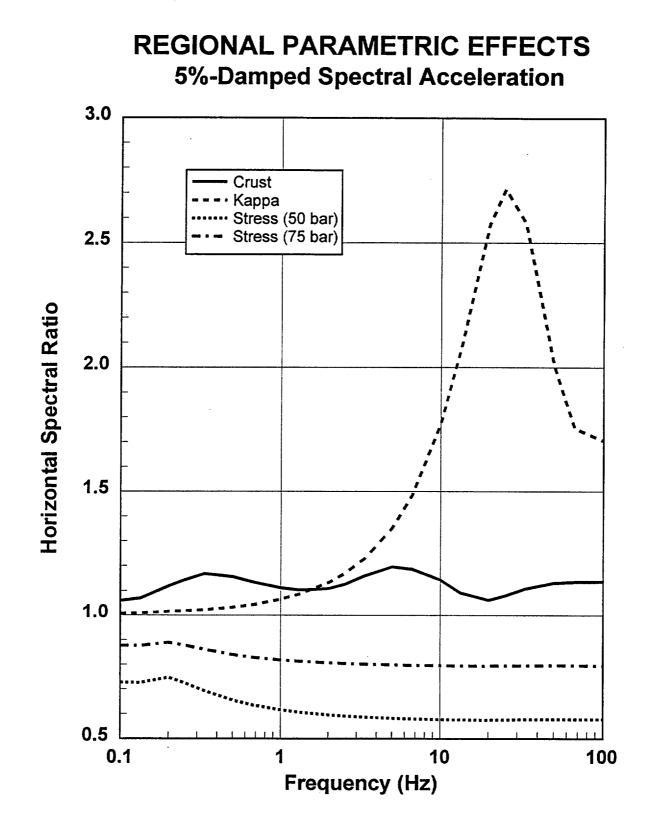
## Conclusions

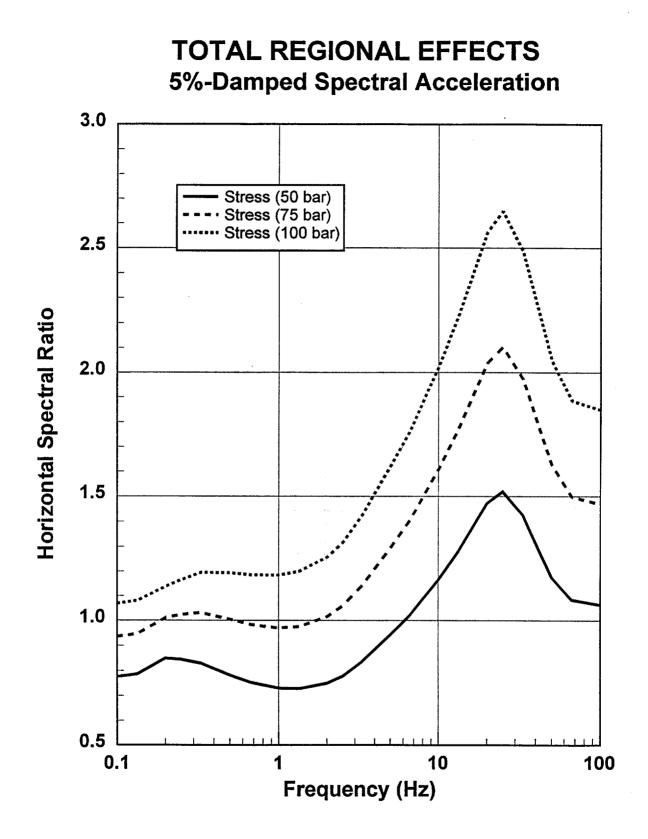
- Greatest sensitivity to regional characteristics between California and Yucca Mountain result from:
  - Site attenuation ( $\kappa_0$ ) at high frequencies
  - Stress drop ( $\Delta \sigma$ ) at all frequencies

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#### YUCCA MOUNTAIN GROUND MOTION WORKSHOP #2 -METHODS, MODELS AND PRELIMINARY INTERPRETATIONS

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#### Salt Lake City January 9-10, 1997

#### **GROUND MOTIONS AT YUCCA MOUNTAIN FROM SHALLOW EVENTS**

Paul Somerville Woodward-Clyde, Pasadena

#### **ISSUE 1: PATH EFFECTS AND SITE AMPLIFICATION AT YUCCA MOUNTAIN**

Analysis of strong motion recordings of NTS explosions at Yucca Mountain sites indicates that they have larger motions than those of other NTS stations by a factor of two on average over the period range of 0.5 to 5 Hz (Phillips, SAND88-3032, 1991). Phillips concluded that this was due to site response at Yucca Mountain, and tentatively attributed it to topographic amplification effects.

A preliminary analysis of explosion and earthquake recordings was described in Appendix B.2 of Seismic Design Inputs for the Exploratory Studies Facility at Yucca Mountain, which is attached. This preliminary analysis indicates that the large motions are due to surface waves which are generated by both NTS explosions and very shallow earthquakes such as those of the Rock Valley sequence of 1993. It is shown that the amplification does not occur in the body wave parts of these seismograms, and so would not affect the ground motions of earthquakes, which are dominated by body waves. It is demonstrated that these surface waves are not present in recordings of two deeper events of the 1993 Eureka Valley sequence that occurred at depths of 2 and 6 km.

At present, the argument in Appendix B.2 is anecdotal, and needs more systematic and rigorous development in order to effectively refute the hypothesis of Phillips (1991). This work should include data analyses of the kind already begun in Appendix B.2, but using a much more comprehensive set of seismograms. It should also include wave propagation modeling studies to investigate whether the crustal structure between NTS and the Yucca Mountain site, as delineated by Walck and Phillips (SAND88-3033; 1990), can give rise to the large surface waves that are observed at Yucca Mountain. The ability to explain these surface waves by modeling would provide a strong demonstration that the amplification effects can be accounted for by path effects, and that no site amplification effect is required to explain them. Since the path model of Walck and Phillips (1990) is a 2-D model, it may be necessary to use 2-D finite difference modeling of the type described by Graves (1993; 1995) to model the wave propagation effects along this path.

#### **ISSUE 2: SHALLOW FAULTING NEAR YUCCA MOUNTAIN**

It was noted in the discussion of Issue 1 that the 1993 Rock Valley earthquakes, which had very shallow depths, generated large surface waves at Yucca Mountain. This raises the question of whether very shallow earthquakes could occur closer to Yucca Mountain (a source characterization issue), and if so, how large their surface waves would be (a ground motion characterization issue). This gives rise to uncertainty in the median value and dispersion of ground motion attenuation relations for use at the site.

# GROUND MOTION SIMULATIONS USING A BROADBAND GREEN'S FUNCTION METHOD

A ground motion modeling exercise will be discussed as part of this meeting. This is an extension of Activity 8.3.1.17.3.3, ground modeling of scenario earthquakes at Yucca Mountain, performed by six ground motion modelers. They generated strong ground motion time histories for specific scenario earthquakes having discrete magnitudes and distances. One of these was a broadband Green's function method used by Somerville and Saikia (Somerville, 1992; Saikia, 1994). In the following, we briefly summarize how the broadband Green's function method was used. We also point out extensions of this method that could incorporate the effects of laterally varying velocity structure described under Issue 1. The results of these modeling activities could also be extended to produce ground motion attenuation relations for use in the probabilistic seismic hazard analysis program to complement the empirical models. This could be done using a comprehensive set of ground motion calculations for the full range of magnitudes and distances relevant to the site.

For source characterization, we considered seismic moment, fault length, fault width, strike, dip, rake, depth of top of fault, hypocenter, rupture velocity, slip distribution, and rise time, using models developed by Somerville and Abrahamson (1991). The most sensitive parameters are source depth, and fault length and width for a given seismic moment. Some constraints on these parameters were obtained from the source parameters of past Basin and Range earthquakes. We modeled the near-fault recordings of the 1992 Little Skull Mountain earthquake, and estimated the modeling and parametric uncertainty in the calculated ground motions using the procedure of Abrahamson et al. (1990).

The path is characterized by seismic velocities, density, and Q of a crustal model. The most sensitive parameters are velocity gradients in the shallow and deep parts of the crust, which should be well controlled by data at Yucca Mountain. Our wave propagation model could be further calibrated by modeling the recorded waveforms of earthquakes (such as the 1971 Massachusetts Mountain earthquake and the 1992 Little Skull Mountain earthquake sequence) and NTS explosions, to test whether flat layered models are adequate given the strong lateral variations in crustal structure noted by Walck and Phillips (1991). As discussed under Issue 1, the large surface waves generated at Yucca Mountain by shallow earthquakes such as the 1993 Rock Valley sequence (CRWMS, 1994, Appendix B2) need to be addressed. Similar large surface waves are recorded routinely at Yucca Mountain from NTS explosions and gave rise to the "site effects" (actually path effects according to our analysis) at Yucca Mountain noted by

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#### Phillips (1991).

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The site response is characterized using surface seismic velocities, density, and Q (kappa). The most sensitive parameter is kappa, which should be well controlled by data from Yucca Mountain. Abundant downhole recordings at Yucca Mountain and other NTS sites from NTS explosions, in addition to sparse underground recordings of the 1992 Little Skull Mountain earthquake sequence, could be used to further calibrate site response models.

The ground motion attenuation function is determined by the crustal structure and the source depth, and thus has predictive power in locations such as Yucca Mountain where crustal structure and source depth are available but few strong motion recordings exist. Our method can include Green's functions calculated using 2-D or 3-D models of crust structure, which may be quite relevant in view of the evidence for significant lateral changes in crustal structure around Yucca Mountain, especially at shallow crustal depths (Walck and Phillips, 1991).

We use empirical source functions to represent several stochastic aspects of high frequency ground motions that are difficult to model using deterministic methods. These include the incoherence that develops in the source radiation pattern at high frequencies, and scattering along the path and in the site region. Ideally, we would like to use recordings from the region to generate empirical source functions for use the site. To date we have not used empirical source functions from the Yucca Mountain region, but it may be possible to use strong motion recordings of the Little Skull Mountain earthquake and its aftershocks.

An important source of uncertainty is in knowing whether earthquake sources near the site radiate significantly at shallow depths, as occurred during the 1993 Rock Valley earthquake sequence (CRWMS, 1993). If so, then large surface waves are expected at Yucca Mountain, and it may be necessary to use 2-D or 3-D models to adequately model the propagation of these surface waves.

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Civilian Radioactive Waste Management System Management & Operating Contractor

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Seismic Design Inputs for the Exploratory Studies Facility at Yucca Mountain

-Technical Report-

#### BAB000000-01717-5705-00001 REV00

April 29, 1994

Prepared for:

U.S. Department of Energy Yucca Mountain Site Characterization Project Office P.O. Box 98608 Las Vegas, NV 89193-8608

#### Prepared by:

Civilian Radioactive Waste Management System Management & Operating Contractor 101 Convention Center Drive Suite P-110 MS 423 Las Vegas, NV 89109

> Under Contract Number DE-AC01-91RW00134

## APPENDIX B SITE-SPECIFIC EFFECTS ON GROUND MOTION

### B.2 PATH EFFECTS: EFFECT OF SHALLOW SOURCE DEPTH ON GROUND MOTIONS AT YUCCA MOUNTAIN

Phillips (1991) analyzed recordings of underground nuclear explosions (UNEs)at four stations near Yucca Mountain and identified an amplification of ground motion by about a factor of 2 relative to other stations recording the events. An understanding of the cause of this amplification is important to assessing ground motion hazard for the ESF from earthquakes. Whether the amplification results from path effects or represents a site response at Yucca Mountain will determine if the probabilistically derived ground motion values need to be modified.

Figure B-1, modified from Walck and Phillips (1990), shows the locations of UNE sources and strong motion recording stations at Yucca Mountain and Jackass Flats. The four sites shown in Figure B-2 (Sites 14, 21, 22 and 23) have significantly larger ground motions than at other stations at comparable distances within the Nevada Test Site (NTS) (Figures B-3 through B-6). Amplifications of horizontal PSRV in the frequency range of 0.5 to 5 Hz are about a factor of 2 on average. Specifically, the amplification factors for horizontal motions are approximately 2.1, 2.4, 2.0 and 1.8 for frequencies of 0.5, 1, 2 and 5 Hz; the corresponding amplification factors for vertical motions are 2.4, 2.4, 2.3, and 1.8.

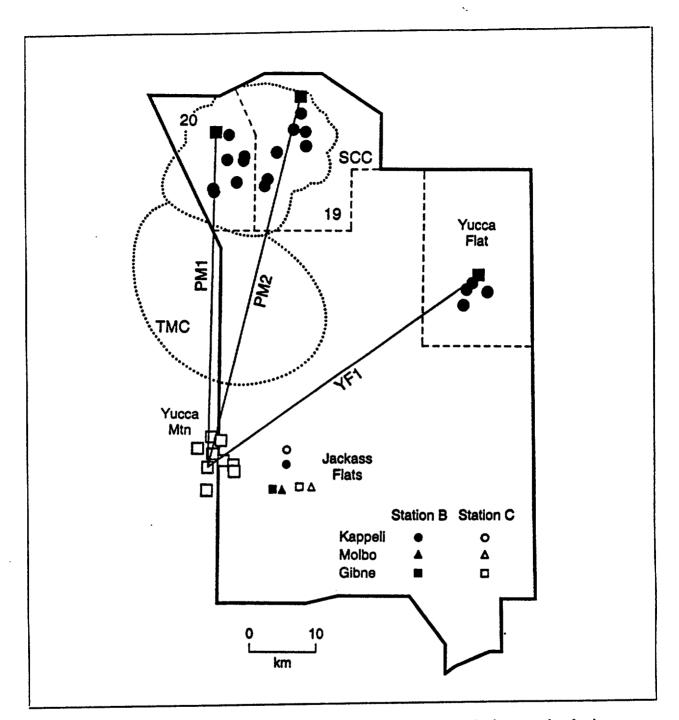


Figure B-1. Map showing locations of seismic stations, explosions, and velocity profiles PM1, PM2, and YF1. Large open squares represent stations at Yucca Mountain. The small circle, square, and triangle west of Jackass Flats indicate the location of station B (solid) and C (open). The larger, solid squares and circles indicate explosion locations. Area 19 and 20 encompass the Pahute Mesa area. Also shown are the Timber Mountain Caldera (TMC) and the Silent Caldera (SCC). (From Walck and Phillips, 1990)

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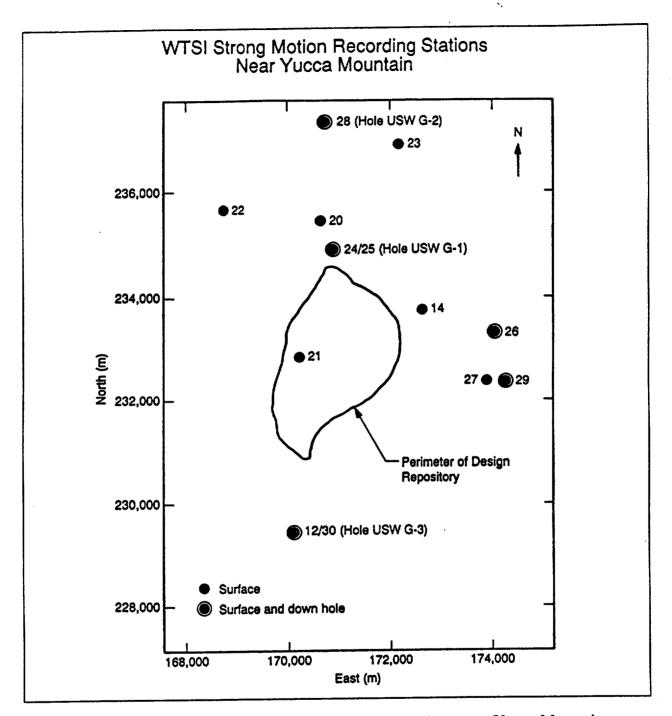
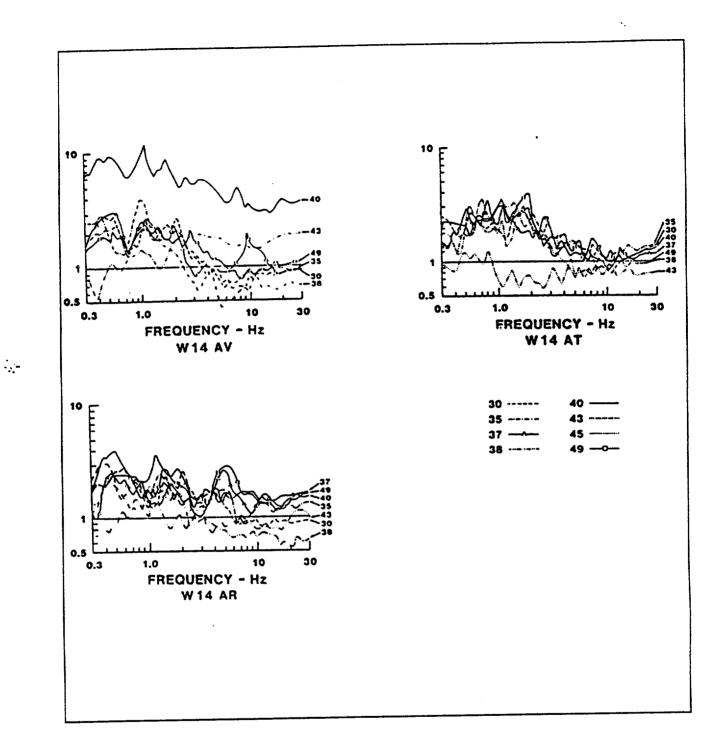
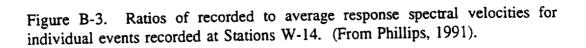


Figure B-2. Location of strong motion recording stations near Yucca Mountain operated as part of WTSI. Solid circles indicate surface recording stations; solid circles enclosed within an open circle represent sites with both surface and down-hole stations. (From Phillips, 1991)



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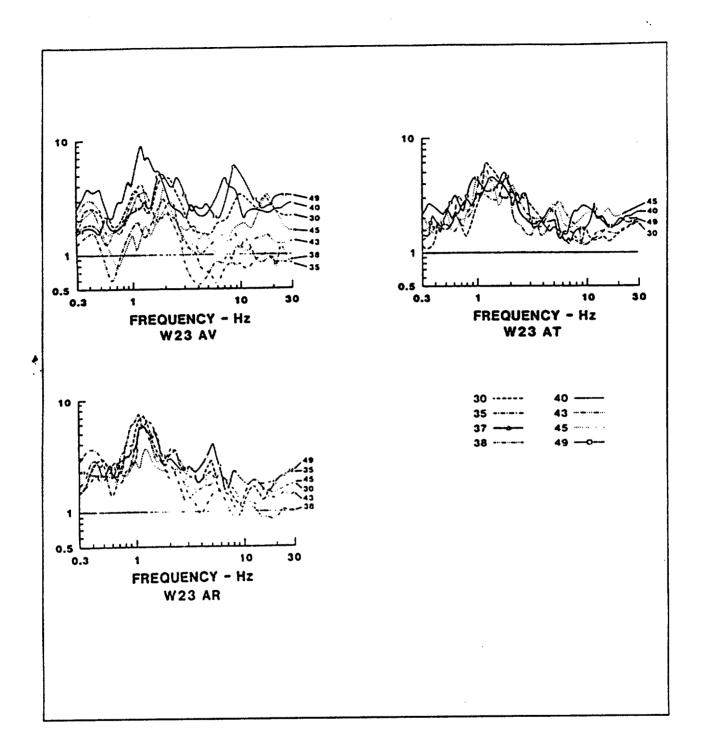


Figure B-4. Ratios of recorded to average response spectral velocities for individual events recorded at Stations W-23. (From Phillips, 1991).

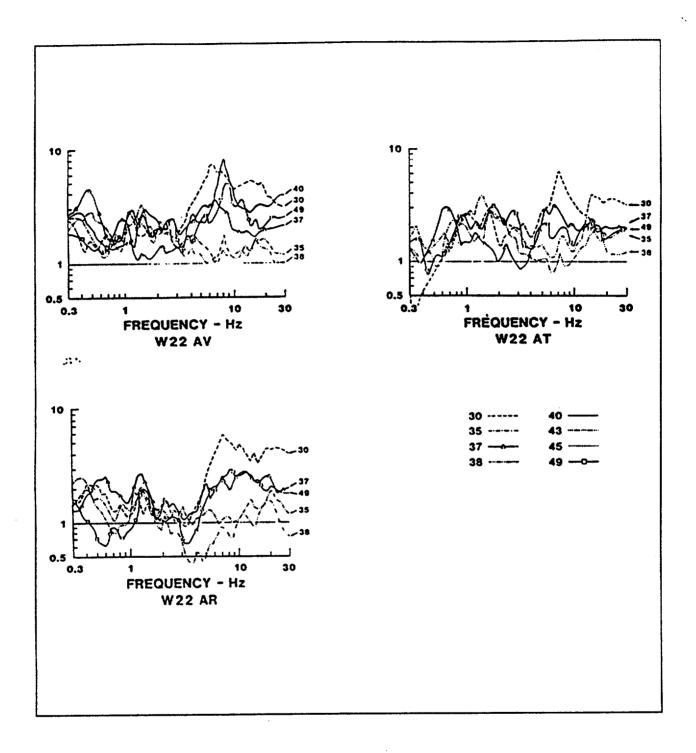
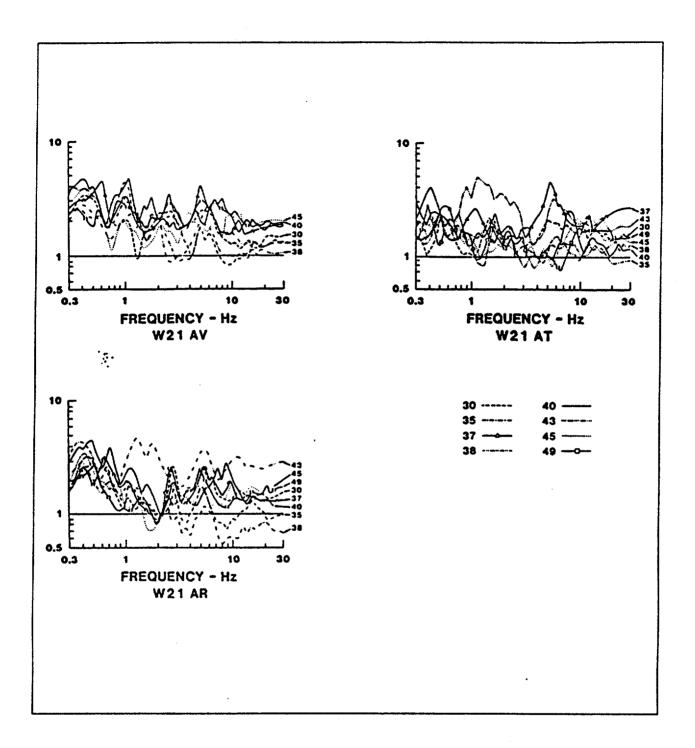
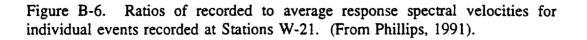


Figure B-5. Ratios of recorded to average response spectral velocities for individual events recorded at Stations W-22. (From Phillips, 1991).

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Based on the analysis that follows, it is demonstrated that the amplification effects observed in the Yucca Mountain recordings are due to the shallow path between NTS and Yucca Mountain, and not to site effects. It is shown that the amplification effects occur only in the surface waves and not in the shear waves. Surface waves are insignificant in Yucca Mountain recordings of earthquakes occurring at normal depths. Therefore, it is not expected that the amplification effects observed in the explosion data at Yucca Mountain will be present in the strong ground motions of earthquakes that occur at normal crustal depths.

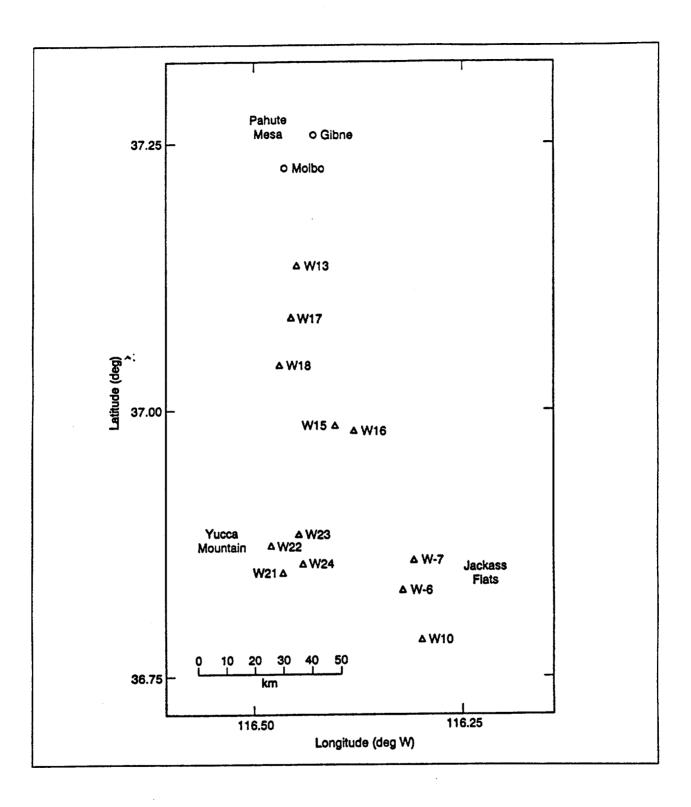
## **B.2.1 SEPARATION OF PATH AND SITE EFFECTS**

Figures B-7 shows the locations of strong motion stations that recorded NTS explosions Gibne and Molbo. The radial component velocity recordings of Gibne along this profile are shown in Figure B-8. This profile shows the presence of surface waves not only at the Yucca Mountain stations W14, W21, W22 and W23, but also at stations both to the north and south of the repository. The surface waves propagate from near Pahute Mesa to Yucca Mountain along this profile. The profile for event Molbo shows similar features indicating that they are characteristic of this path.

The shallow structure for this path to Yucca Mountain (path PM2 in Figure B-1) is shown in the center panel of Figure B-9 (Walck and Phillips, 1990). This structure has been approximated using a 1-D velocity model shown in Table B-1, and the travel times for direct and reflected phases shown in Figure B-8 were calculated. The P wave onset is generally no larger than the immediately following coda, and there is no distinct change in the character of the motions at the expected S wave arrival time. The large surface waves, which may be described as Rg, arrive at a time that corresponds to the time of the direct S wave in the top layer. This direct S wave is not expected to have any significant energy, and its arrival time is shown only as a guideline for interpreting the surface wave.

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Although the stations due south of Pahute Mesa all contain surface waves, they are absent from stations in Jackass Flats, which include stations W6, W7, and W10; this absence is particularly notable in station W6. For event Kappeli, Jackass Flats stations B and C (Figure B-1) were located on tuff like that at the Yucca Mountain stations W14 and W21. The tangential component velocity seismograms for the Kappeli event at stations B and C are compared with those at stations W21 and W14 in Figures B-10 and B-11, respectively. The plots all have different vertical axes scaled to the maximum velocity. The presence of much larger surface waves at the two Yucca Mountain stations W14 and W21 is evident in these recordings. The very heterogeneous nature of the shallow structure shown in Figure B-9 may explain why the path from Pahute Mesa to Yucca Mountain can produce such different seismograms compared with the path from Pahute Mesa to Jackass Flats.



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Figure B-7. Locations of stations that recorded UNE's Gibne and Molbo. Stations are shown by triangles; the two events by open circles.

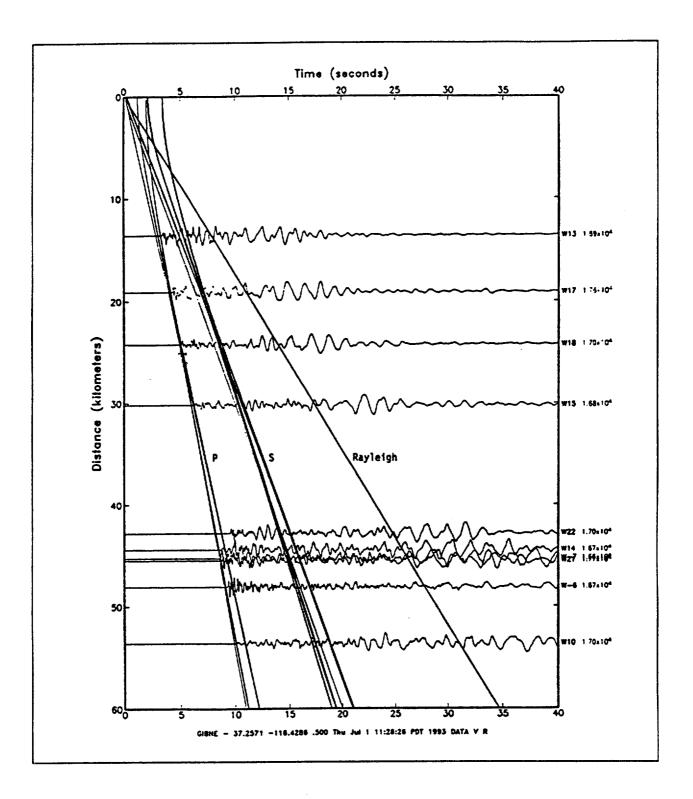


Figure B-8. Profile of velocity seismograms recorded from UNE Gibne at stations shown in Figure B-7..

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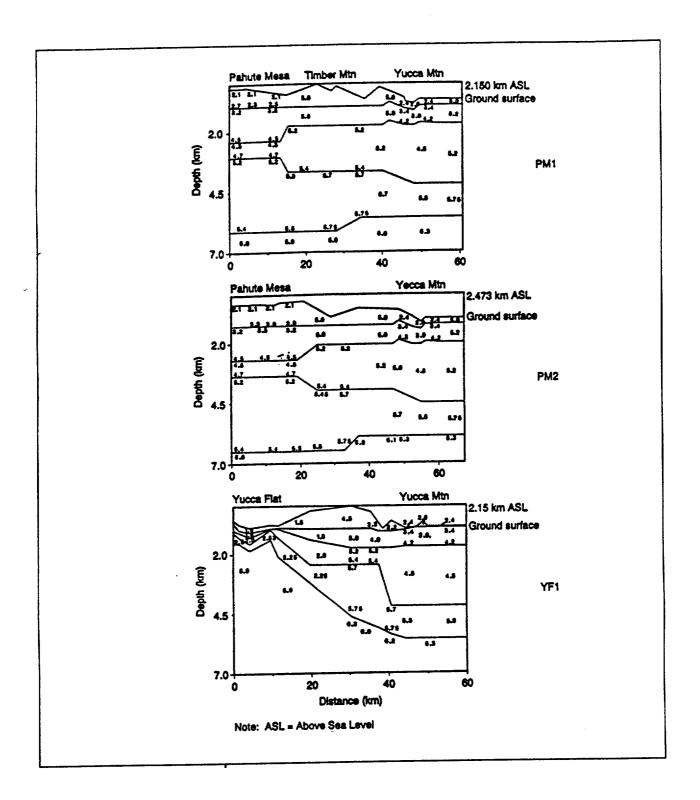
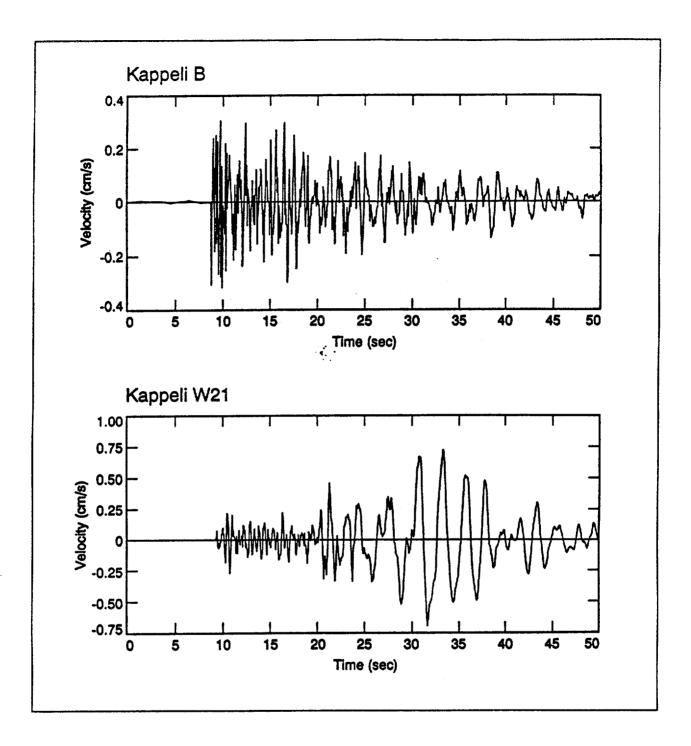


Figure B-9. Crustal seismic velocity cross sections to Yucca Mountain from the three UNE source areas shown in Figure B-1. (From: Walck and Phillips, 1990.)



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Figure B-10. Velocity seismograms of UNE Kappeli recorded at Stations B and W21.

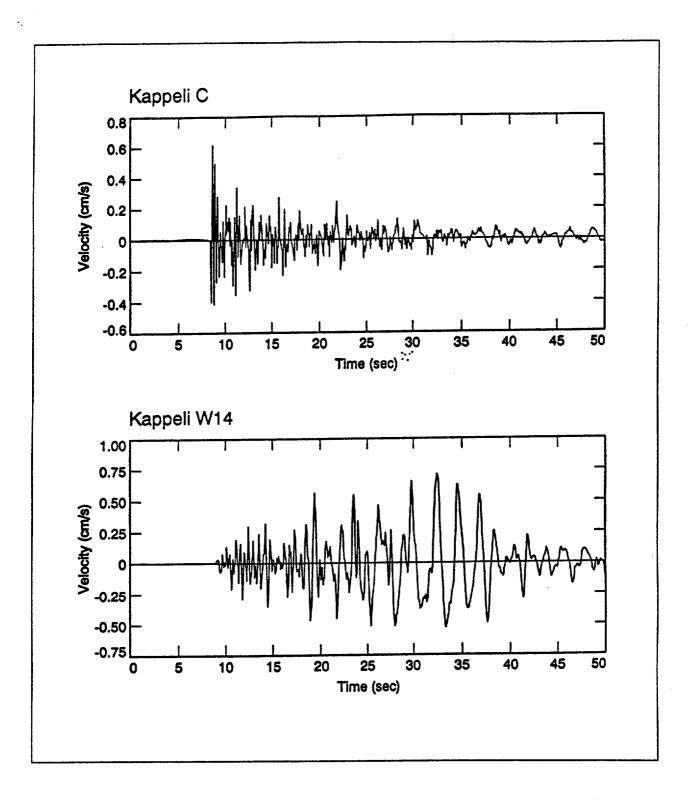


Figure B-11. Velocity seismograms of UNE Kappeli recorded at Stations C and W14.

P Wave Velocity (km/sec)	S Wave Velocity (km/sec)	Density (gm/cc)	Depth to Top (km)
3.0	1.73	2.21	0.0
5.0	2.89	2.53	0.5
5.7	3.29	2.65	3.2
6.0	3.47	2.70	5.3

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Table B-1.	Yucca	Mountain	Crustal	Structure
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# B.2.2 DEMONSTRATION THAT THE SHALLOW PATH EFFECT DOES NOT AFFECT BODY WAVES

The next step of the analysis is to show that surface waves, not body waves, cause the amplification effects observed in the Yucca Mountain recordings of explosions. The amplification is therefore not expected to be present in the recordings of earthquakes except those that have significant energy release at shallow depths, generating higher mode surface waves. The approach is to compare amplitudes between Yucca Mountain and Jackass Flats for both the surface wave and the shear wave. It is found that the surface wave amplitudes at Yucca Mountain are larger than those at Jackass Flats, but the shear wave amplitudes are approximately equal.

The separation of seismic phases is difficult in seismograms of nuclear explosions recorded at this distance range. While the first motion is certainly the P wave, the S wave does not have a clear onset. It is assumed that the first 5 seconds of motion are P waves, the second five seconds are predominantly S waves, and the subsequent waves are predominantly surface waves. These assumptions are consistent with the sense of particle motion inferred from superposition of the vertical and radial components.

The recordings of the three explosions used in this study are listed in Table B-2. Measurements of the peak velocity and peak acceleration of each component of each record were made in each of these three time windows. For peak velocity, the predominant period of the wave having the peak velocity was also measured. The results are given in Table B-3 for peak velocity, Table B-4 for period of peak velocity, and Table B-5 for peak acceleration. Neglecting the differences in magnitude between the three events, and the differences in site conditions, the ground motions of the three events at each pair of stations are averaged to derive an overall comparison of ground motion characteristics between the Yucca Mountain stations and those on Jackass Flats.

It is observed that the S wave peak horizontal velocity amplitudes between the two pairs of stations are comparable, but the surface wave peak velocities are about twice as large at Yucca Mountain as at Jackass Flats. Also, the period of the peak S wave horizontal velocity is comparable (about 0.7 sec. in each case), but the period of the peak surface wave velocity is about twice as long (about 2.0 sec) for Yucca Mountain as it is on Jackass Flats (about 1.0 sec). The peak horizontal accelerations are similar between Yucca Mountain and Jackass Flats for both the S wave and the surface wave. These results support the hypothesis that the amplification of peak velocity observed in Yucca Mountain recordings of explosions is due to surface waves.

Event	Station	Range (km)		
Kappeli	14	45.6		
Kappeli	21	46.7		
Kappeli	В	45.9		
Kappeli	С	44.0		
Molbo	14	40.8		
Molbo	21	41.7		
Molbo	В	45.6		
Molbo	С	45.6		
Gibne	14	44.2		
Gibne	21	45.3		
Gibne	В	48.1		
Gibne	С	48.1		

Table B-2. Recordings Used to Evaluate the Ground Motion Amplification at Yucca Mountain

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Event	Com-		Station 14	4	5	Station 21		Station B			Station C		
	ponent	0 <t∡5 (P)</t∡5 	5⊲t±10 (S)	t>10 (Surf)	0 <t∡5 (P)</t∡5 	5⊲t∡10 (S)	t>10 (Surf)	0 <t<b>∡5 (P)</t<b>	5 <t∡10 (S)</t∡10 	t>10 (Surf)	0 <t∡5 (P)</t∡5 	5⊲1≰10 (S)	t>10 (Surf)
Kappeli	v	0.0049	0.0030	0.0038	0.0039	0.0027	0,0027	0.0044	0.0018	0.0014	0.0029	0.0014	0.0013
	R	0.0032	0.0032	0.0051	0.0025	0.0025	0.0041	0,0043	0.0037	0,0030	0.0029	0.0029	0.0014
	T	0.0030	0.0047	0.0072	0.0026	0.0022	0.0073	0.0032	0.0030	0.0020	0.0062	0.0028	0.0024
Molbo	v	0.0053	0.0026	0.0040	0.0061	0.0032	0.0049	0.0085	0.0030	0.0010	0.0088	0.0021	0.0025
	R	0.0040	0.0044	0.0065	0.0032	0.0046	0.0059	0.0095	0.0038	0.0035	0.0029	0.0035	0.0036
	Т	0.0039	0.0053	0.0064	0.0036	0.0035	0.0053	0.0047	0.0024	0.0029	0.0035	0.0044	0.0045
Gibne	v	0.0041	0.0022	0.0036	0.0056	0.0030	0.0044	0.0041	0.0016	0.0016	0.0034	0.0019	0.0025
	R	0.0043	0.0037	0.0044	0.0040	0.0027	0.0053	0.0035	0.0022	0.0024	0.0033	0.0024	0.0025
	Т	0.0022	0.0044	0.0063	0.0057	0.0031	0.0045	0.0030	0.0035	0.0040	0.0026	0.0026	0.0027
Average H	Iorizontal		0.0043	0.0060		0.0031	0.0056		0.0030	0.0029		0.0031	0.029

Table B-3. Peak Particle Velocity (m/sec) by Recording Station for Three Distinct Time Windows

Event	Com-		Station 14			Station 21		Station B			Station C		
	ponent	0 <t<b>±5 (P)</t<b>	5 <t<b>≾10 (S)</t<b>	t>10 (Surf)	0 <t<b>≾5 (P)</t<b>	5 <t<b>≾10 (S)</t<b>	t>10 (Surf)	0 <t<b>≤5 (P)</t<b>	5 <t<b>≾10 (S)</t<b>	t>10 (Surf)	0 <t<b>≾5 (P)</t<b>	5 <t<b>≾10 (S)</t<b>	t>10 (Surf)
	v		0.4	1.0		0.9	1.8		0.7	1.1		0.9	1.1
(Surf) Kappeli	R		0.5	2.0		0.5	2.0	-	0.7	0.9		0.4	0.7
	Т		0.7	2.2		0.7	3.0		0.9	0.8		0.5	0.7
Molbo	v		1.0	1.8		0.8	2.1		0.3	0.8		1.0	0.9
	R		0.5	1.8		1.0	2.3		0.7	2.1		0.9	0.9
	Т		0.4	0.9		0.6	2.5		0.4	1.3		0.4	1.2
Gibne	v		0.7	1.8		0.8	1.9		0.9	0.8		1.0	0.9
	R		1.1	2.1		0.8	2.2		0.6	0.3		1.0	0.5
	Т		1.0	1.0		0.9	1.8		0.6	2.0		0.5	1.1 <sup>AV</sup>
Average	Horizontal		0.7	1.7		0.8	2.3		0.7	1.2		0.6	0.8

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Table B-4. Period of Peak Particle Velocity by Recording Station for Three Distinct Time Windows

Event	Com-		Station 14			Station 21			Station B			Station C	
	ponent	0 <t<b>≤5 (P)</t<b>	5 <t<b>≤10 (S)</t<b>	t>10 (Surf)	0 <t<b>≾5 (P)</t<b>	5 <t<b>±10 (S)</t<b>	t>10 (Surf)	0 <t<b>≾5 (P)</t<b>	5 <t<b>≤10 (S)</t<b>	t>10 (Surf)	0 <t<b>≾5 (P)</t<b>	5 <t<b>≾10 (S)</t<b>	t>10 (Surf)
Kappeli	v												
	R	0.059	0.052	0.037	0.043	0.039	0.031	0.145	0.055	0.050	0.083	0.048	0.043
	Т	0.044	0.047	0.047	0.042	0.036	0.043	0.107	0.057	0.048	0.147	0.054	0.034
Molbo	v												
	R	0.063	0.055	0.042	0.060	0.051	0.031	0.314	0.070	0.040	0.088	0.050	0.047
	Т	0.059	0.071	0.057	0.083	0.064	0.036	0.146	0.062	0.038	0.088	0.060	0.038
Gibne	v												
	R	0.085	0.037	0.032	0.063	0.031	0.024	0.135	0.022	0.018	0.065	0.038	0.040
	Т	0.047	0.043	0.054	0.104	0.030	0.027	0.096	0.054	0.032	0.050	0.040	0.027
N	rage zontal		0.051	0.045		0.042	0.032		0.053	0.038		0.048	0.038

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Table B-5. Peak Particle Acceleration (m/sec/sec) by Recording Station for Three Distinct Time Windows

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#### B.2.3 ABSENCE OF SHALLOW PATH EFFECT ON GROUND MOTIONS FROM NORMAL DEPTH EARTHQUAKES

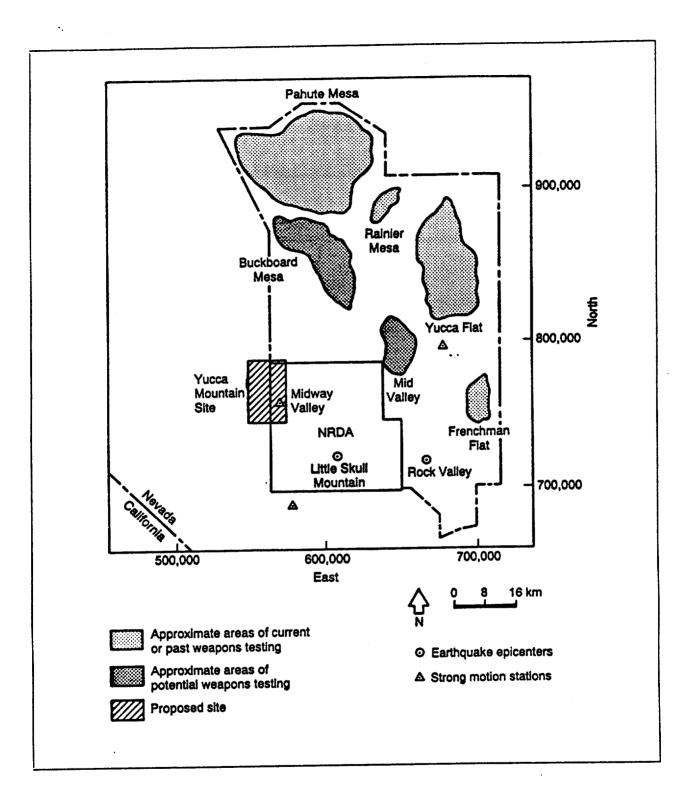
The next step of our analysis is to evaluate whether surface waves like those recorded from explosions could be present in the ground motions of the earthquakes that dominate the seismic hazard at the site. The analyses that follow indicate that the large surface waves evident in the explosion data recorded at Yucca Mountain are not present in the recordings of earthquakes that occur at depths greater than a few km.

A list of some of the larger earthquakes that have been recorded recently at the Yucca Mountain site is given in Table B-6. In the following, velocity seismograms of four earthquakes recorded on rock in Midway Valley are described. The first is a magnitude 3.2 aftershock of the June 29, 1992 Little Skull Mountain earthquake, which occurred at a depth of about 9.5 km at a distance of about 16 km from the recording station on 9 May 1993. The second is a magnitude 4.0 earthquake in Rock Valley that occurred on 30 May 1993 at a very shallow depth (1.5 km). The third and fourth are magnitude 4 aftershocks of the May 17, 1993 Eureka Valley earthquake at depths of 6 and 2 km respectively. The parameters of the earthquakes are listed at the bottom of Table B-6, and the locations of the first two epicenters and the recording station are shown in Figure B-12.

The three component velocity seismograms of the first two earthquakes are shown in Figure B-13. The seismograms of the deeper event have S waves that are much larger in amplitude than the surface waves. In contrast, the seismograms of the shallow event have surface waves that are larger than the S waves. The three component velocity seismograms of the two Eureka Valley aftershocks are shown in Figures B-14 and B-15. The peak velocities of both seismograms are dominated by body waves. However, surface waves are present in both seismograms, and are more pronounced for the shallower event. For the Massachusetts Mountain earthquake of August 5, 1971, which occurred at a depth of about 4 km and had a magnitude of 4.3, displacement seismograms exhibit large shear waves and small surface waves (Vortmann, 1982).

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While the general question of site response at Yucca Mountain has not been addressed by this analysis, it has been shown that the amplification effects evident in explosion data recorded at Yucca Mountain are related to the shallow nature of the source. Further, such effects are not observed for earthquakes occurring at more than a few kilometers depth. Hence, because most of the energy release occurs at depths greater than 3 km in large earthquakes, and because earthquakes at very shallow depth do not contribute strongly to the ground motion hazard at Yucca Mountain, ground motion amplification associated with higher mode surface wave propagation from shallow sources need not be considered in development of ESF seismic design inputs.



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Figure B-12. Locations of strong motion recording stations and selected earthquakes in relation to the Yucca Mountain site.

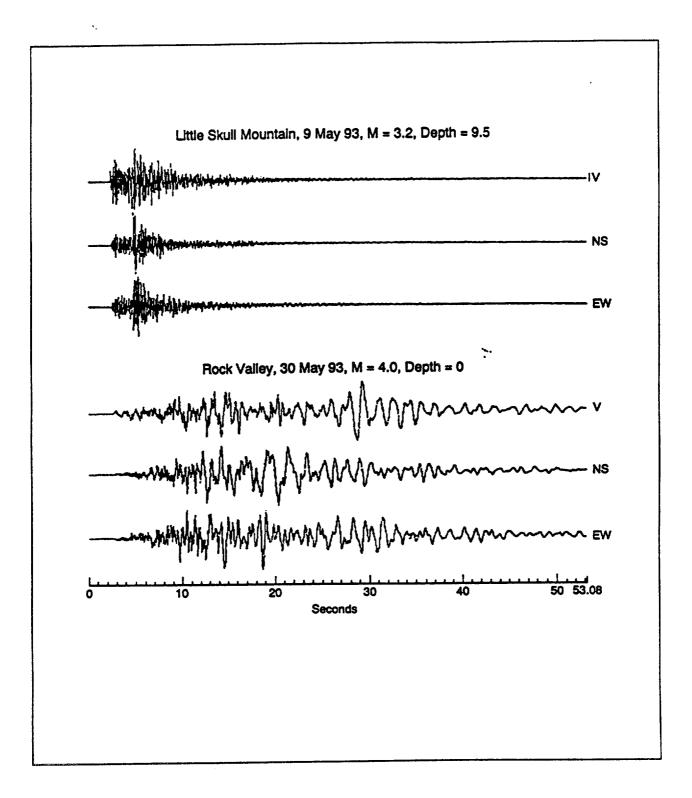


Figure B-13. Velocity time histories of a Little Skull Mountain aftershock and a Rock Valley earthquake recorded at Midway Valley.

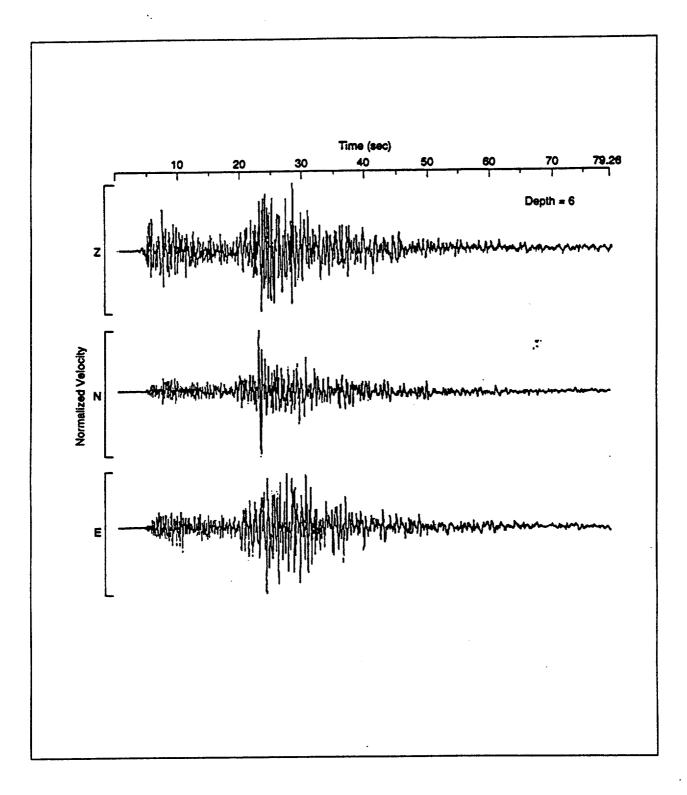


Figure B-14. Velocity time seismogram of a Eureka Valley aftershock with a depth of 6 km recorded at Midway Valley.

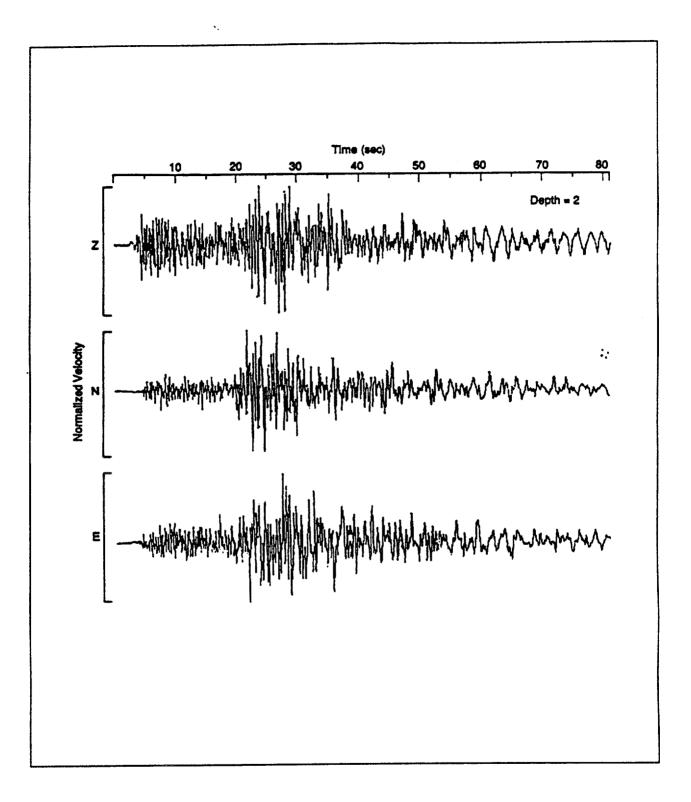


Figure B-15. Velocity seismogram of a Eureka Valley aftershock with a depth of 2 km recorded at Midway Valley.

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Location	Date	Depth (km)	Magnitude	Mechanism
Massachusetts Mtn	1971.8.5	4.3	4.3	strike-slip
Little Skull Mountain	1992.6.29	9.6	5.6	normal
Little Skull Mountain	1992.7.5		4.4	strike-slip
Southwestern Utah	1992.9.2		5.9	
Little Skull Mountain	1992.9.7		3.1	
Rock Valley	1993.5.15		3.6 4.0 2.8	
Eureka Valley	1993.5.17 1993.6.3 1993.6.8	9.1 5.9 1.7	6.1 3.9 4.4	normal
EVENTS IN FIG. B-13:				
Little Skull Mountain	1993.5.9	9.5	3.2	
Rock Valley	1993.5.30	0	4.	

Table B-6. List of Earthquakes Having Strong Motion Recordings Near Yucca Mountain

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#### **REGULATIONS AND ORDERS**

- 10 CFR Part 60 (Code of Federal Regulations) (1990): Title 10, Energy, Part 60, "Disposal of High-Level Radioactive Wastes in Geologic Repositories", Washington, D.C.
- DOE (U.S. Department of Energy), 1993, Natural Phenomena Hazards Mitigation, Order DOE 5480.28.

## EVALUATION OF EMPIRICAL ATTENUATION RELATIONS FOR EXTENSIONAL REGIME EARTHQUAKES

Presentation by Paul Spudich, U.S. Geological Survey, Menlo Park, CA

Ground Motion Workshop #2 -Methods, Models, and Preliminary Interpretations

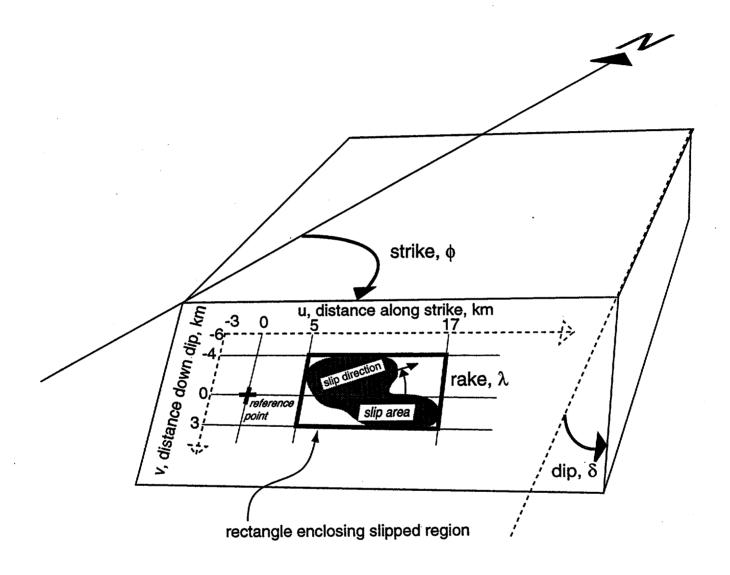
> Doubletree Hotel Salt Lake City, UT

January 9, 1997

Two ways to estimate ground motions based on the extensional regime data set:

1. Develop a new ground motion prediction relation (SEA96)

2. Calculate correction factors for existing ground motion prediction relations



## GEOLOGIC SITE CONDITIONS

We characterized each site by a geologic code G=1,...,6, and by a depth to basement, when available.

#### Hard rock (G=1)

- plutonic igneous rocks, lava flows, welded tuffs, and metamorphic rocks (if not severely weathered)

#### Soft rock (G=2)

 ordinary sedimentary rocks (unless described as very hard), severely weathered rocks, pyroclastic rocks (except welded tuffs)

#### Rock of unknown hardness (G=0)

- (treated like soft rock in all calculations)

#### Deep soil (G=6)

- alluvium, sand, gravel, clay, slit, mud, fill, glacial outwash, etc, >20 m thick

#### Shallow soil (G=7)

- alluvium, sand, gravel, clay, slit, mud, fill, glacial outwash, etc, 5m to 20 m thick

#### Soil of unknown thickness (G=5)

- (treated like deep soil in all calculations)

#### Campbell's "depth to basement"

- depth to the top of unweathered crystalline igneous or metamorphic rock, or the depth at which P velocities of 5.0 km/s or S velocities of 3.0 km/s are reached and velocity gradients are low. (*not available for all sites*)

# DEVELOPMENT OF NEW PREDICTIVE RELATIONSHIP SEA96

We used the two stage regression method of Joyner and Boore (1993, 1994) to obtain the coefficients of the following regression relation (which we have baptized *SEA96*):

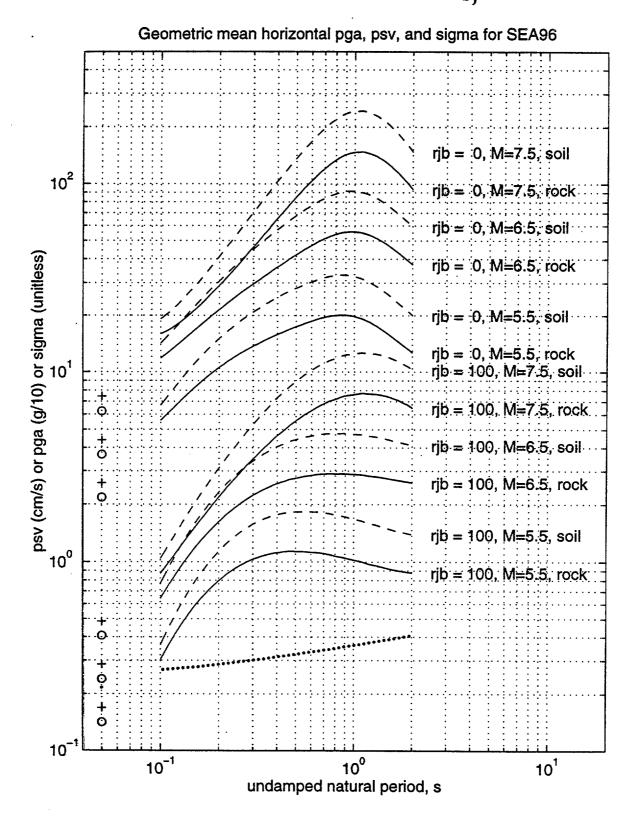
$$\log_{10} Y = b_1 + b_2 (M - 6) + b_3 (M - 6)^2 + b_4 R + b_5 \log_{10} R + g b_6$$

where

$$R := \sqrt{r_{jb}^2 + h^2}$$
,  $g = 0$  for rock,  $g = 1$  for soil ,  $M =$ moment magnitude  
 $r_{jb} =$ closest distance to the vertical projection of the fault surface  
 $b_2$ ,  $b_4$ , h are coefficients determined by Boore et al. (1994)  
 $b_1$ ,  $b_5$ ,  $b_6$  are coefficients determined by our regression

We were forced to use  $b_2$ ,  $b_4$ , and h from Boore et al. (1994) because our data set did not span a wide enough range of magnitude to determine these coefficients adequately.

# Figure 3. Sample evaluations of SEA96 for $M = 5.5, 6.5, 7.5, r_{bi} = 0, 100 \text{ km}$



# COMPARISON OF OUR EXTENSIONAL REGIME DATA WITH OTHER GROUND MOTION PREDICTION RELATIONS

We compared our data set with the following relations:

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our abbrev.	reference
BJF94	Boore, Joyner, and Fumal (1993, 1994)
CB94	Campbell and Bozorgnia (1994)
	Campbell (1989) (scaled so its pha equals CB94 pha)
C90 or C90/94	Campbell (1990) (scaled so its pha equals CB94 pha)
C93/94	Campbell (1993) (scaled so its pha equals CB94 pha)
193	Idriss (1991, 1993)
JB88	Joyner and Boore (1988)
SP96	Sabetta and Pugliese (1996)
S93	Sadigh et al. (1993)

Table 5:Correspondence between various authors' site classifications and the classifications used in this work.• indicates the combinations of Campbell's relations and site classes actually used in this reportOur soil classes(4)

				Our son cia				
Authors	Predicted	horizontal	rock of	hard rock	soft rock	soil of	deep soil	shallow soil
	parameters	used	unknown	(6)	(6)	unknown	(h > 20m)	(5m < h < 20m)
	(7)		hardness			thickness		20m)
	( <i>italic</i> =used in this study)		(3,6) (G=0)	(G=1)	(G=2)	(G=5)	(G=6)	(C-7)
<b>B 10</b> 0 4		ļ		· · · · · · · · · · · · · · · · · · ·	· · · · · · · · · · · · · · · · · · ·			(G=7)
BJF 94	pha, psvh	geom. mean (5)	Vs = 620 m/s					Vs = 310 m/
C 89 (2)	pha, <i>phv</i> ,	arith. mean	"soil/soft	n/a	"soil/soft	•"soil/soft	•"soil/soft	•"soil/soft
	psvh		rock" (3)		rock"	rock"	rock"	rock"
	pza, pzv,							:
	psvz							
C 90	pha, phv,	arith. mean	•'>10m soil	n/a	•'>10m soil	'>10m soil	'>10m soil	n/a
	psvh		or soft rock'		or soft rock'	or soft rock'	or soft rock'	
	pza, pzv,							
<b></b>	psvz							
C 93 (1)	pha, <i>psah</i>	arith. mean	'rock'(1)	•'rock' (1)	'rock' (1)	'soil' (1)	'soil' (1)	'soil' (1)
CB 94	pha	geom. mean	•'soft rock'	•'hard rock'	•'soft rock'	•'alluvium'	•'alluvium'	•'alluvium'
JB 88	psvh, pha,	geom. mean	'rock'	'rock'	'rock'	'soil'	'soil'	'soil'
	phv	(5)						
Idriss 93	pha, psah	geom. mean	'rock'	'rock'	'rock'	n/a	n/a	n/a
			(	(	( 100			
SP 96	pha, phv,	larger	'stiff	'stiff	'stiff	'deep soil,	'deep soil,	'shallow,
	psvh		<5m soil'	<5m soil'	<5m soil'	>20m soil'	>20m soil'	5-20m soil'
S 93	pha, psah,	geom. mean	'rock'	'rock'	'rock'	n/a	n/a	n/a
	pza, psaz							

(1) C93 has two site catagories: "Quaternary deposits (soil)" and "Tertiary or older sedimentary, metamorphic, and igneous deposits (rock)". Campbell (written communication, 1995) says we should use this relation for psa on *hard* rock only.

(2) C89 was developed using soil data only, but stated to be appropriate for soft rock also. Campbell (written communication, 1995) says we should use this relation for psvh, pza, psvz and psaz on soil.

(3) rock of unknown hardness is assumed to be a soft rock, as true hard rock sites are relatively rare, particularly in the Western US.

(4) G is an arbitrary site code number. Numbers 3 and 4 are not used.

(5) Coefficients for the random horizontal were used, which is identical to the geometric mean. See Appendix A for  $\sigma_{\log y}^2$  calculation.

(6) Sites having 5m of soil or less are considered rock sites

(7) Abbreviations: h=horizontal, z=vertical, a=acceleration, v=velocity, pza=peak vertical acceleration, psah=horizontal pseudospectral acceleration, etc ...

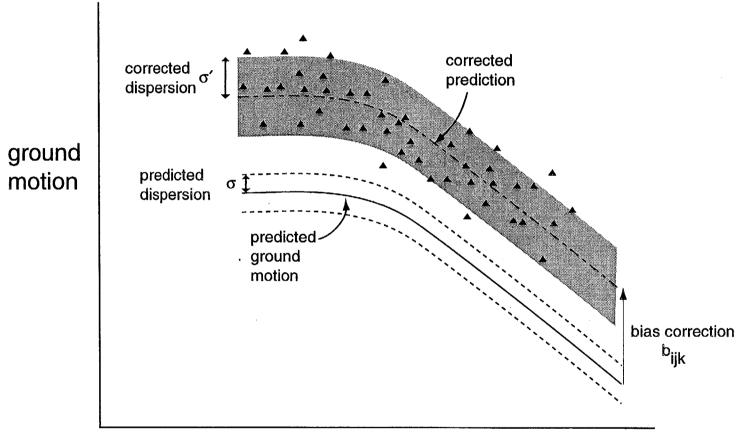
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# Table 5 p

All correction factors and slope parameters were calculated for each row of the following table,
1) for data in the 0-105 km distance range
2) for data in the 0-20 km distance range

relation	h/z	pga	psv/ paa	pgv	hard rock G=1	soft rock G=2	unkn rock G=0	shal soil G=7	deep soil G=6	unkn soil G=5
BJF94	h	•	•		•	•	•			
BJF94	h	•	•					•	•	•
C89/94	h	•	•					•	•	•
C89	Z	•	•					•	•	•
C89	h			•				•	•	•
C89	Z			•				•	•	•
C90/94	h	•	•			•	•			
C90	Z	•	•			•	•	<u> </u>		
C90	h			•		•	•			
C90	Z			•		•	•	<u></u>		
C93/94	h	•	•		•					
I93	h	•	•		•	•	•			
JB88	h			•	<u> </u>			•	•	•
JB88	h			•		<u> </u>		•	•	•
SP96	h	•	• `		•	•	•	<u> </u>		
SP96	h	•	•					<b>_</b>	•	•
SP96	h	•	•					•	<u> </u>	
SP96	h			•	•	•	•	<b> </b>	<u> </u>	
SP96	h			•		<u> </u>		•	•	•
S93	h	•	•		•	•	•	ļ		<u> </u>
S93	Z	•	•					•	•	•
Sea96	h	•	•		•	•	•		<u> </u>	
Sea96	h	•	•					•	•	•

## Illustration of bias correction and dispersion correction



distance

# "Uncorrected" Predictive Relations

Predictive relations are of the form:

 $log(y) = f(M,R,G_i,C_j,D,F,T_k)$ , where

y = ground motion parameter (e.g. pga)

M = magnitude

R = distance

D = depth to basement

F =source mechanism term (we use strike – slip always)

 $G_i$  = site geology, i = 1,...,6

 $C_i$  = component of motion (j = 1 horiz, j = 2 vert(z))

$$T_k = period, k = 1, \dots, m$$

Predicted standard error of log(y) ("dispersion") is

 $\sigma(M, pga, G_i, C_i, T_k)$ 

For each combination of i, j, and k (site geology, component of motion, and period) there is a population  $P_{iik}$  of relevant data.  $P_{ijk}$  has  $N_{ijk}$  elements.

"Corrected" Predictive Relations

$$\log(y') = f(M, R, G_i, C_j, D, F, T_k) + b_{ijk}$$

where

b<sub>ijk</sub> ="bias correction" for site class i, component j, and period k

$$\sigma' := \sigma(M, pga, G_i, C_j, T_k) e_{ijk}$$

where

e<sub>ijk</sub> ="dispersion correction" for site class i, component j, and period k Calculation of correction factors - bias correction b<sub>ijk</sub>

Define observed residual:

 $r := \log_{10}(y_0) - \log_{10}(y_{ijk})$ 

where

y<sub>o</sub> = observed ground motion for site category i, component j, and period k

 $y_{ijk}$  = (uncorrected) predicted value of  $y_0$ 

Bias correction:

$$b_{ijk} := \frac{1}{N_{ijk}} \sum_{P_{ijk}} r$$

The bias correction is the mean residual taken over all data for site category i, component j, and period k Define demeaned residual:

$$\mathbf{r'} \coloneqq \mathbf{r} - \mathbf{b_{ijk}}$$

Population standard deviation of r' is:

$$\sigma_{p} \coloneqq \left(\frac{1}{N_{ijk}} \sum_{P_{ijk}} (r')^{2}\right)^{\frac{1}{2}}$$

Standard deviation of bias correction  $\mathsf{b}_{ijk}$  is :

$$\sigma_b \coloneqq N_{ijk}^{-1/2} \sigma_p$$

Calculation of correction factors - dispersion correction Objective : determine  $e_{ijk}$  so that  $\frac{r'}{r} = \frac{r'}{r}$  has unit variance over P::

 $\frac{\mathbf{r'}}{\sigma'} \equiv \frac{\mathbf{r'}}{\sigma \, \mathbf{e}_{ijk}}$  has unit variance over  $P_{ijk}$ 

where

- r' = demeaned residual for  $P_{ijk}$
- $\sigma$  = uncorrected dispersion
- $\sigma'$  = corrected dispersion

 $e_{ijk} = \sqrt{v_{ijk}}$ 

where

$$v_{ijk} = \text{variance of } \mathbf{r'}/\sigma$$
  
$$\coloneqq \left(\frac{1}{N_{ijk}} \sum_{P_{ijk}} \left(\frac{\mathbf{r'}}{\sigma}\right)^2\right)$$

#### Significance of dispersion correction

Method 1: standard deviation of standard deviation

$$\sigma_{e} \coloneqq \left(\frac{N_{ijk} - 1}{2}\right)^{1/2} \frac{e_{ijk}}{N_{ijk}}$$

Method 2: chi-squared test

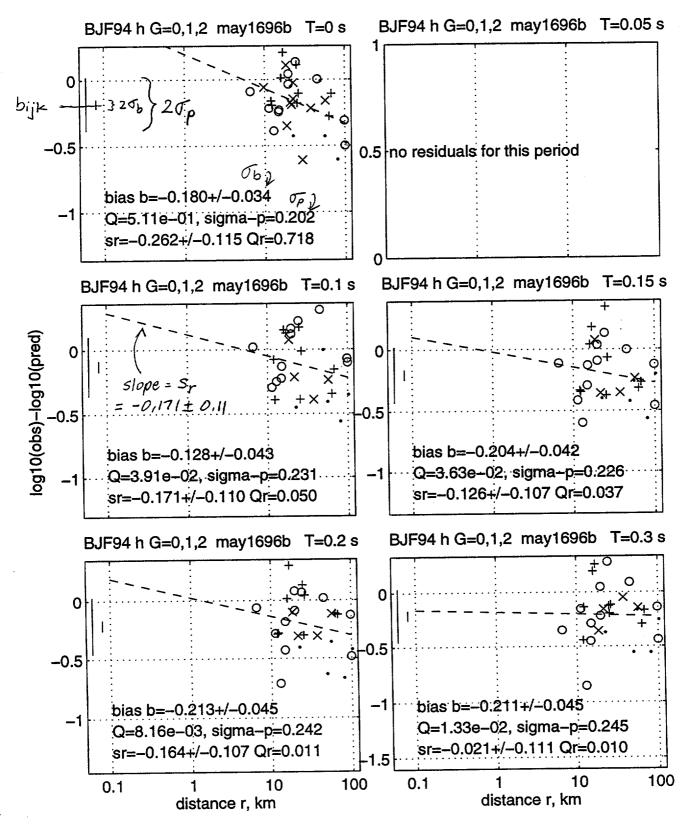
Observed chi - squared :=  $\chi_o^2 = \sum_{P_{ijk}} \left(\frac{r'}{\sigma}\right)^2$ 

Q statistic :

$$Q(\chi_0^2 | v) := 1 - P(v/2, \chi_0^2/2)$$

where

P(a, x) is incomplete Gamma function v = number of degrees of freedom = N<sub>ijk</sub> -1 Q is the probability of obtaining, from a set of residuals drawn from a population having dispersion  $\sigma$ ,  $\chi^2 > \chi_0^2$   $Q \rightarrow 1 \Rightarrow \sigma$ , predicted dispersion, is too big  $Q \rightarrow 0 \Rightarrow \sigma$ , predicted dispersion, is too small



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Table 9. Correction factors for each predictive relation, determined from data at all distances.

BJF94 h G=0,1,2 T(s) bijk	may2196b sigma-b	sigma-p	eijk	at mar a	0	27
0.00 -0.180 0.05 -	0.034	0.202	0.973	sigma-e 0.115 -	Q 5.11e-01 - 0	N 35
0.10 -0.128 0.15 -0.204	0.043 0.042	0.231 0.226	1.210 1.215	0.156	3.91e-02	29
0.20 -0.213	0.045	0.242	1.301	0.157 0.168	3.63e-02 8.16e-03	29 29
0.30 -0.211	0.045	0.245	1.275	0.164	1.33e-02	29
0.40 -0.190	0.042	0.228	1.139	0.147	1.06e-01	29
0.50 -0.157	0.040	0.214	1.031	0.133	3.25e-01	29
0.75 -0.160	0.046	0.246	1.117	0.144	1.38e-01	29
1.00 - 0.164	0.049	0.265	1.150	0.148	9.20e-02	29
1.50 -0.116 2.00 -0.219	0.061 0.074	0.291	1.201	0.173	5.92e-02	23
BJF94 h G=5,6,7	may2196b	0.338	1.363	0.205	6.64e-03	21
T(s) bijk	sigma-b	sigma-p	eijk	sigma-e	0	NT
0.00 -0.083	0.021	0.204	0.981	0.072	Q 5.55e-01	N 93
0.05 -	-	-	-	-	- 0	
0.10 -0.040	0.024	0.225	1.179	0.088	7.34e-03	89
0.15 -0.065	0.025	0.238	1.284	0.096	8.89e-05	89
0.20 -0.087	0.026	0.247	1.330	0.099	7.97e-06	89
$\begin{array}{rrr} 0.30 & -0.118 \\ 0.40 & -0.139 \end{array}$	0.024.	0.229	1.193	0.089	4.42e-03	89
0.40 - 0.139 0.50 - 0.099	0.026 0.027	0.245 0.256	$1.224 \\ 1.235$	0.091 0.092	1.28e-03 8.14e-04	89
0.75 -0.110	0.034	0.318	1.443	0.108	6.46e-09	89 89
1.00 -0.122	0.034	0.323	1.397	0.104	1.39e-07	89
1.50 -0.084	0.035	0.322	1.329	0.102	1.39e-05	84
2.00 -0.084	0.038	0.333	1.346	0.107	1.12e-05	78
C89/94 h G=5,6,7						
T(s) bijk 0.00 -0.012	sigma-b	sigma-p	eijk	sigma-e	Q	N
0.00 -0.012 0.05 0.090	0.019 0.022	0.188 0.195	0.973 1.021	0.071	5.96e-01	93
0.10 0.064	0.024	0.222	1.021	0.081 0.079	3.45e-01 1.67e-01	78 89
0.15 0.022	0.025	0.240	1.107	0.082	6.39e-02	89
0.20 0.003	0.026	0.249	1.148	0.086	2.00e-02	89
0.30 -0.027	0.023	0.221	1.017	0.076	3.60e-01	89
0.40 -0.030	0.025	0.238	1.097	0.082	8.11e-02	89
0.50 -0.003	0.026	0.242	1.116	0.083	5.05e-02	89
0.75 -0.042 1.00 -0.064	0.033	0.310	1.427	0.106	1.97e-08	89
1.50 -0.043	0.033 0.032	0.309 0.243	$1.423 \\ 1.117$	0.106 0.103	2.66e-08	89
2.00 -0.017	0.032	0.242	1.116	0.105	8.26e-02 8.66e-02	58 56
C89 z G=5,6,7	may2196b	0.212	*****	0.100	0.000-02	50
T(s) bijk	sigma-b	sigma-p	eijk	sigma-e	Q	N
0.00 -0.008	0.024	0.223	0.904	0.068	8.78e-01	88
0.05 0.179	0.031	0.280	1.040	0.082	2.66e-01	79
0.10 -0.103 0.15 0.023	0.036	0.327	1.215	0.093	2.38e-03	84
0.20 0.078	0.028 0.030	0.257 0.272	0.956 1.012	0.073	6.71e-01	84
0.30 0.197	0.031	0.272	1.012 1.044	0.078 0.080	3.89e-01 2.44e-01	84 84
0.40 0.070	0.035	0.321	1.190	0.091	5.87e-03	84 84
0.50 -0.010	0.035	0.317	1.179	0.090	8.62e-03	84
0.75 -0.100	0.039	0.346	1.285	0.102	1.87e-04	79
1.00 -0.078	0.041	0.357	1.325	0.107	4.33e-05	75
1.50 -0.152 2.00 -0.161	0.053	0.378	1.405	0.138	2.86e-05	51
2.00 -0.161 C89V h G=5,6,7	0.051 may1696c	0.351	1.303	0.133	1.45e-03	47
T(s) bijk	sigma-b	sigma-p	eijk	sigma-e	Q	N
pk vel 0.026	0.026	0.200	1.168	0.107	2.67e-02	59
C89V z G=5,6,7	may1696c				2.0.0 02	
T(s) bijk	sigma-b	sigma-p	eijk	sigma-e	Q	N
pk vel 0.029	0.027	0.255	1.129	0.085	3.57e-02	88
C90/94 h G=0,2	may2196b					

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Slope parameters (not corrections)

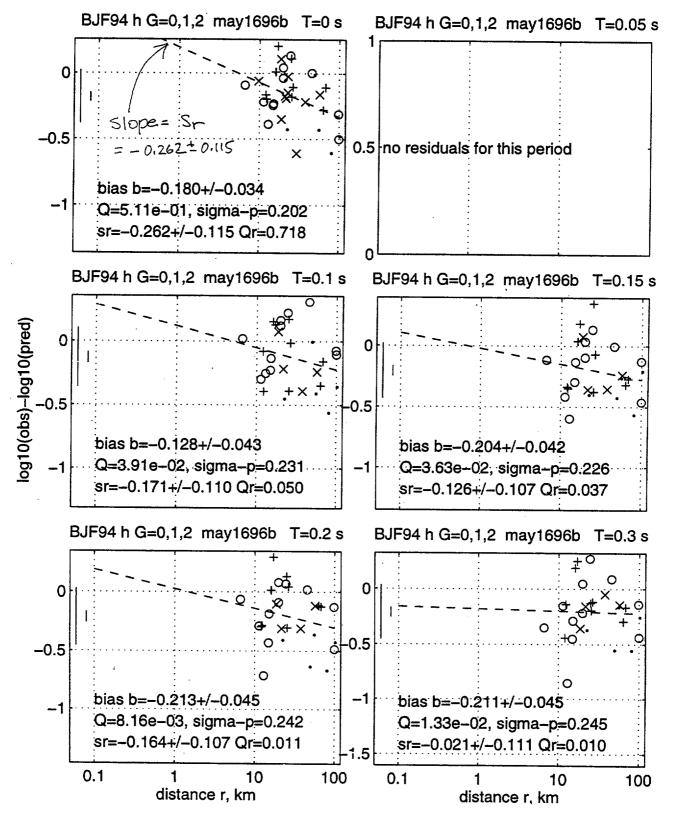
Distance dependence of residuals

For each population  $P_{ijk}$ , we fit a straight line through residuals r as a function of  $log_{10}(R)$ , where

 $R = r_{rup} \text{ (rupture distance, used by Idriss and Sadigh et al)}$   $r_{seis} \text{ (seismogenic distance, used by Campbell)}$   $\sqrt{5^2 + r_{jb}^2} \text{ (Joyner - Boore distance plus 5 km}$ pseudodepth, for BJF94, JB88, SP96, and SEA96)

We obtain :

 $s_r = slope$   $\sigma_r = standard deviation of slope$   $a_r = intercept$   $\sigma_{ar} = standard deviation of intercept$  $Q_r = \chi^2$  goodness of fit parameter



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Table 10. Distance dependences for each predictive relation, determined from data at all distances.

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T(s) ar 0.00 1.93e-01	sigma-ar 1.68e-01	sr -2.62e-01	sigma-sr 1.15e-01	cas -1.89e-02	ras -0.978	Qr 7.18e-01	N 35
0.05 -	-	-	-	-	-	-	0
0.10 1.20e-01		-1.71e-01 -1.26e-01			-0.976 -0.976	5.03e-02 3.75e-02	29 29
0.15 -2.12e-02 0.20 2.47e-02		-1.64e-01			-0.976	1.05e-02	29
0.20 - 1.80e - 01		-2.10e-02			-0.976	9.67e-03	29
0.40 -1.61e-01		-2.00e-02			-0.976	8.47e-02	29
0.50 -1.44e-01		-8.72e-03	1.20e-01	-2.07e-02	-0.976	2.79e-01	29
0.75 8.75e-02		-1.70e-01	1.27e-01		-0.976	1.55e-01	29
1.00 3.62e-01		-3.63e-01			-0.976	2.74e-01	29
1.50 2.30e-01		-2.50e-01			-0.978	7.30e-02	23
2.00 1.80e-01		-2.94e-01		-4.54e-02	-0.977	9.36e-03	21
BJF94 h G=5,6,7 T(s) ar	sigma-ar	Distance d	sigma-sr	cas	ras	Qr	N
0.00  1.60e-01	-	-2.01e-01		-4.23e-03	-0.958	8.35e-01	93
0.05 -	7.400 02	2.010 01	-	-	_	-	0
0.10 9.30e-02	7.02e-02	-1.11e-01	5.63e-02	-3.79e-03	-0.958	1.15e-02	89
0.15 6.22e-02		-1.07e-01			-0.958	1.53e-04	89
0.20 1.63e-02		-8.61e-02		-3.58e-03	-0.958	1.04e-05	89
0.30 2.06e-02		-1.16e-01			-0.958	7.38e-03	89
0.40 - 2.23e - 02		-9.78e-02		-4.15e-03	-0.958	1.71e-03	89
0.50 3.16e-02		-1.09e-01		-4.45e-03	-0.958	1.19e-03 2.18e-08	89 89
0.75 7.86e-02		-1.58e-01 -1.71e-01		-5.04e-03 -5.53e-03	-0.958 -0.958	4.95e-07	89
1.00 8.32e-02 1.50 1.51e-01		-2.02e-01		-7.12e-03	-0.960	4.78e-05	84
2.00 3.36e-01		-3.65e-01		-8.18e-03	-0.961	5.78e-04	78
C89/94 h G=5,6,7				0.200 00	0.00		
T(s) ar	sigma-ar	sr	sigma-sr	cas	ras	Qr	N
0.00 -8.65e-02	6.20e-02	5.85e-02		-3.11e-03	-0.948	6.11e-01	93
0.05 4.58e-02	7.04e-02	3.90e-02		-3.92e-03	-0.952	3.28e-01	78
0.10 3.31e-02	7.11e-02	2.59e-02		-3.86e-03	-0.951	1.52e-01	89
0.15 -8.40e-02		8.93e-02		-4.19e-03	-0.951	7.38e-02	89
0.20 -1.23e-01	7.41e-02	1.07e-01		-4.19e-03	-0.951	2.72e-02	89
0.30 -7.74e-02	7.41e-02			-4.19e-03	-0.951 -0.951	3.46e-01 7.24e-02	89 89
0.40 -6.15e-02	7.41e-02	2.63e-02 8.96e-04		-4.19e-03 -4.19e-03	-0.951	4.34e-02	89
0.50 -3.76e-03 0.75 6.59e-02	7.41e-02	-9.15e-02		-4.19e-03	-0.951	2.55e-08	89
1.00 4.38e-02		-9.07e-02		-4.19e-03	-0.951	3.41e-08	89
1.50 -4.34e-02		6.45e-04	8.56e-02	-7.97e-03	-0.956	6.96e-02	58
2.00 -7.75e-03		-8.92e-03		-8.43e-03	-0.956	7.31e-02	56
C89 z G=5,6,7	may2196b	Distance d					
T(s) ar	sigma-ar	sr	sigma-sr	cas	ras	Qr	N
0.00 -1.12e-01			6.92e-02	-5.73e-03		8.89e-01	88 79
0.05 2.61e-01		-7.01e-02		-7.84e-03 -7.25e-03	-0.953 -0.953	2.58e-01 1.04e-01	84
0.10 -5.69e-01 0.15 -1.86e-01		3.97e-01 1.78e-01		-7.25e-03	-0.953	7.87e-01	84
0.15 -1.88e-01 0.20 -2.97e-01				-7.25e-03	-0.953	8.36e-01	84
0.30 -2.47e-01		3.78e-01		-7.25e-03	-0.953	8.59e-01	84
0.40 -4.32e-01		4.27e-01	7.86e-02	-7.25e-03	-0.953	2.70e-01	84
0.50 -5.24e-01				-7.25e-03	-0.953	3.71e-01	84
0.75 -7.52e-01				-8.55e-03	-0.956	2.11e-01	79
1.00 -6.60e-01				-9.15e-03	-0.956	2.44e-02	75
1.50 -7.38e-01				-1.41e-02	-0.956	5.12e-03 3.13e-02	51 47
2.00 -6.72e-01				-1.60e-02	-0.957	5.13e-02	41
C89V h G=5, 6, 7	may1696c		dependence sigma-sr		ras	Qr	N
T(s) ar pk vl -8.05e-02	sigma-ar 7.59e-02					3.15e-02	59
C89V z G=5,6,7	may1696c		dependence				-
T(s) ar	sigma-ar		sigma-sr		ras	Qr	N
pk vl -3.78e-02	2 7.94e-02				-0.953	3.39e-02	88
C90/94 h G=0,2	may2196b	Distance	dependence	:			

Table 10 p1/4

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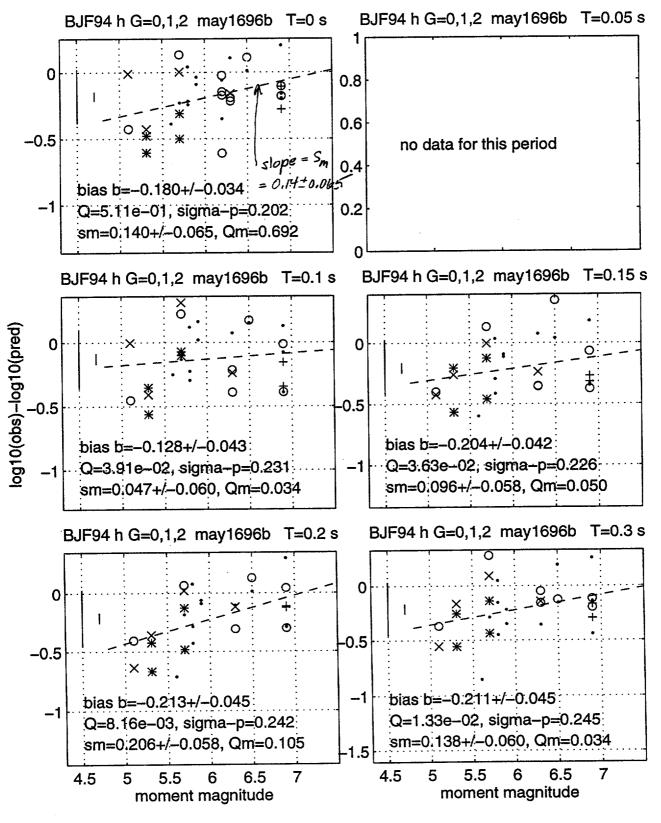
## More slope parameters (not corrections)

#### Magnitude dependence of residuals

For each population  $P_{ijk}$ , we fit a straight line through residuals r as a function of moment magnitude, M

We obtain :

 $s_m = slope$   $\sigma_m = standard deviation of slope$   $a_m = intercept$   $\sigma_{am} = standard deviation of intercept$  $Q_m = \chi^2$  goodness of fit parameter



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Table 11. Magnitude dependences for each predictive relation, determined from data at all distances.

BJF94 h G=0,1,2 may1196b Magnitude dependence T(s) am sigma-am s sigma-am cas cas cas com s com n 0.00 -1.03e+00 3.96e-01 1.40e-01 5.48e-02 -2.05e-02 -0.995 3.98e-02 29 0.15 -7.48e-01 3.54e-01 9.55e-02 5.98e-02 -2.17e-02 -0.995 3.98e-02 29 0.20 -1.46e+00 3.54e-01 9.55e-02 5.98e-02 -2.05e-02 -0.995 3.98e-02 29 0.30 -1.05e+00 3.54e-01 1.65a-01 6.26e-02 -2.05e-02 -0.995 3.98e-02 29 0.30 -1.05e+00 3.54e-01 1.65a-01 6.26e-02 -2.15e-02 -0.995 3.98e-02 29 0.40 -1.18e+00 3.82e-01 1.65a-01 6.26e-02 -2.15e-02 -0.995 5.6.32e-01 29 0.59 -1.18e+00 3.82e-01 1.65a-01 6.26e-02 -2.15e-02 -0.995 5.6.32e-01 29 0.59 -1.08e+00 3.60e-01 1.40a-01 6.90e-02 -2.98e-02 -0.995 6.32e-01 29 0.59 -1.08e+00 3.60e-01 1.40a-01 8.36e-02 -4.30e-02 -0.995 6.5.2e-01 29 0.59 -1.08e+00 3.50e-01 1.70e-01 6.90e-02 -2.98e-02 -0.995 6.5.2e-01 29 0.50 -1.03e+00 5.18e-01 4.03a-01 8.36a-02 -4.30e-02 -0.995 4.55a-01 23 2.00 -2.70e+00 5.18e-01 4.03a-01 8.36a-02 -4.30e-02 -0.995 5.6.57e-01 23 0.00 -1.01e-01 3.59e-01 2.75e-03 5.76e-02 -2.07e-02 -0.998 5.26e-01 93 0.05 -0 -0 -0 98 1.98e-01 -1.42e-01 5.14e-02 -1.058e-02 -0.998 1.84e-02 89 0.15 8.17e-01 3.31e-01 -1.42e-01 5.14e-02 -1.65e-02 -0.998 1.84e-02 89 0.16 8.77e-01 3.32e-01 -1.39e-01 5.72e-02 -1.76e-02 -0.998 1.84e-02 89 0.30 4.79e-01 3.32e-01 -1.57a-01 5.72e-02 -1.76e-02 -0.998 1.92e-03 89 0.30 4.79e-01 3.52e-01 -7.57a-01 6.40e-02 -2.55e-02 -0.998 1.92e-03 89 0.30 5.56e-01 3.99e-01 -1.76e-01 5.74e-02 -0.998 1.92e-03 89 0.50 5.97e-01 3.58e-01 -1.76e-01 5.74e-02 -0.998 7.59e-08 80 0.50 5.97e-01 3.59e-01 -1.75e-01 5.78e-02 -0.998 7.59e-08 80 0.50 5.96e-01 3.99e-01 -1.75e-01 5.78e-02 -0.998 7.59e-08 80 0.50 5.97e-01 3.58e-01 -1.75e-01 5.78e-02 -0.998 7.59e-08 80 0.50 5.97e-01 3.58e-01 -1.75e-01 5.78e-02 -0.998 7.59e-08 80 0.50 5.56e-01 3.75e-01 -1.73e-01 5.78e-02 -0.998 7.59e-08 80 0.50 5.97e-01 3.75e-01 -1.73e-01 5.78e-02 -0.998 7.59e-08 80 0.50 5.97e-01 3.75e-01 -1.73e-01 5.78e-02 -0.998 7.59e-08 80 0.50 1.58e+00 3.75e-01 -1.73e-01 5.78e-02 -0.998 8.458e-01 78 0.00 1.64e+00 3.6							
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	BJF94 h G=0,1,2	may2196b	Magnitude	dependence			
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	T(S) am	sigma-am			ras	Om	N
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2.00 2.49e+00 8.31e-01 -4.17e-01 1.31e-01 -1.08e-01 -0.999 1.06e-02 47 C89V h G=5,6,7 may1696c Magnitude dependence T(s) am sigma-am sm sigma-sm cas ras Qm N pk vl 3.38e-01 4.55e-01 -4.94e-02 7.19e-02 -3.27e-02 -0.999 2.36e-02 59 C89V z G=5,6,7 may1696c Magnitude dependence T(s) am sigma-am sm sigma-sm cas ras Qm N pk vl 1.47e+00 4.30e-01 -2.32e-01 6.91e-02 -2.97e-02 -0.998 1.30e-01 88				9.13e-02 -5.22e-02	-0.999	3.40e-03	75
C89V h G=5,6,7 may1696c Magnitude dependence T(s) am sigma-am sm sigma-sm cas ras Qm N pk vl 3.38e-01 4.55e-01 -4.94e-02 7.19e-02 -3.27e-02 -0.999 2.36e-02 59 C89V z G=5,6,7 may1696c Magnitude dependence T(s) am sigma-am sm sigma-sm cas ras Qm N pk vl 1.47e+00 4.30e-01 -2.32e-01 6.91e-02 -2.97e-02 -0.998 1.30e-01 88	1.50 3.16e+00	8.18e-01	-5.22e-01	1.29e-01 -1.05e-01	-0.999	1.28e-03	51
C89V h G=5,6,7 may1696c Magnitude dependence T(s) am sigma-am sm sigma-sm cas ras Qm N pk vl 3.38e-01 4.55e-01 -4.94e-02 7.19e-02 -3.27e-02 -0.999 2.36e-02 59 C89V z G=5,6,7 may1696c Magnitude dependence T(s) am sigma-am sm sigma-sm cas ras Qm N pk vl 1.47e+00 4.30e-01 -2.32e-01 6.91e-02 -2.97e-02 -0.998 1.30e-01 88	2.00 2.49e+00	8.31e-01	-4.17e-01	1.31e-01 -1.08e-01	-0.999	1.06e-02	47
T(s)amsigma-amsmsigma-smcasrasQmNpk vl 3.38e-014.55e-01-4.94e-027.19e-02-3.27e-02-0.9992.36e-0259C89V z G=5,6,7may1696cMagnitude dependenceT(s)amsigma-amsmsigma-smcasrasQmNpk vl 1.47e+004.30e-01-2.32e-016.91e-02-2.97e-02-0.9981.30e-0188	C89V h G=5,6,7	may1696c	Magnitude			_	
pk vl 3.38e-01 4.55e-01 -4.94e-02 7.19e-02 -3.27e-02 -0.999 2.36e-02 59 C89V z G=5,6,7 may1696c Magnitude dependence T(s) am sigma-am sm sigma-sm cas ras Qm N pk vl 1.47e+00 4.30e-01 -2.32e-01 6.91e-02 -2.97e-02 -0.998 1.30e-01 88					ras	Om	N
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T(s) am sigma-am sm sigma-sm cas ras Qm N pk vl 1.47e+00 4.30e-01 -2.32e-01 6.91e-02 -2.97e-02 -0.998 1.30e-01 88					0.000	2.306-02	
pk vl 1.47e+00 4.30e-01 -2.32e-01 6.91e-02 -2.97e-02 -0.998 1.30e-01 88					***	0	ът
CJ0/J4 n G-0,2 may2130D magnitude dependence	-			donondonac	~0.998	1.306-01	88
	CJ0/J4 II G-0,2	may2130D	naynitude	dependence			

Table 11 p1/4

Table 12. Correction factors for each predictive relation and period, determined from data at distance less than or equal to 20 km.

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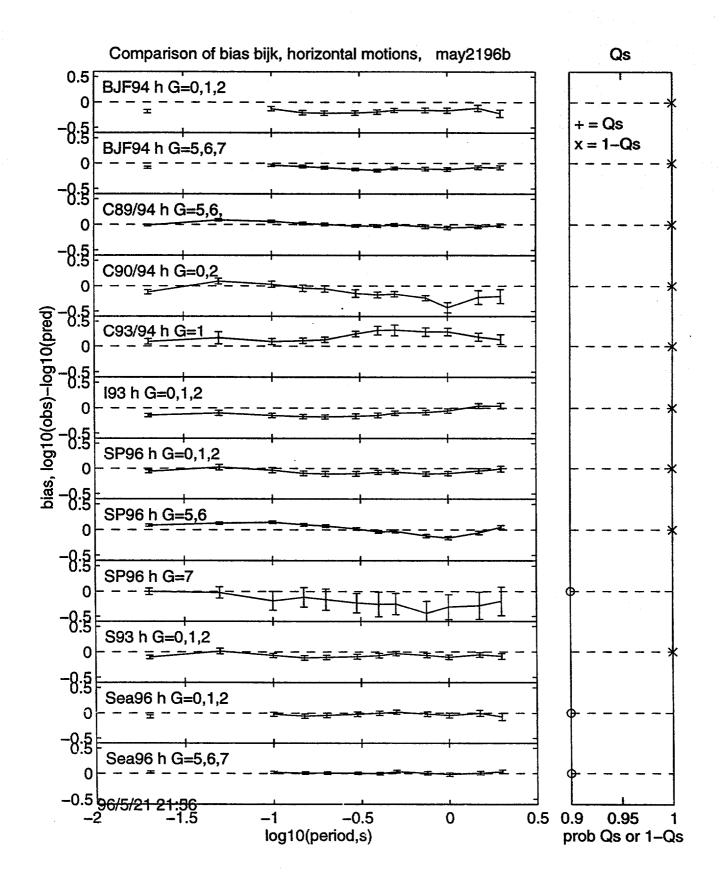
191

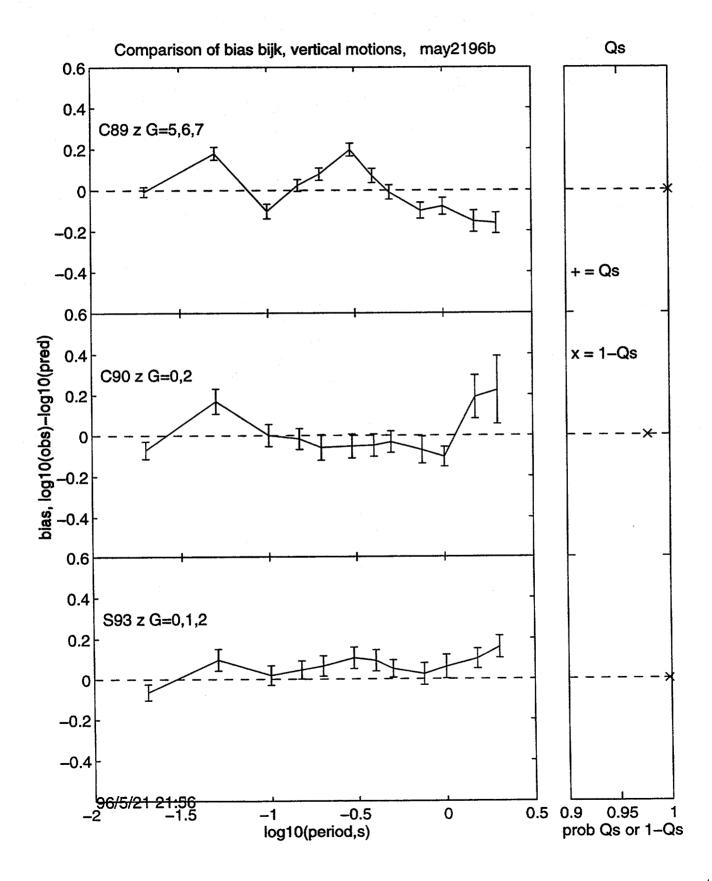
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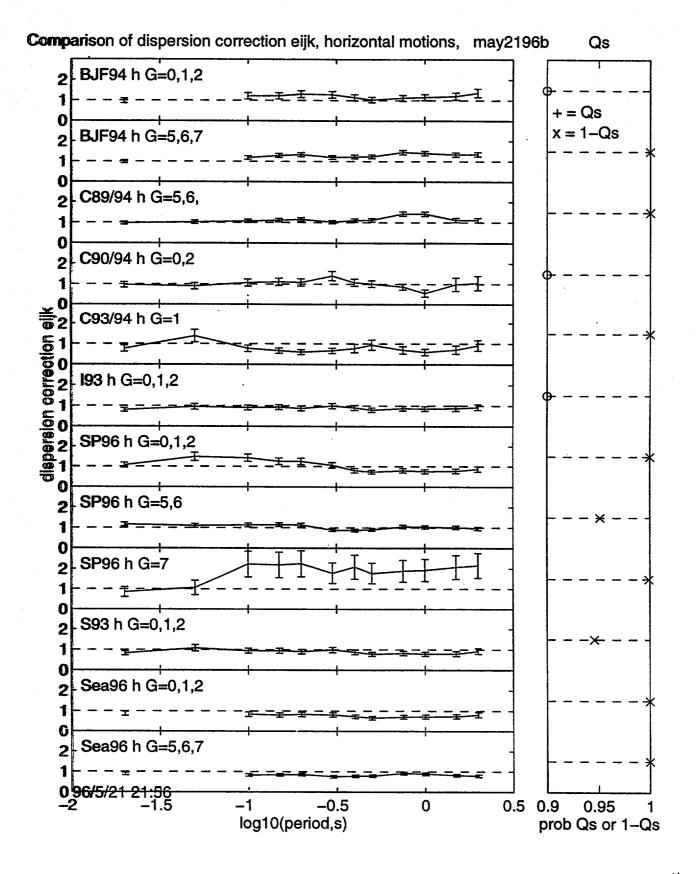
BJF94 h G=0,1,2	may2196c<=2	20				
T(s) bijk	sigma-b	sigma-p	eijk	sigma-e	Q	N
0.00 -0.115	0.044	0.165	0.793	0.144	7.87e-01	14
0.05 -	-	-	_	-	-	0
0.10 -0.059	0.054	0.188	0.984	0.192	3.92e-01	12
0.15 -0.166	0.064	0.223	1.200	0.235	9.95e-02	12
0.20 -0.171	0.072	0.248	1.334	0.261	2.99e-02	12
0.30 -0.229	0.084	0.292	1.519	0.297	3.59e-03	12
0.40 -0.195	0.080	0.278	1.391	0.272	1.64e-02	12
0.50 -0.168	0.069	0.239	1.154	0.226	1.42e-01	12
0.75 -0.095	0.068	0.237	1.075	0.210	2.41e-01	12
1.00 -0.050	0.064	0.221	0.959	0.187	4.41e-01	12
1.50 -0.056	0.085	0.281	1.159	0.236	1.40e-01	11
2.00 -0.175	0.100	0.331	1.338	0.272	3.24e-02	11
BJF94 h G=5,6,7	may2196c<=2					
T(s) bijk	sigma-b	sigma-p	eijk	sigma-e	Q	N
0.00 -0.035	0.023	0.169	0.811	0.076	9.72e-01	56
0.05 -	-	. –	-	-	-	0
0.10 -0.020	0.025	0.188	0.982	0.092	5.12e-01	56
0.15 -0.043	0.029	0.217	1.169	0.109	2.90e-02	56
0.20 -0.080	0.027	0.204	1.100	0.103	1.17e-01	56
0.30 -0.100	0.025	0.190	0.989	0.093	4.83e-01	56
0.40 -0.112	0.027	0.206	1.029	0.096	3.23e-01	56
0.50 -0.060	0.029	0.214	1.033	0.097	3.05e-01	56
0.75 -0.072	0.034	0.252	1.143	0.107	5.17e-02	56
1.00 -0.079	0.034	0.251	1.087	0.102	1.43e-01	56
1.50 -0.034	0.034	0.255	1.052	0.099	2.43e-01	55
2.00 -0.015	0.036	0.264	1.065	0.102	2.05e-01	53
C89/94 h G=5,6,7						
T(s) bijk	sigma-b	sigma-p	eijk	sigma-e	Q	N
0.00 -0.042	0.024	0.174	1.010	0.096	3.95e-01	54
0.05 0.066	0.026	0.187	0.980	0.096	5.16e-01	51
0.10 0.044	0.026	0.190	0.911	0.087	7.80e-01	54
0.15 -0.010	0.031	0.224	1.033	0.098	3.09e-01	54
0.20 -0.045	0.028	0.209	0.964	0.092	5.84e-01	54
0.30 -0.059	0.025	0.187	0.862	0.082	9.04e-01	54
0.40 -0.053	0.026	0.195	0.896	0.085	8.26e-01	54
0.50 -0.008	0.027	0.200	0.923	0.088	7.40e-01	54
0.75 -0.034	0.035	0.256	1.181	0.113	2.38e-02	54
1.00 -0.060	0.034	0.248	1.142	0.109	5.47e-02	54
1.50 -0.053	0.036	0.228	1.050	0.116	2.65e-01	40
2.00 -0.025	0.037	0.234	1.079	0.119	1.90e-01	40
C89 z G=5,6,7	may2196c<=	20				
T(s) bijk	sigma-b	sigma-p	eijk	sigma-e	Q	N
0.00 -0.026	0.034	0.245	0.992	0.097		51
0.05 0.200	0.040	0.282	1.047	0.105	2.63e-01	49
0.10 -0.185	0.049	0.352	1.306	0.128	9.35e-04	51
0.15 -0.021	0.039	0.276	1.027	0.101	3.33e-01	51
0.20 -0.017	0.037.	0.264	0.981	0.096	5.12e-01	51
0.30 0.090	0.039	0.279	1.038	0.102	2.93e-01	51
0.40 -0.054	0.043	0.309	1.147	0.112	5.38e-02	51
0.50 -0.126	0.041	0.296	1.098	0.108	1.27e-01	51
0.75 -0.237	0.040	0.285	1.057	0.105	2.32e-01	50
1.00 -0.206	0.041	0.287	1.064	0.106	2.13e-01	49
1.50 -0.261	0.057	0.343	1.273	0.148	7.99e-03	36
2.00 -0.239	0.052	0.309	1.148	0.133	7.84e-02	36
C89V h G=5,6,7	may1696e<=				-	
T(s) bijk	sigma-b	sigma-p	_	sigma-e	Q	N
pk vl 0.006	0.030	0.187	1.091	0.120	1.62e-01	40
C89V z G=5,6,7	may1696e<=	=20		•	-	
T(s) bijk	sigma-b	sigma-p			1 77-01	N E 1
pk vl 0.002	0.034	0.243	1.076	0.106	1.77e-01	51
C90/94 h G=0,2	may2196c<=	=20				

Table 12 p1/4

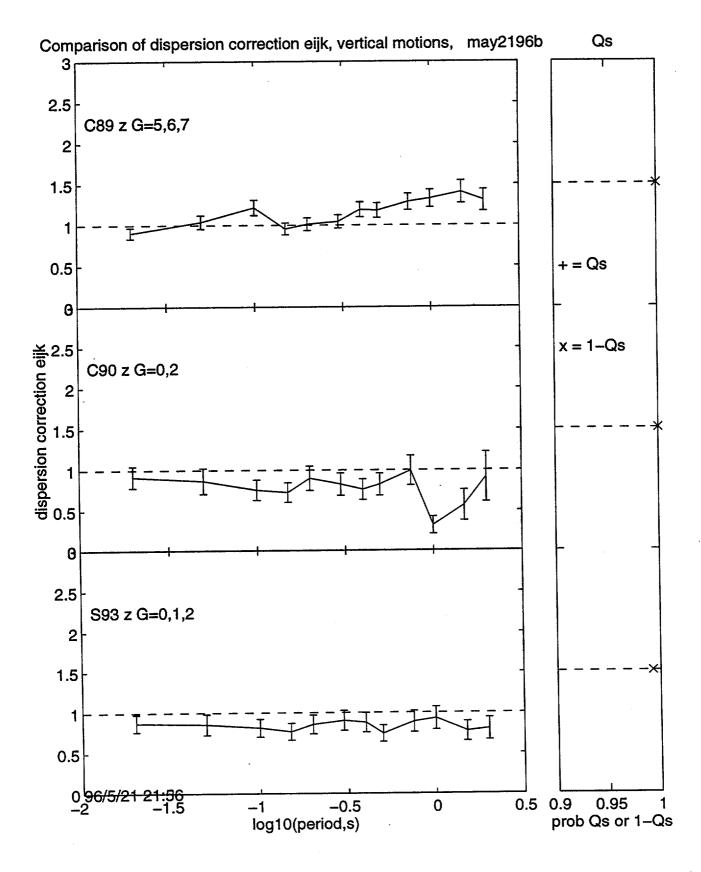




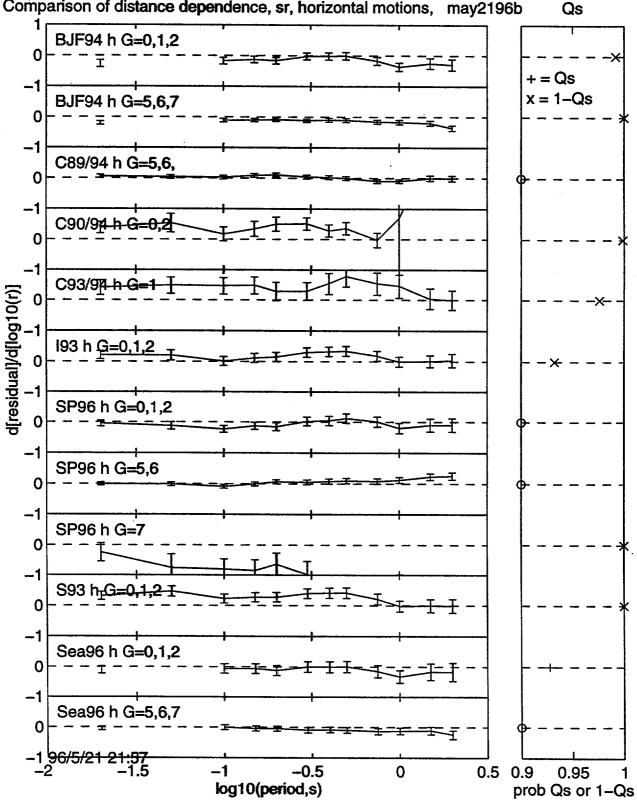
165



16 c

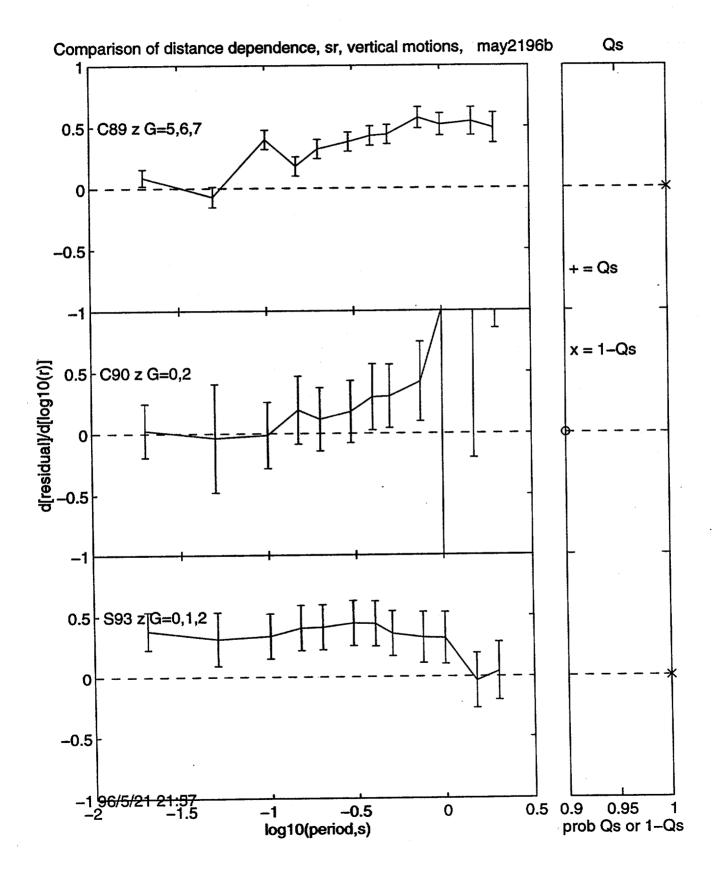


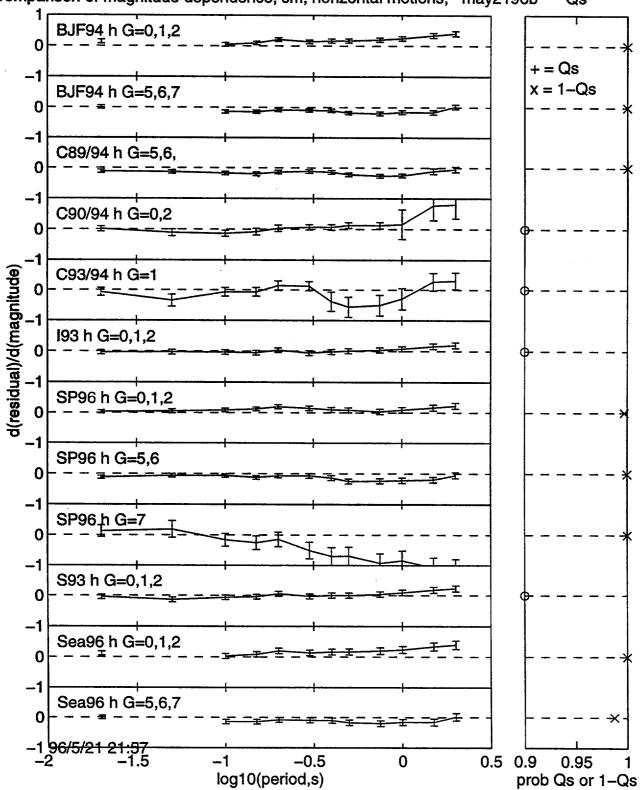
16 d



Comparison of distance dependence, sr, horizontal motions, may2196b

16 e

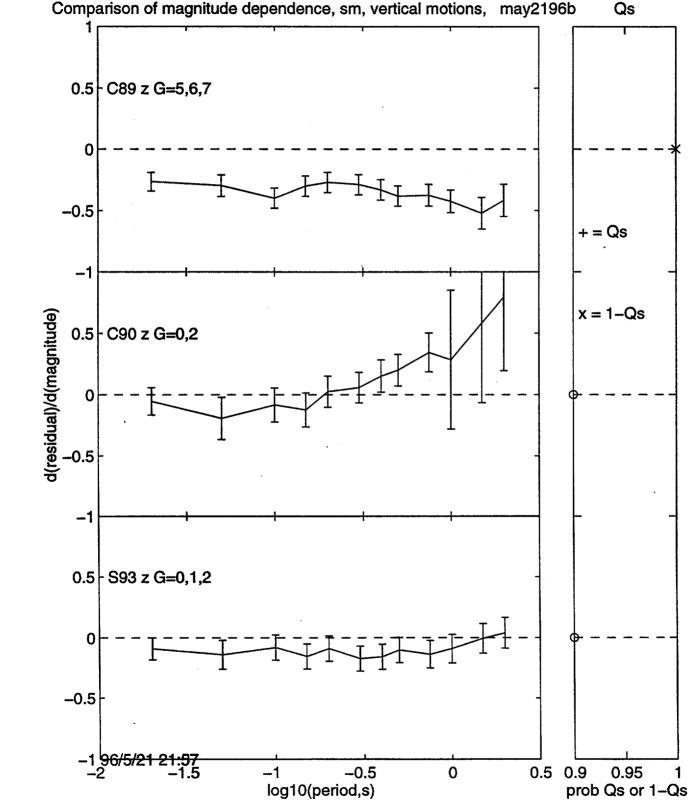




Comparison of magnitude dependence, sm, horizontal motions, may2196b Qs

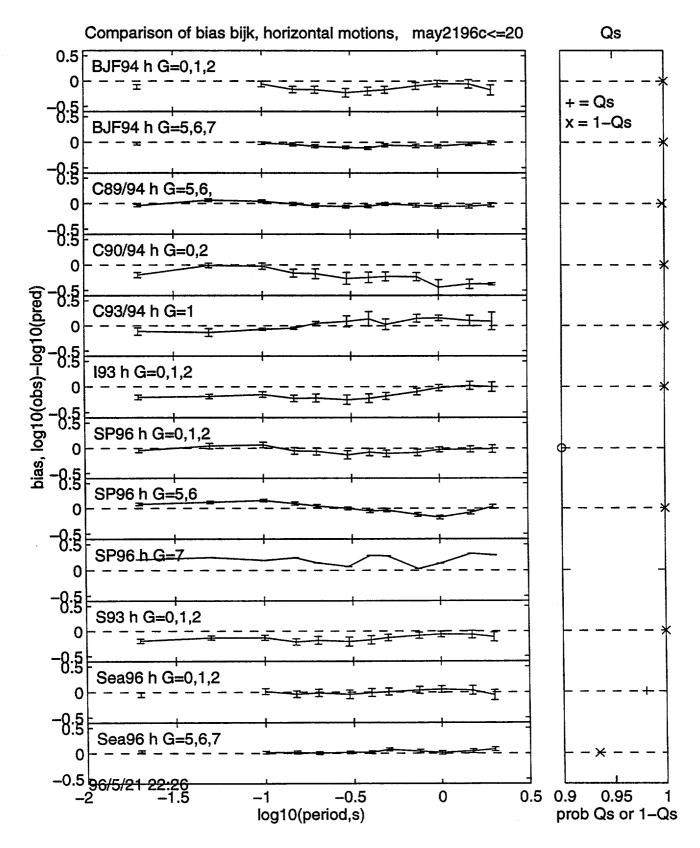
16g

257

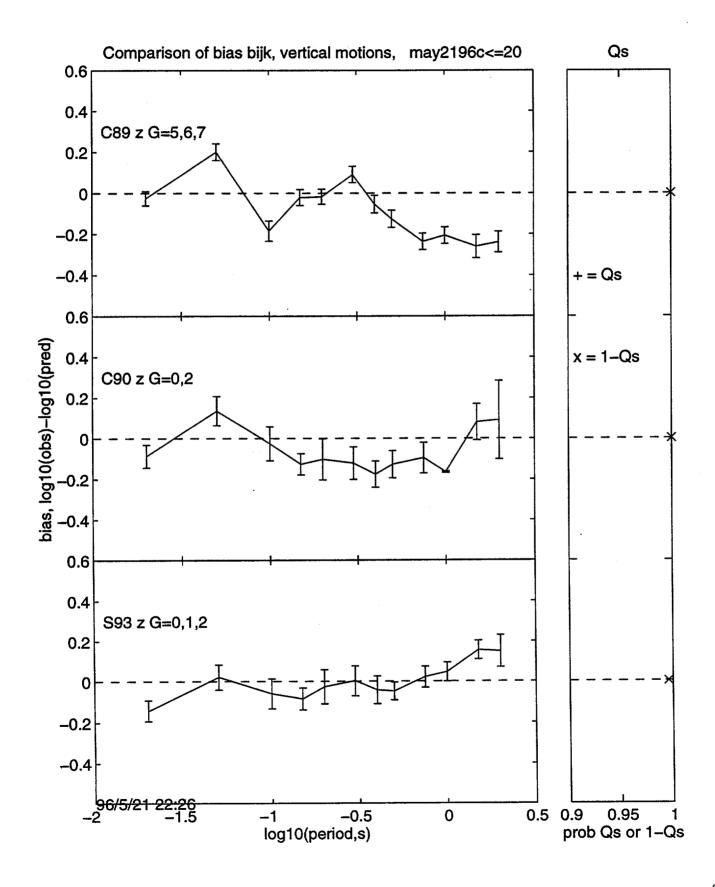


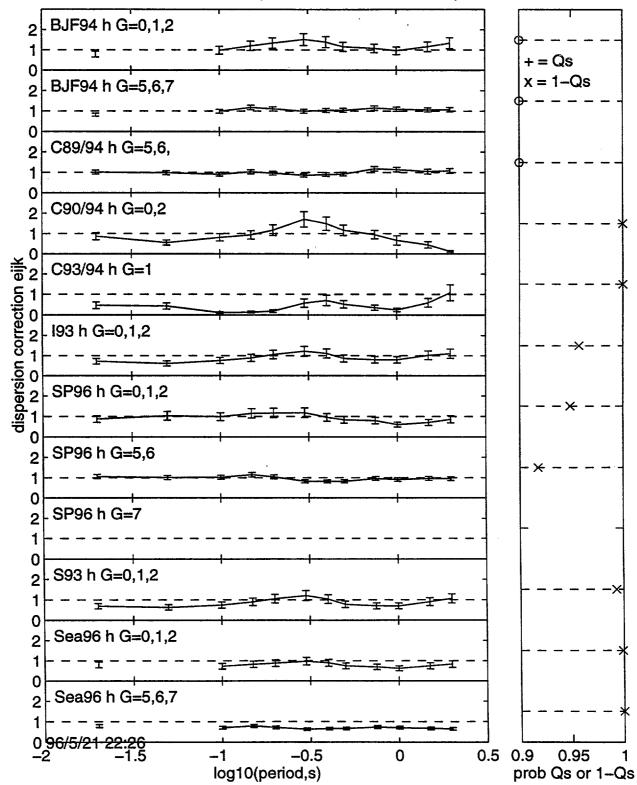
Comparison of magnitude dependence, sm, vertical motions, may2196b

25 Ps

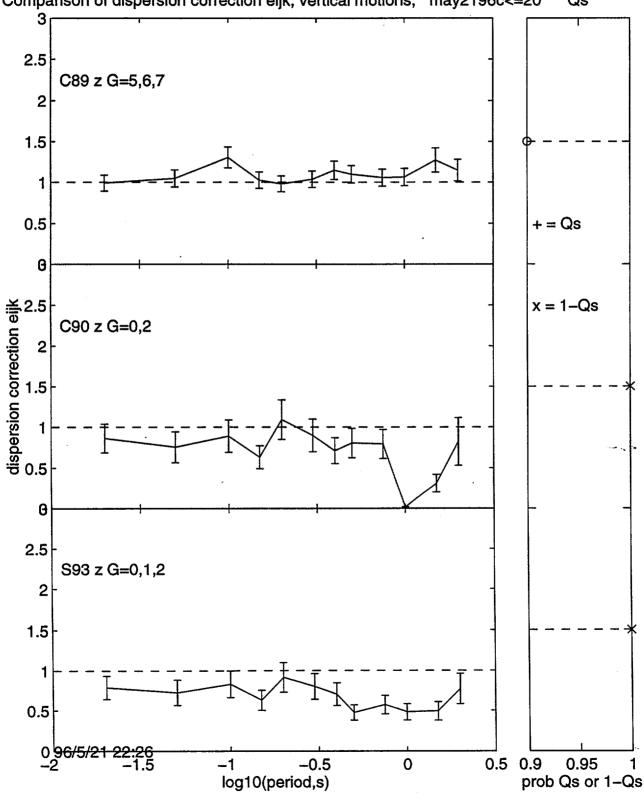


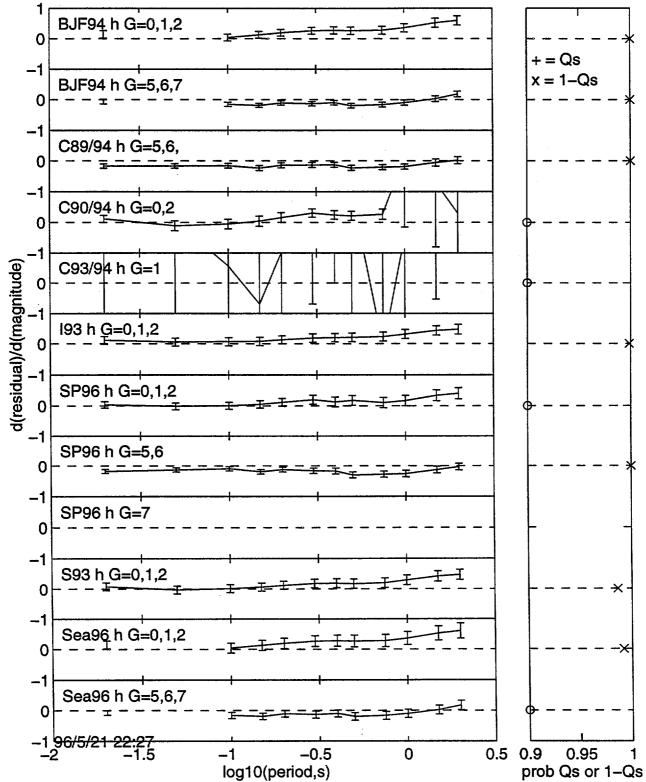
19a



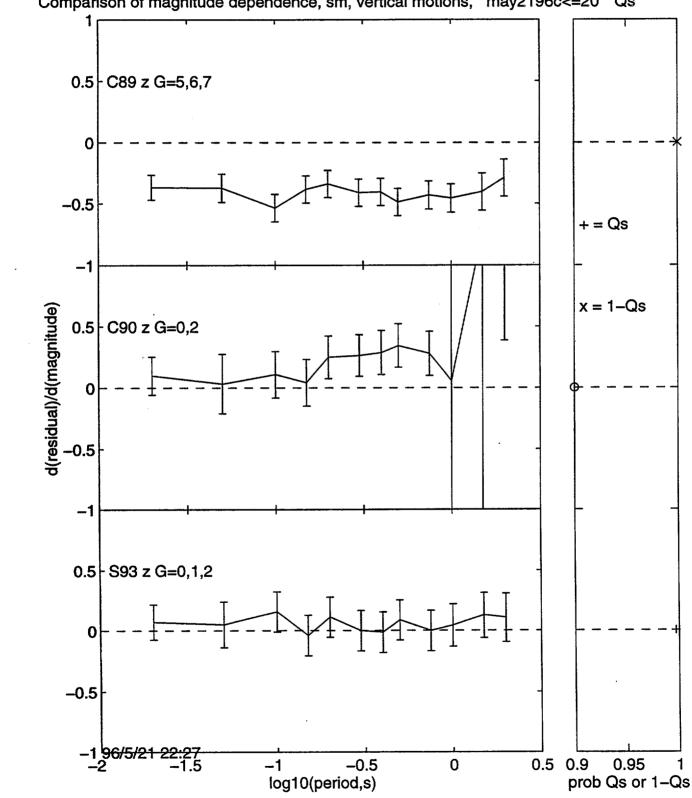


Comparison of dispersion correction eijk, horizontal motions, may2196c<=20 Qs





Comparison of magnitude dependence, sm, horizontal motions, may2196c<=20 Qs



#### Attenuation Relation for Normal Faulting Events

Norm Abrahamson

Jan 10, 1997

#### Approach

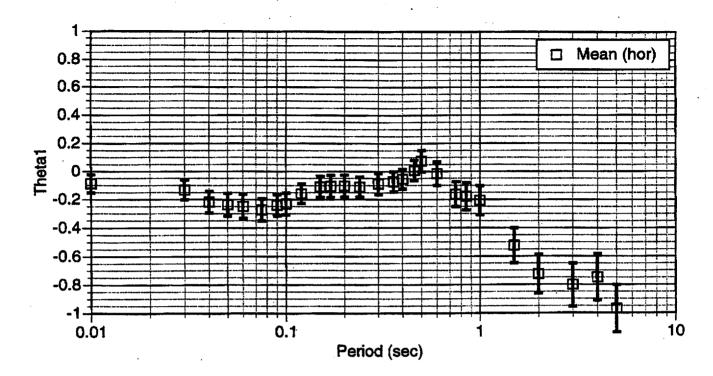
Compute residuals for normal faulting events (Spudich data set) - using Abrahamson and Silva (1996) strike-slip model

Use random effects model to estimate the mean residual Check magnitude and distance dependence of intra-event residuals Check magnitude dependence of inter-event residuals (event terms) Compare total standard error with previous model estimates

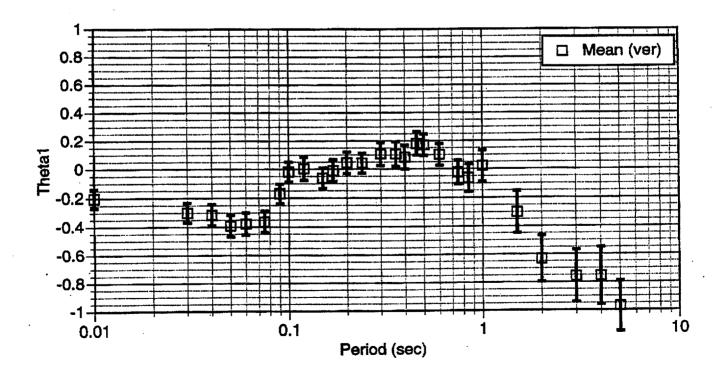
Data Set:

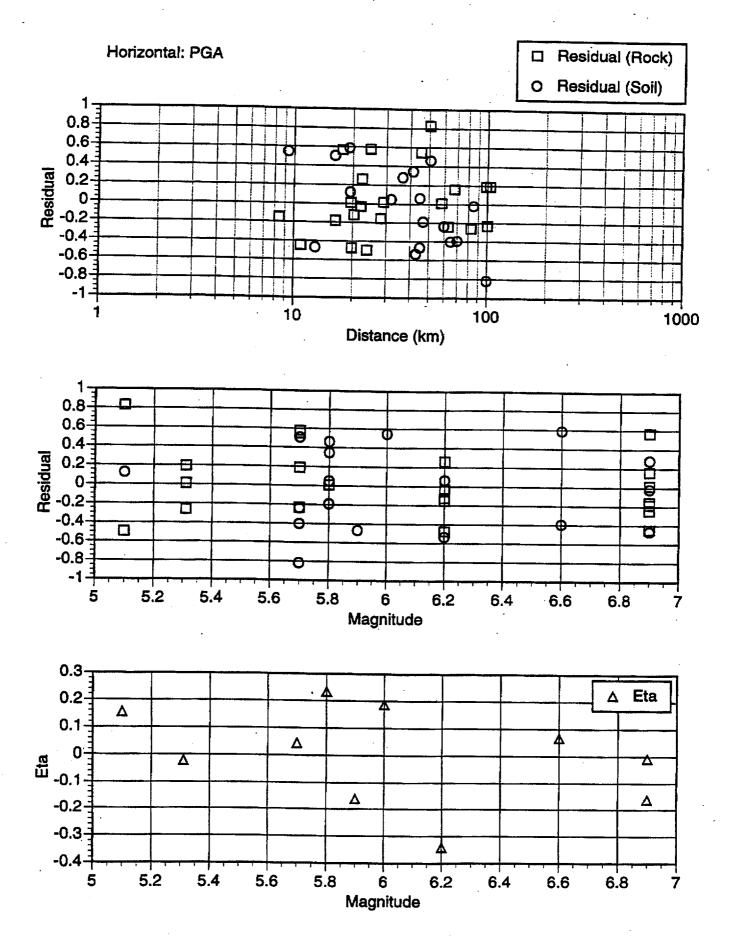
40 horizontal and 35 vertical recordings

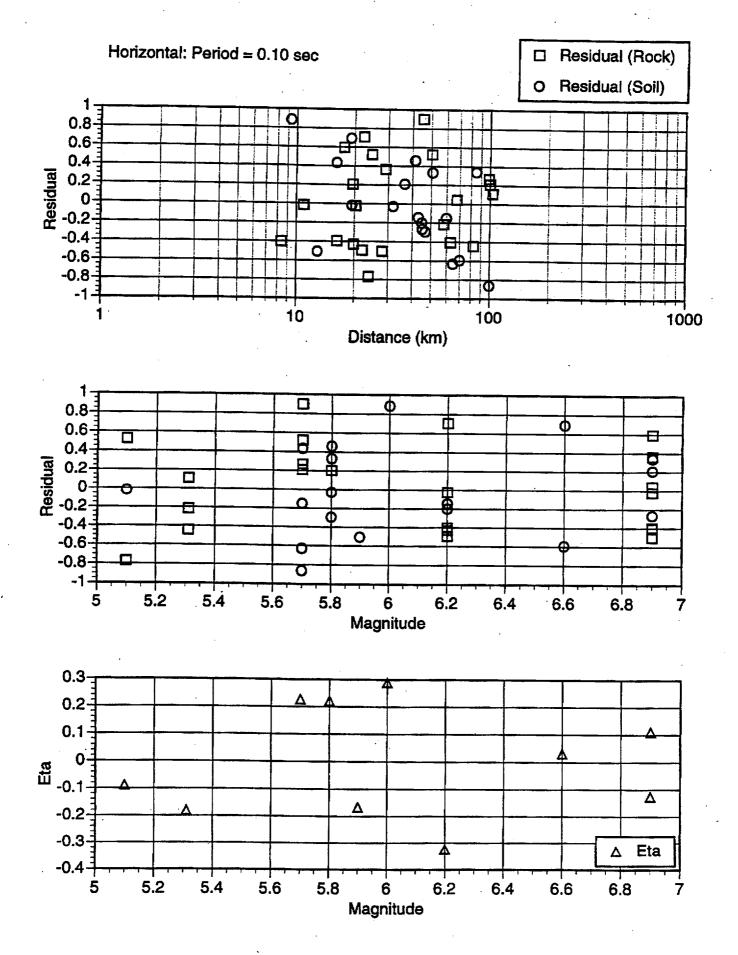


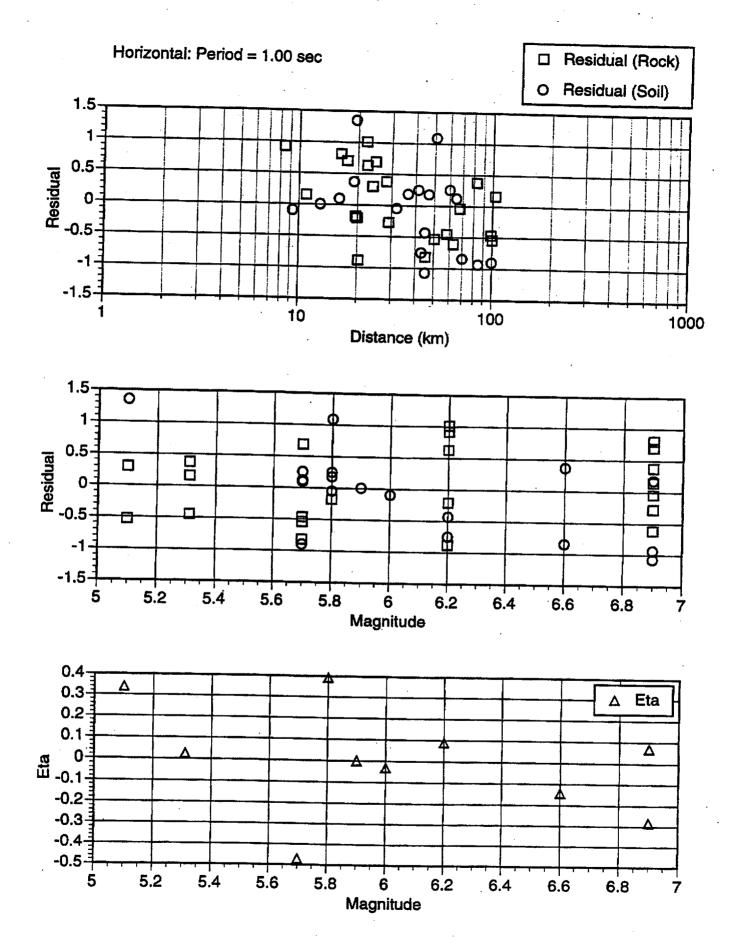


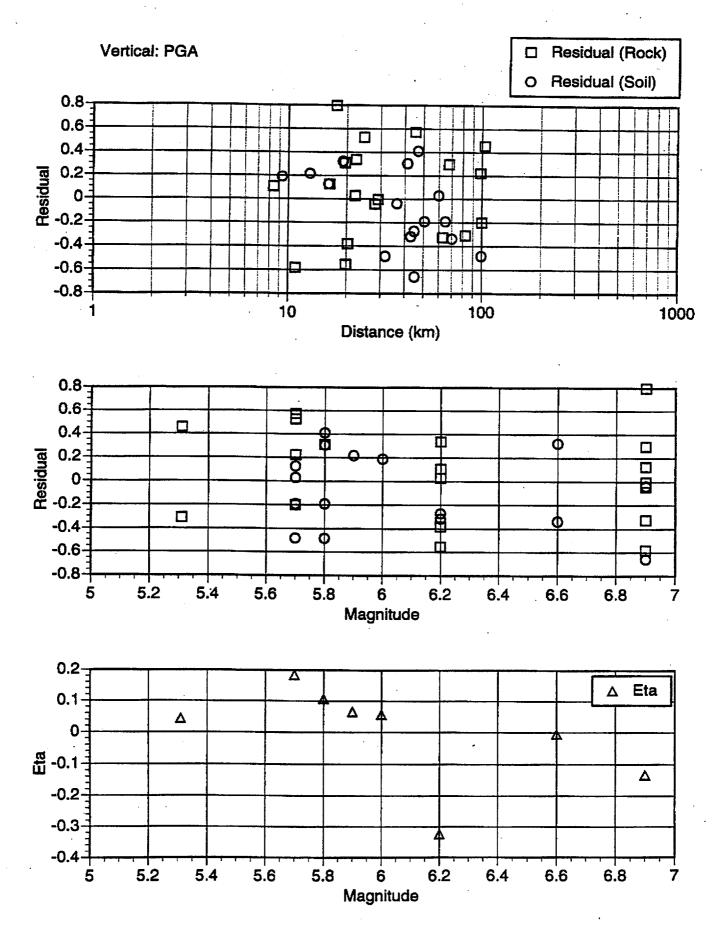
Vertical: All Sites, Random Effects

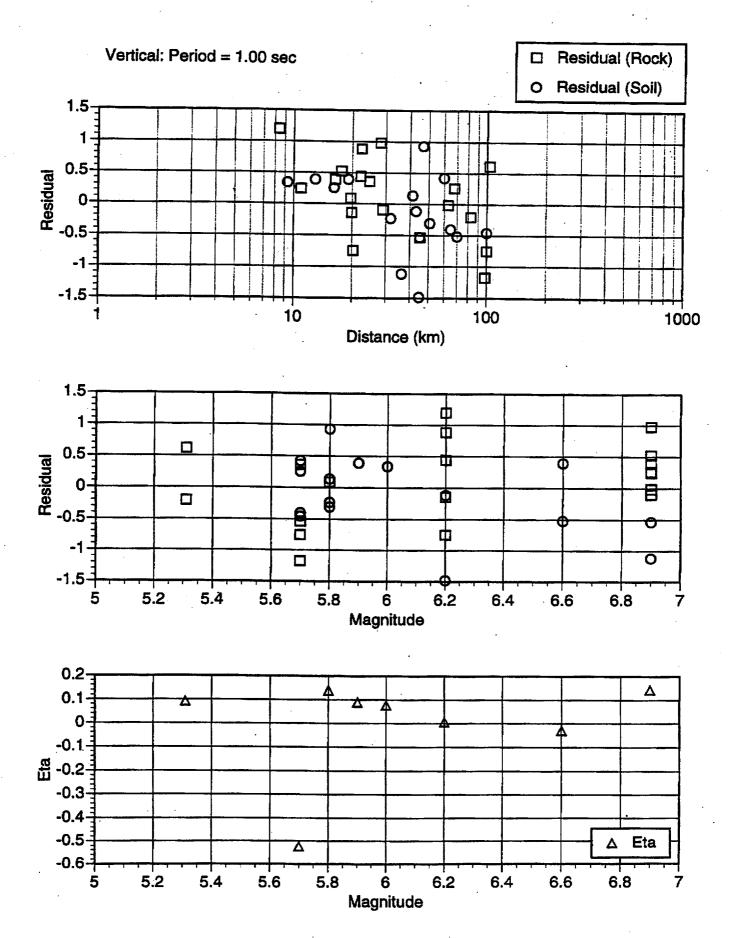












#### Style-of-Faulting factor for Normal Faulting Events for Abrahamson and Silva (1996) (in Natural Log units)

	He	oriz	Vert		
<u>Freq</u>	<u>Bias</u>	<u>σ Bias</u>	Bias	<u> </u>	
pga	-0.087	0.065	-0.203	0.065	
20.0	-0.236	0.081	-0.392	0.076	
10.0	-0.231	0.078	-0.018	0.070	
5.0	-0.104	0.078	0.045	0.078	
2.0	0.074	0.077	0.171	0.078	
1.0	-0.207	0.103	0.022	0.110	
0.5	-0.726	0.136	-0.632	0.164	

#### Standard Errors Ave Horizontal Component

freq	sigma	tau	se sigma	se tau	cov sigma tau	total sigma	se total sigma	A&S 96 total sigma
pga	0.41	0.24	0.05	0.10	-0.00046	0.48	0.06	0.55
20	0.51	0.25	0.07	0.12	-0.00099	0.57	0.08	0.56
10	0.49	0.28	0.06	0.12	-0.00093	0.56	0.08	0.59
5	0.50	0.24	0.06	0.12	-0.00088	0.55	0.07	0.62
2	0.49	0.17	0.06	0.12	-0.00073	0.52	0.06	0.66
1	0.65	0.36	0.08	0.16	-0.00280	0.74	0.14	0.70
0.5	0.86	0.37	0.11	0.21	-0.00760	0.94	0.21	0.74

### Vertical Component

freq	sigma	tau	se sigma	se tau	cov sigma tau	total sigma	se total sigma	A&S 96 total sigma
pga	0.38	0.21	0.05	0.10	-0.00035	0.43	0.05	0.55
20	0.45	0.34	0.06	0.13	-0.00080	0.56	0.10	0.56
10	0.41	0.34	0.06	0.13	-0.00059	0.53	0.09	0.59
5	0.45	0.17	0.06	0.12	-0.00057	0.48	0.06	0.62
2	0.46	0.25	0.06	0.12	-0.00071	0.52	0.07	0.66
1	0.65	0.31	0.09	0.17	-0.00270	0.72	0.14	0.70
0.5	0.97	0.39	0.13	0.25	-0.01220	1.05	0.28	0.74

# Smoothed Model Coefficients a14

Freq	Horiz	Vert
PGA	-0.16	-0.25
20	-0.16	-0.25
10	-0.16	-0.13
5	-0.12	0.00
2	-0.07	0.07
1	-0.20	-0.08
2	-0.40	-0.30

## Modeling Methods

Group	Method
USC	Specific Barrier Method
PEA	Stochastic Method with ω-2 Sub-Events
USGS	Stochastic Slip Functions Method
UNR	Composite Fractal Source Model
WCC	Broadband Green's Function Method
WCC	Broadband Green's Function Method
SCubed	Empirical Method from Nuclear Explosion Sources

.

Scenario	Fault	Length (km)	Width (km)	Dip	Rake	M	Dist. (km)
1	Paintbrush Canyon- Bow Ridge	14 to 15	14.2	45 to 70 W	-70 (Normal/LL)	6.31	PC: 4.5 BR: 2.5
2	Solitario Canyon	21±7	14.2	58±8W	-65±5 (Normal/LL)	6.48	1.0
3	Rock Valley	42	12	90±5	0 to -30 (LL/dip)	6.71	~25
4	Bare Mountain	18±4	14.2	45 to 70 E	-90 (Normal)	6.42	15.5
5	Furnace Creek	90±10	12	90	180 (RL)	7.04	~50
6	Solitario Canyon- Fatigue Wash- Windy Wash <sup>1</sup>	FW: 17 WW: 25	14.2	FW: 80 to 90 WW: -50 to -60	FW: -80 to -90 WW: -70 to -90 (Normal/LL)	~6.6 <sup>2</sup>	1.0

 Table 2.4 Selected scenario earthquakes.

1Volcanic triggered event with 2/3 displacement on Solitario Canyon, 1/3 on Fatigue Wash and Windy Wash.

<sup>2</sup> Based on an average fault rupture length of 25 km.

## YUCCA MOUNTAIN PROJECT

#### WORKSHOP 2

January 8 - 10, 1997

WALT SILVA

PACIFIC ENGINEERING and ANALYSIS

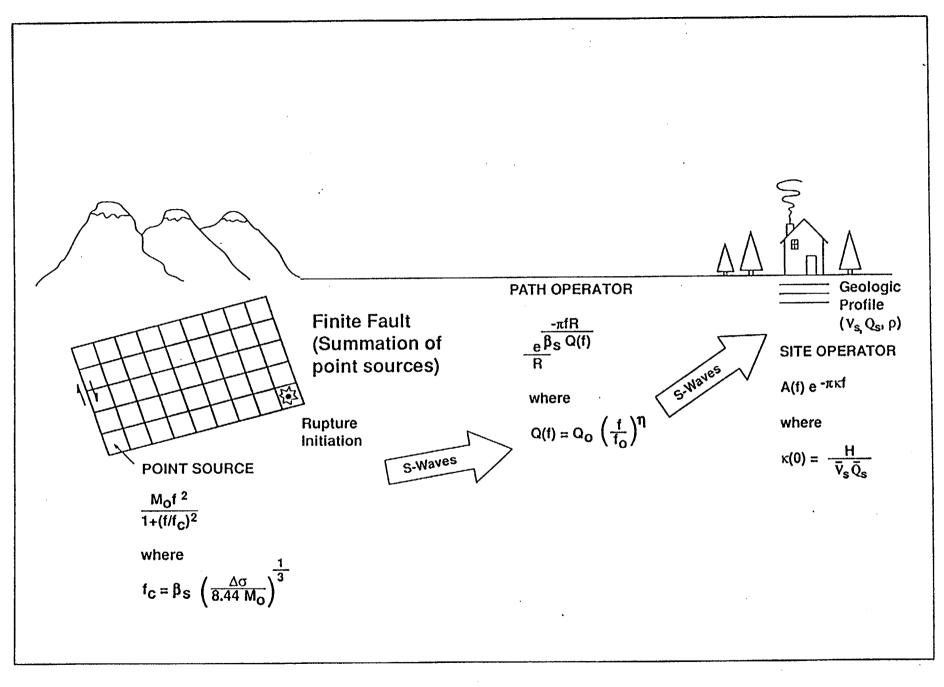


FIGURE 1. SCHEMATIC OF GROUND MOTION MODEL.

	POINT SOURCE SIMULATIONS								
М	$\Delta\sigma$ (bars)	Depth (km)	Kappa (sec)						
5.0	25	5	0.01						
5.5	50	10	0.02						
6.0	100	15	0.03						
6.5	200		0.04						
7.0		· · · · · · · · · · · · · · · · · · ·							
7.5									
8.0									

D(km): 1, 3, 5, 10, 20, 50, 75, 100, 150, 200

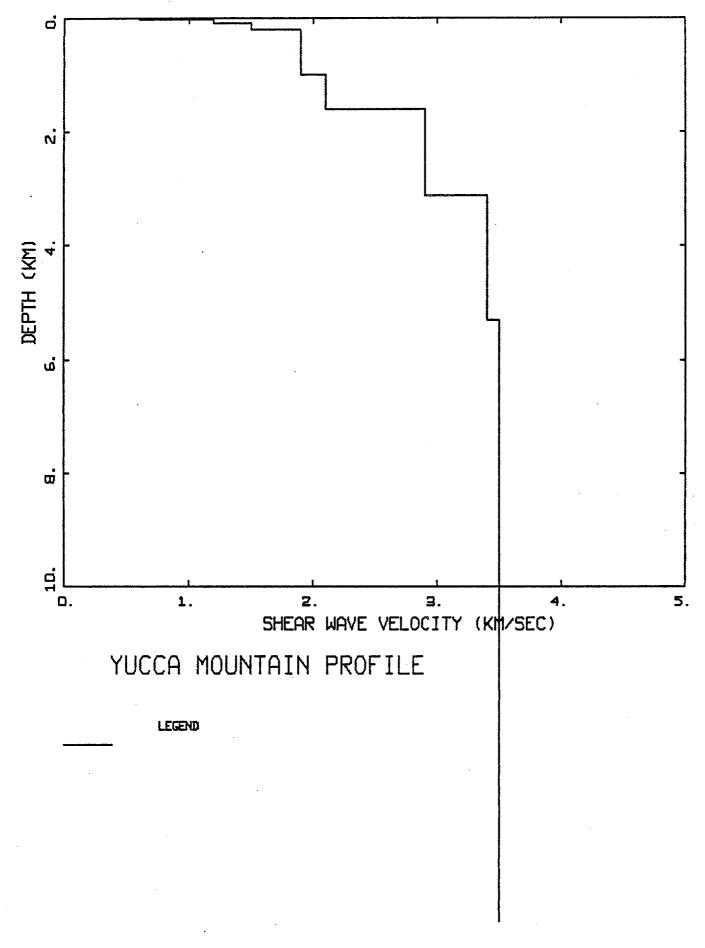
 $Q(f) = 250 f^{0.4}$ 

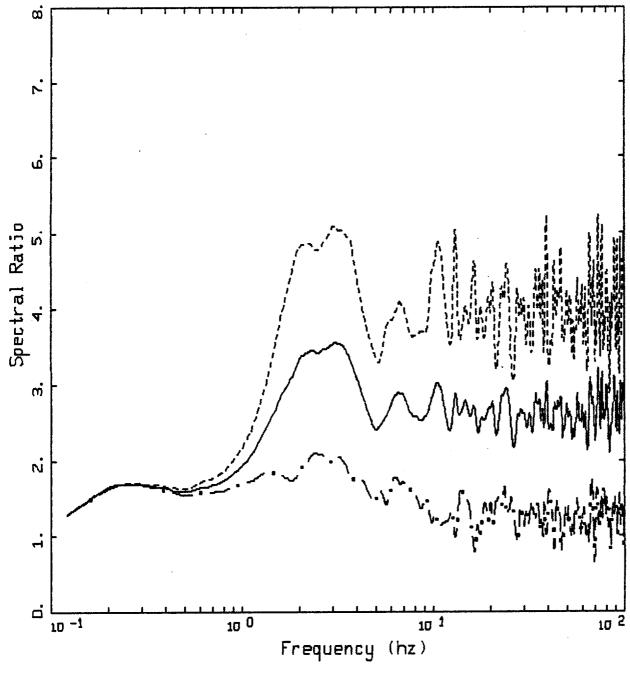
Crustal Model: Regional plus local near surface

Geometrical Attenuation: 1/R; 1/ $\sqrt{R}$ , R>64 km

Duration:  $1/f_c + 0.05 \text{ R} (\text{R} \ge 10 \text{ km})$ 

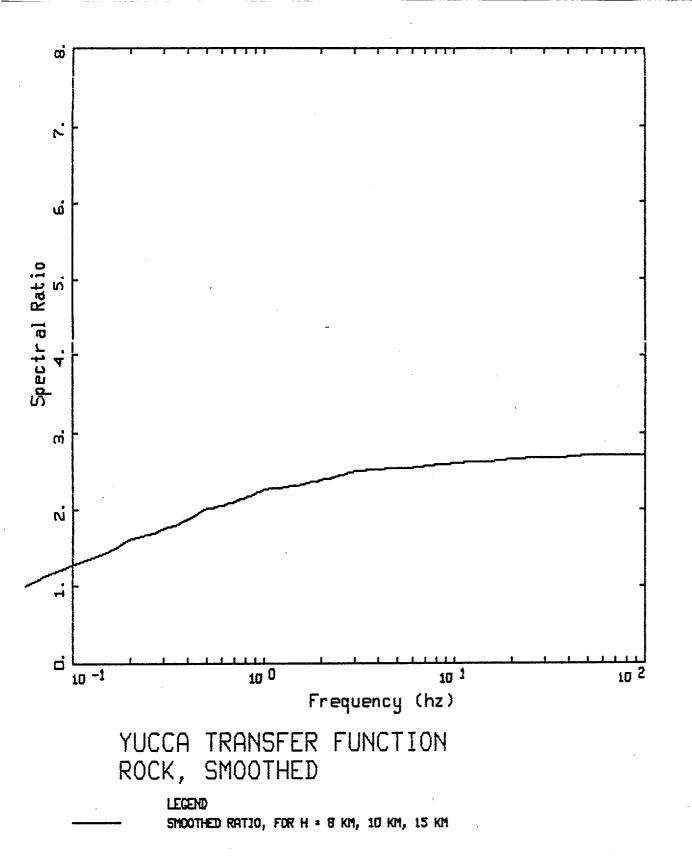
PGA Range: 10.25g - 0.0005g





YUCCA H=8 KM OVER HALFSPACE, RANDOMIZED PROFILE MEAN TRANSFER FUNCTION OF 30

LEGEND ----- GBTH PERCENTILE, 1 Hz SMOOTHING ----- MEAN, 1 Hz SMOOTHING ----- 3ZTH PERCENTILE, 1 Hz SMOOTHING



January 6, 1997

### ATTENUATION MODEL

$$\ln (y) = C_1 + C_2 (M - 6) + C_3 (M - 6)^2 - C_4 \ln (R) - C_5 R$$

 $R = SQRT (D^2 + H^2)$ 

VALIDATION:

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D = CLOSEST HORIZONTAL DISTANCE TO

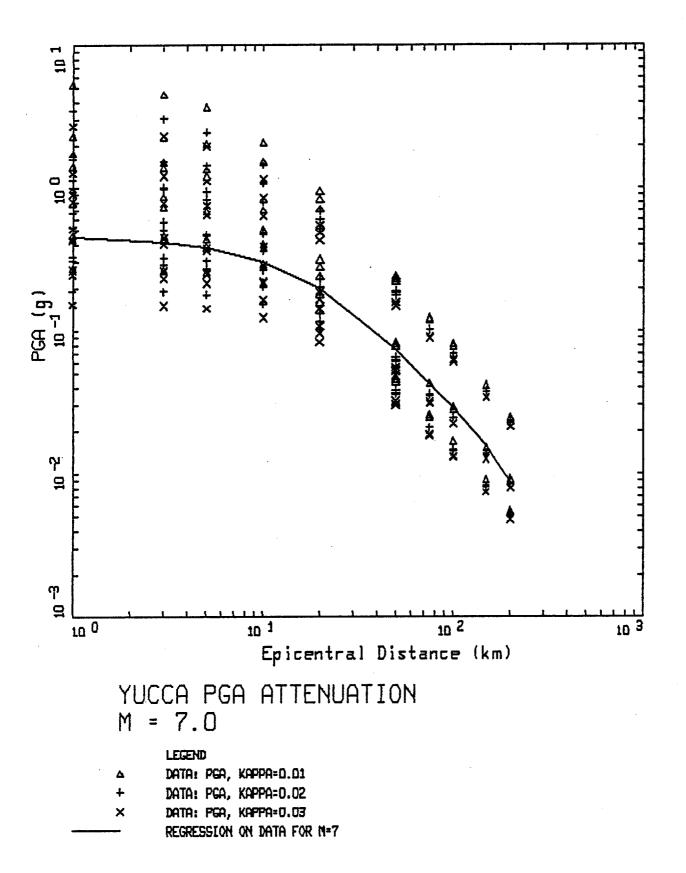
SURFACE PROJECTION

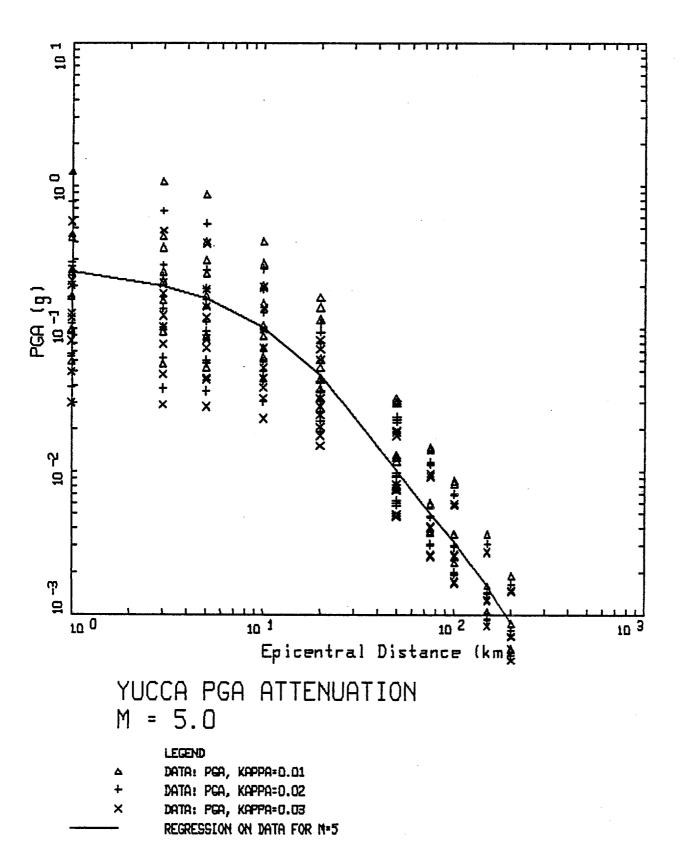
H = DEPTH TO ASPERITY ( $\approx 8 \text{ km}$ )

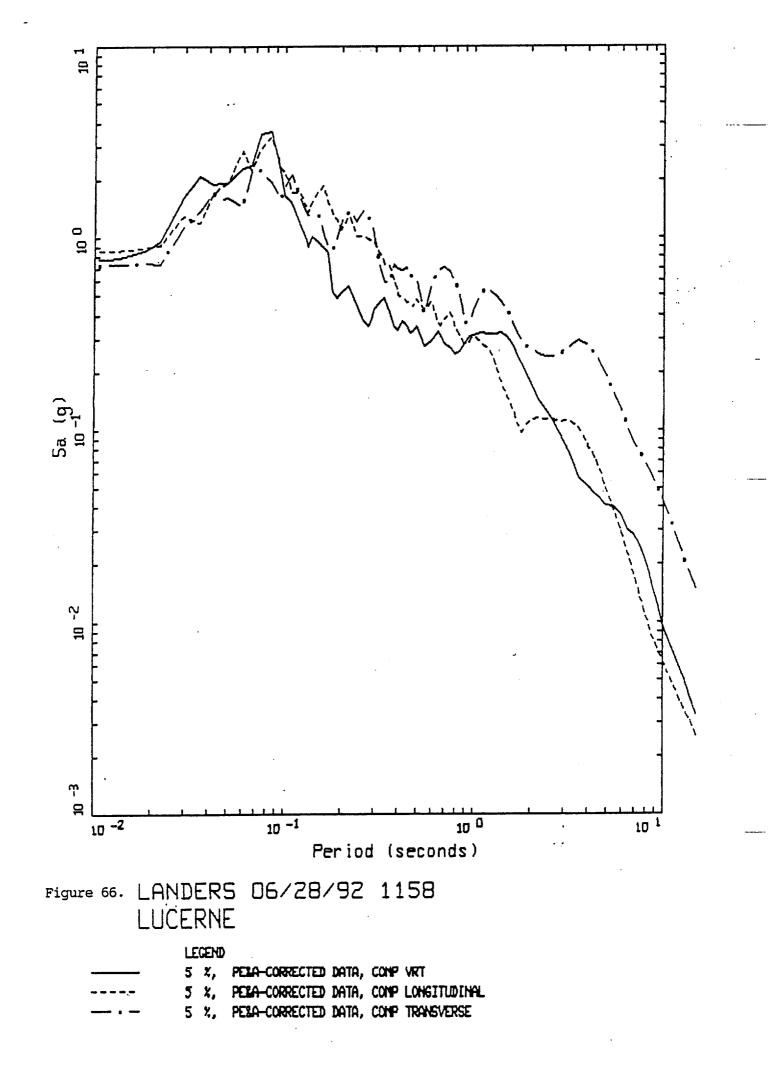
yucca/pres/equation

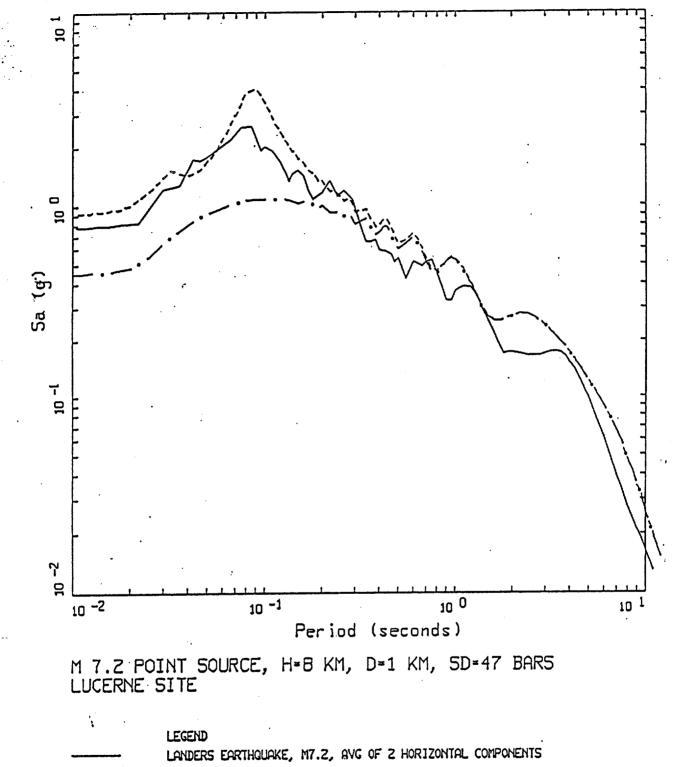
	REGRESSION WEIGHTS	3
Parameter		Weight
$\Delta\sigma$ (bars)		
25		0.185
50		0.630
200		0.185
Kappa (sec)		
0.01		0.185
0.02		0.630
0.03	·	0.185
М	H (km)	
5	5	0.80
	10	0.10
	15	0.10
6	5	0.10
	10	0.80
	15	0.10
		· · · · · · · · · · · · · · · · · · ·
7	5	0.10
	10	0.10
	15	0.80

yucca97\pres\regression









ENA 20 FT OVER LANDERS CRUST, K=0.016 SEC, PGA=0.90 G LANDERS CRUST, K=0.020 SEC, PGA=0.45 G

Comparison of 5% damped spectral acceleration: 1992 M 7.2 Landers earthquake recordings at the shallow stiff soil site Lucern (solid line) with motion computed using a point source at a depth of 8 km and epicentral distance of 1 km. The point source stress drop is 47 bars (based on multiple site inversions). Dash-dotted line: Landers hard rock crust with a kappa of 0.02 sec. Dashed line: 20 ft stiff generic ENA soil on Landers crust with a rock kappa of 0.016 sec.

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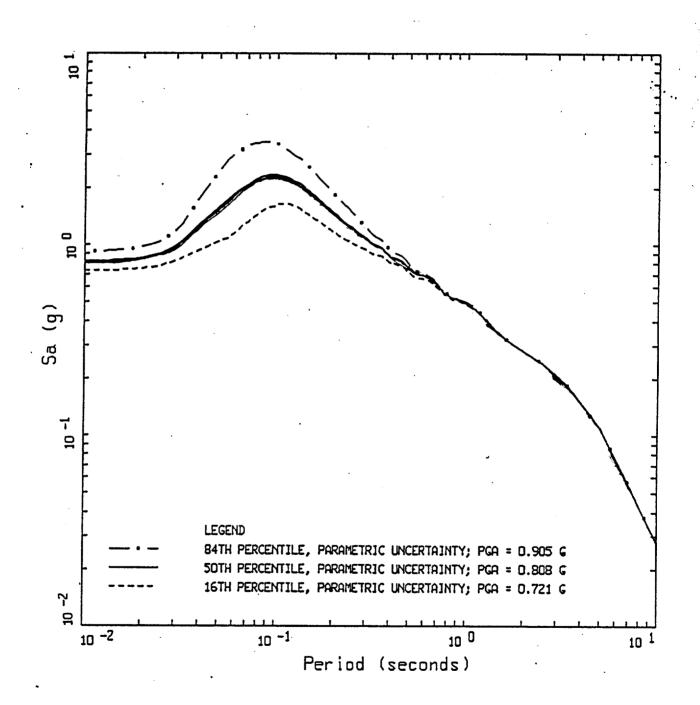
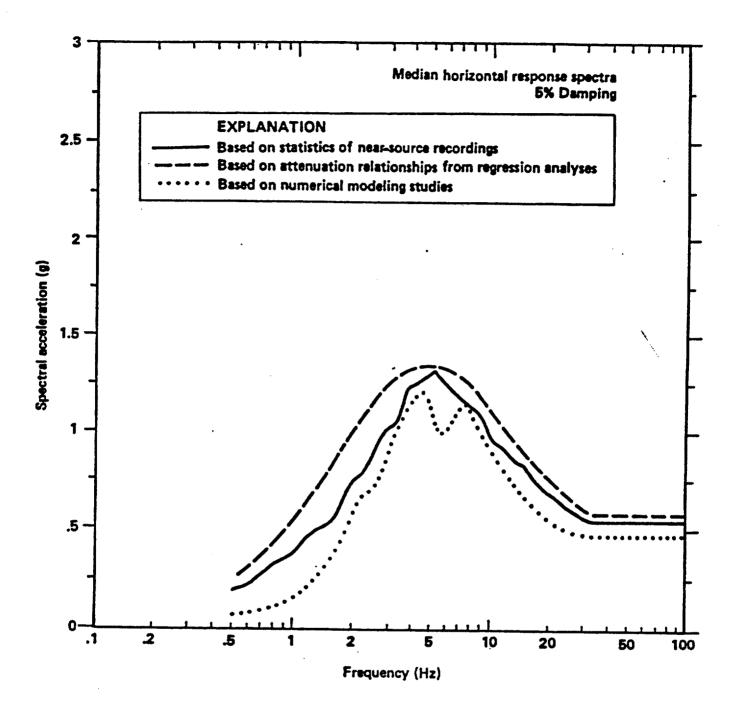
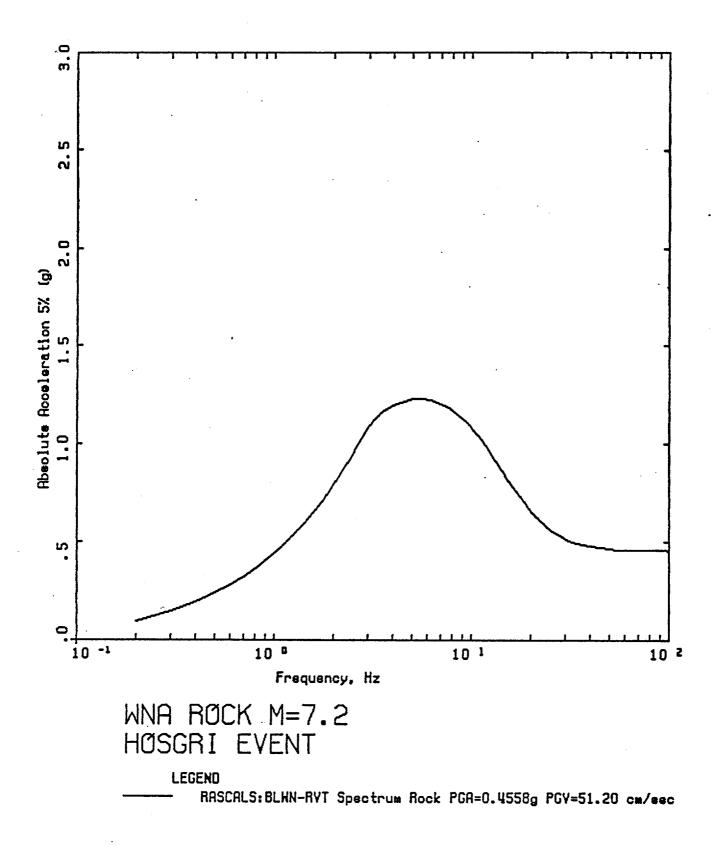


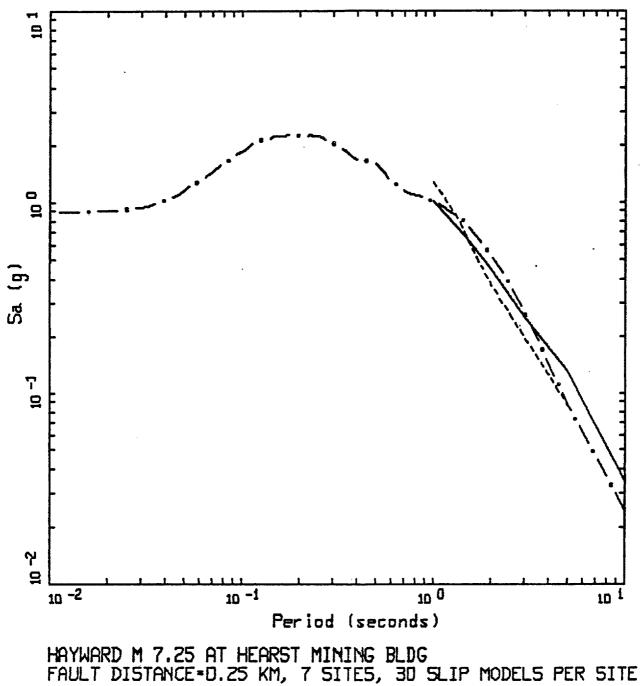
Figure 4. 5% damped spectral acceleration computed for site Lucern using the stochastic point source for a M 7.2 earthquake with a stress drop of 75 bars at an epicentral distance of 1.8 km and depth of 8 km. Median and 1-sigma estimates are based on 50 simulations using the random profiles shown in Figure 3.

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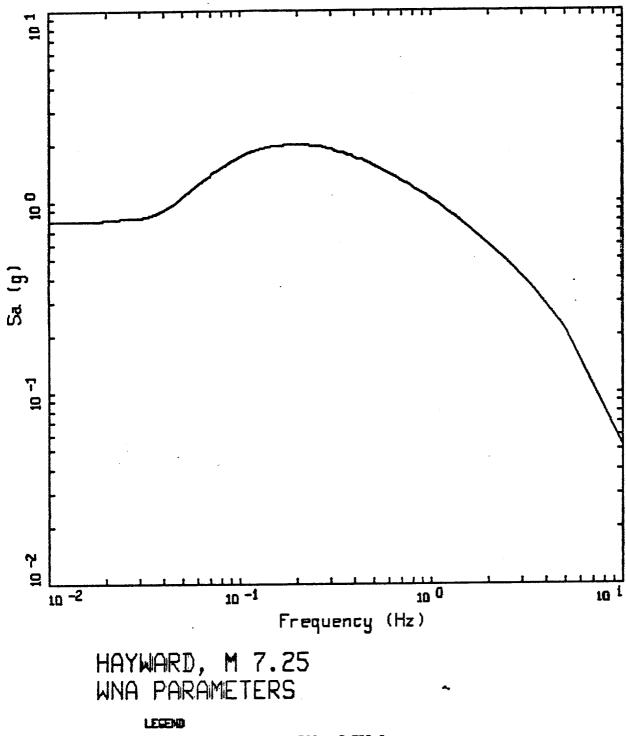


**Figure 14.** The Diablo Canyon site-specific median horizontal acceleration response spectra developed by PG&E, weighted for style of faulting as follows: 0.65, strike-slip; 0.30, oblique; 0.05, thrust (PG&E, 1988, Fig. 4-25).

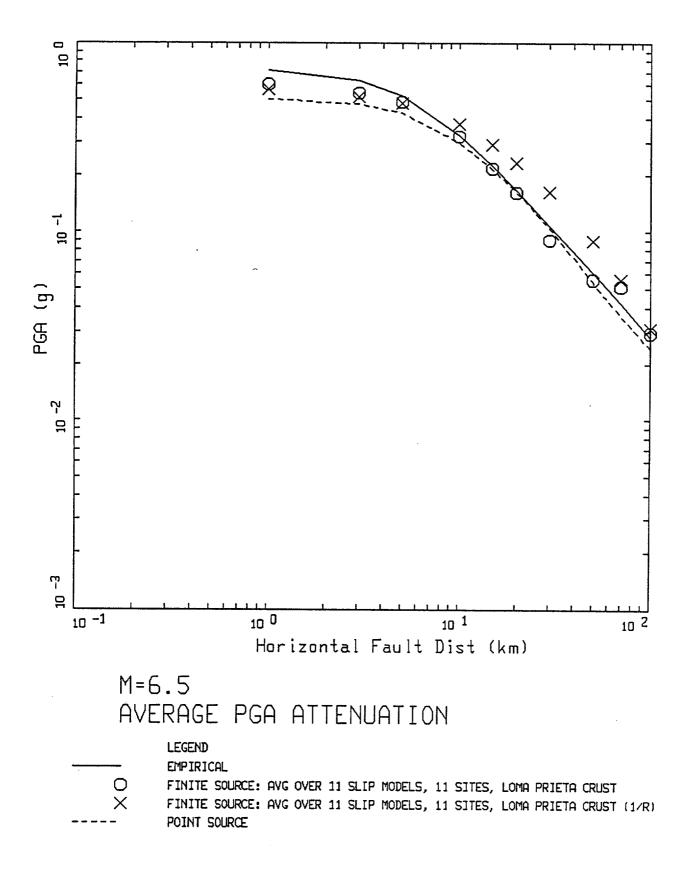


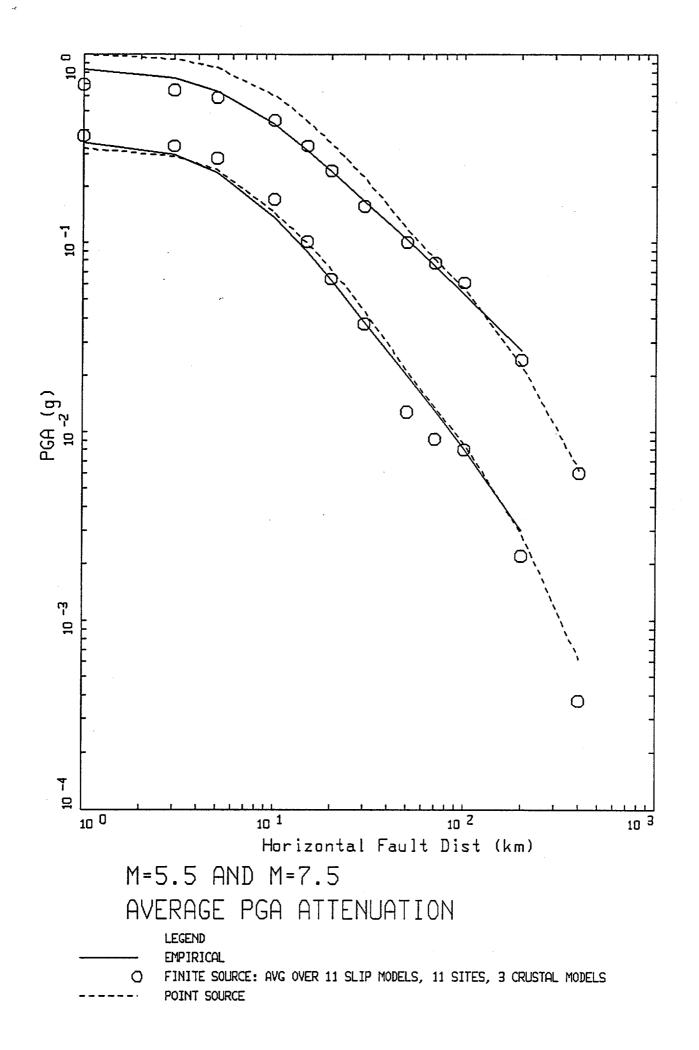


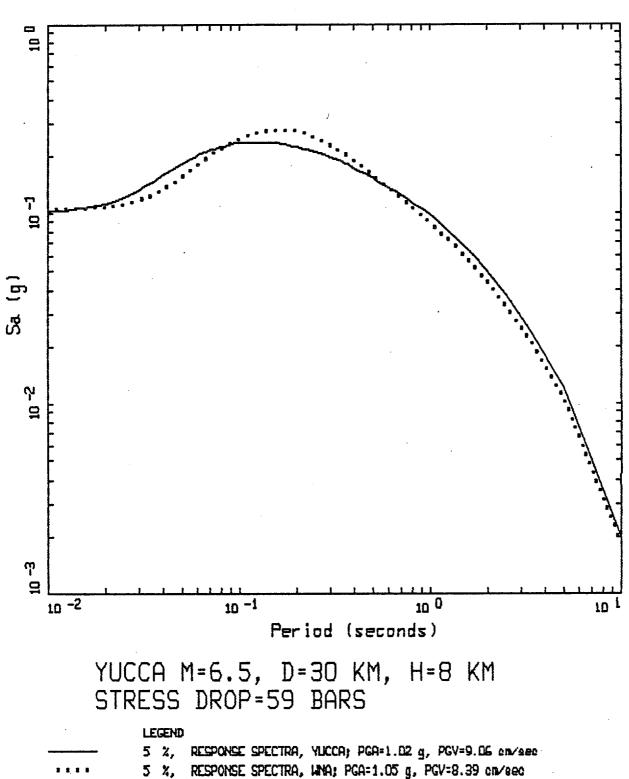
LEGEND EMPIRICAL LPA MEDIAN, RVT MEDIAN, DETERMINISTIC

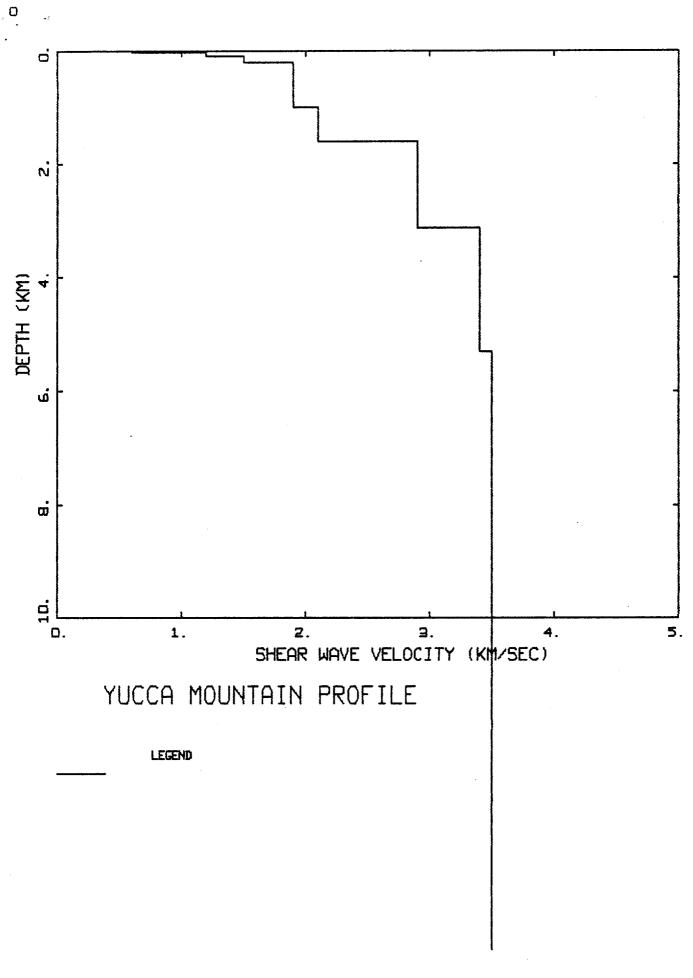


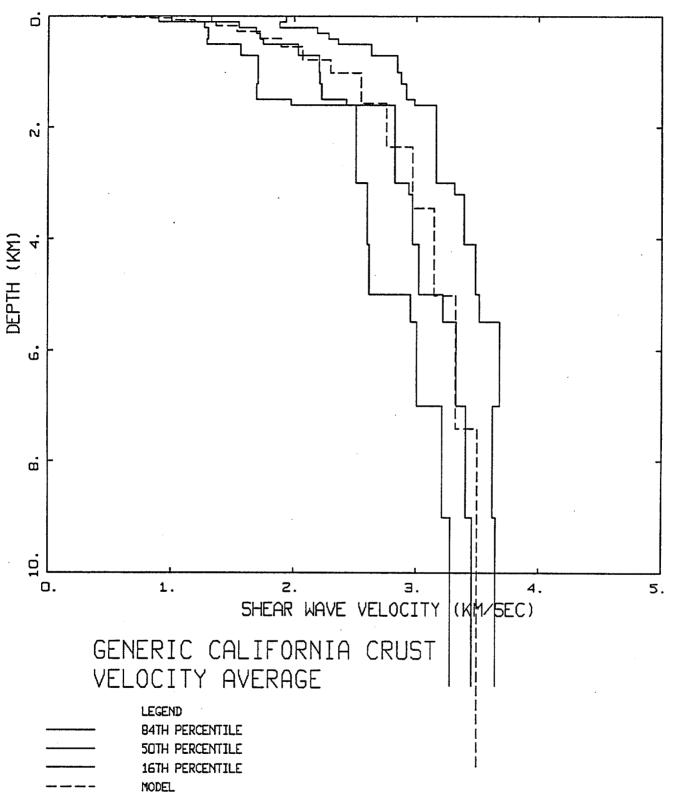
D = 0.25 KM, H = 8 KM; PGA = 0.798 G

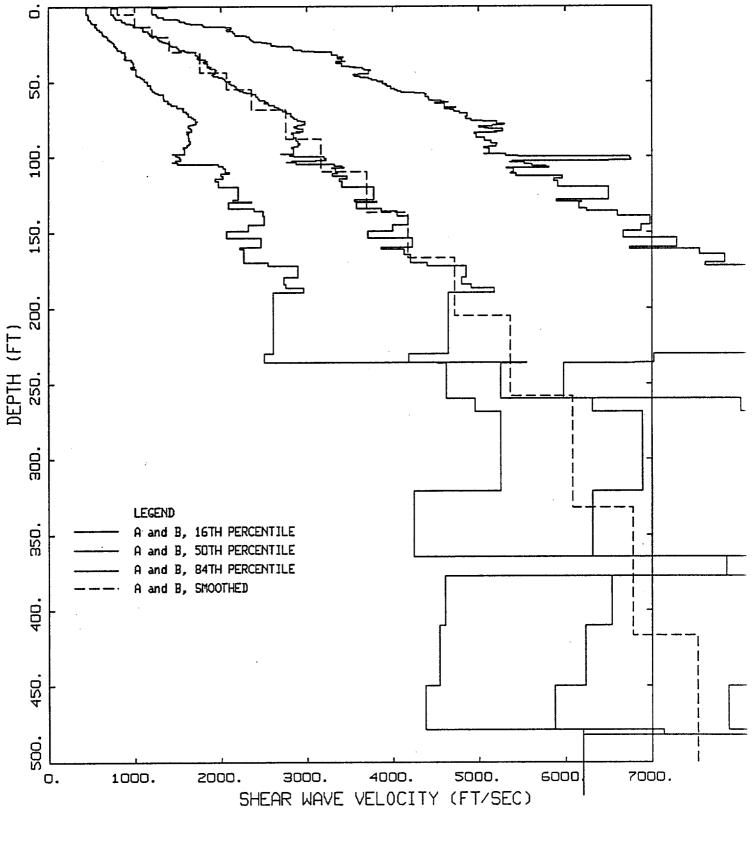




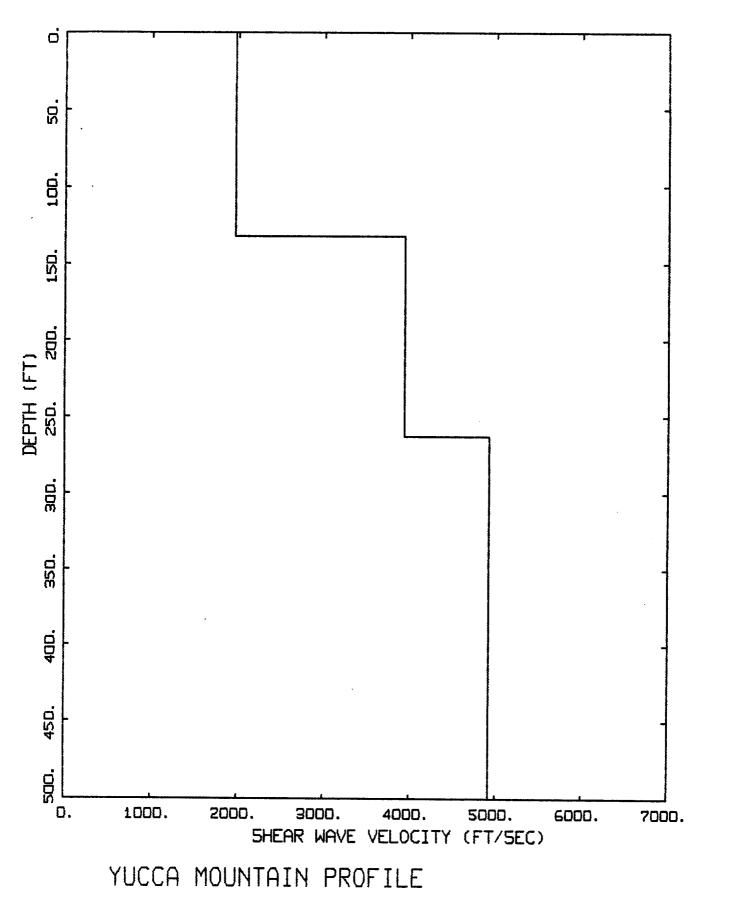






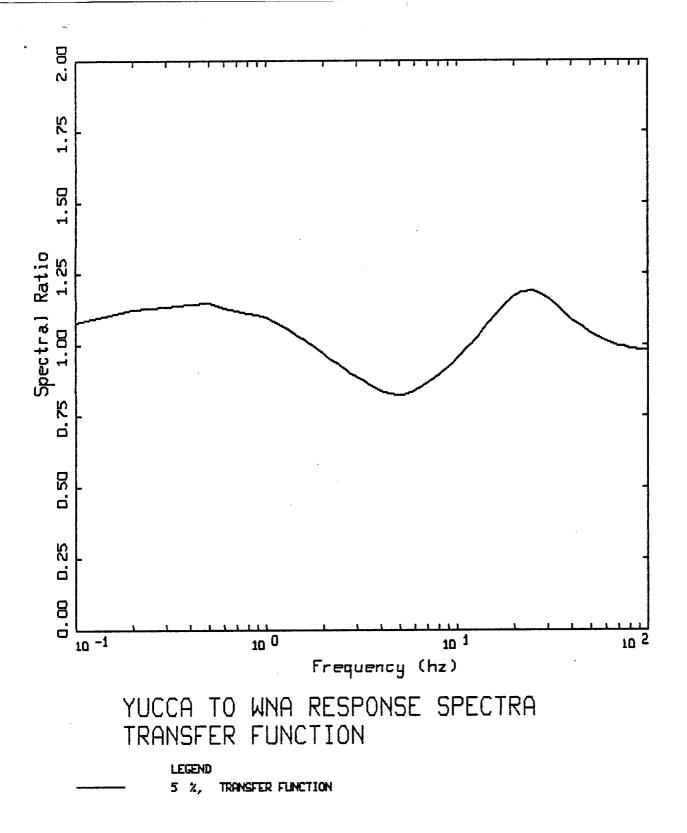


GEOMATRIX CLASS A & B

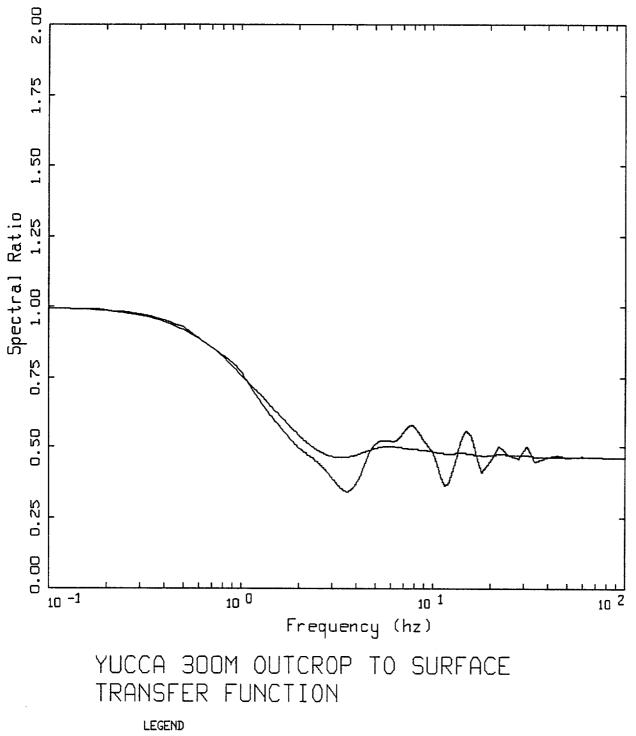


LEGEND

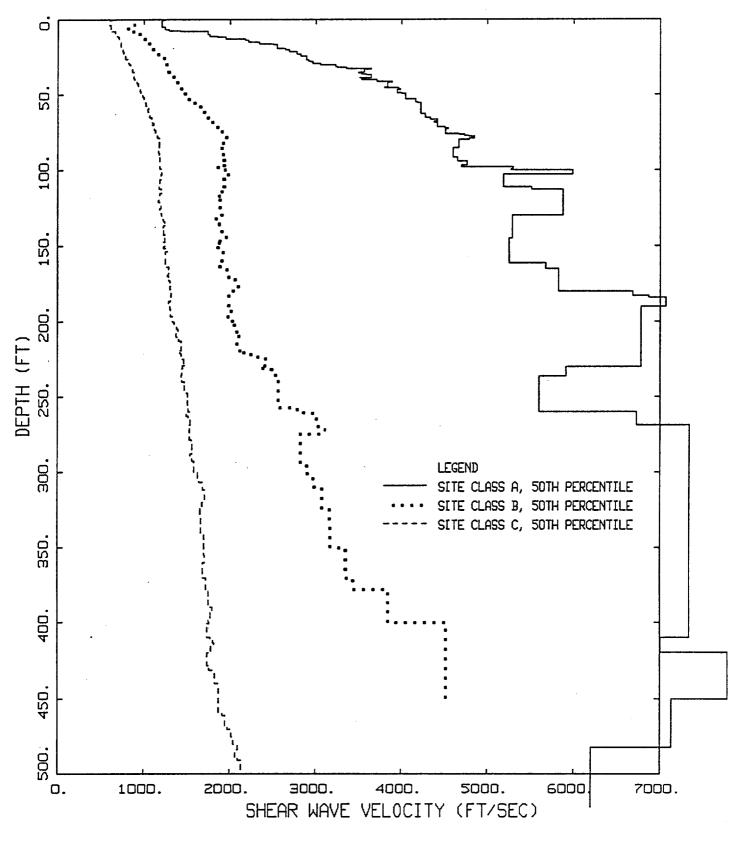
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- 5 %, TRANSFER FUNCTION
- 5 %, TRANSFER FUNCTION; 20 Hz smoothing



USGS SITE CLASSES VELOCITY AVERAGE

## **Major Limitations**

- Assumes similar near-source scaling characteristics in both regions
- Requires knowledge of earthquake, crustal, and site characteristics in both regions
- Seismological models are simplistic

EQE

Model	Type S	Site	California	Yucca Mountain						
			100 Bars	50 Bars		75 Bars		100 Bars		
			PGA (g)	Ratio	PGA (g)	Ratio	PGA (g)	Ratio	PGA (g)	
Abrahamson & Silva (1997)	Empirical	Rock	0.325	1.053	0.342	1.455	0.473	1.832	0.595	
Boore et al. (1997)	Empirical	V <sub>s</sub> =620 m/s	0.193	1.053	0.203	1.455	0.281	1.832	0.354	
Campbell (1997)	Empirical	Soft Rock	0.326	1.053	0.343	1.455	0.474	1.832	0.597	
Idriss (1997)	Empirical	Rock	0.290	1.053	0.305	1.455	0.422	1.832	0.531	
Sadigh et al. (1993)	Empirical	Rock	0.313	1.053	0.330	1.455	0.455	1.832	0.573	
Spudich (1996)	Empirical	Rock	0.186	1.053	0.196	1.455	0.271	1.832	0.341	
Silva	Theoretical	Site-Specific								
Zeng & Anderson	Theoretical	Site-Specific						·····		
Chin & Aki	Theoretical	Site-Specific								
Somerville & Saikia	Theoretical	Site-Specific								
MEAN			0.265		0.279		0.385		0.485	
SIGMA (EPISTEMIC)			0.114		0.114		0.114		0.114	

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#### PEAK GROUND ACCELERATION Moment Magnitude 6.5 at 10 km From Surface Trace of Vertical Strike-Slip Fault

# Methodology

• Point-source BLWN model

EQE

- Regional earthquake, crustal, and site characteristics
- **RVT** estimate of ground motion parameters
- Scaling factors California/Yucca Mountain
- Empirical estimate of California ground motion parameters from published attenuation relationships
- Hybrid estimate of Yucca Mountain ground motion parameters by applying regional scaling factors to California empirical ground motion estimates

# **Major Strengths** Based on empirically derived near-source scaling characteristics from published attenuation relationships Calibrated with strong-motion recordings Uses basic seismological principles to derive regional scaling characteristics EQE c:\trw\plots\Hybrid.ppt/colo/4

## **HYBRID EMPIRICAL GROUND MOTION MODEL**

## Kenneth W. Campbell

Yucca Mountain Ground Motion Workshop #2 Salt Lake City, Utah January 9-10, 1997



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# Objective

 Estimate ground motion parameters in a specific region by modifying empirical attenuation relationships developed for a different region using scaling parameters that account for differences in earthquake, crustal, and site characteristics between the two regions

EQE

Mw	Distance	Fault Type	PGA	Sigma			
	(km)		(g)	Aleatory	Epistemic		
6.5	10	Strike Slip	0.49	0.5	0.2		
6.5	10	Normal (Hanging Wall)	0.62	0.5	0.2		
6.5	10	Normal (Foot Wall)	0.44	0.5	0.2		

#### PEAK GROUND ACCELERATION Yucca Mountain Crust and Attenuation; 100 Bar Stress Drop

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#### PEAK GROUND ACCELERATION Moment Magnitude 6.5 on Hanging Wall at 10 km From Surface Trace of 65° Dipping Normal Fault

Ξ.

Model	Туре	Site	California 100 Bars PGA (g)						
				50 Bars		75 Bars		100 Bars	
				Ratio	PGA (g)	Ratio	PGA (g)	Ratio	PGA (g)
Abrahamson & Silva (1997)	Empirical	Rock	0.366	1.053	0.385	1.455	0.533	1.832	0.671
Boore et al. (1997)	Empirical	V <sub>s</sub> =620 m/s	0.306	1.053	0.322	1.455	0.445	1.832	0.561
Campbell (1997)	Empirical	Soft Rock	0.371	1.053	0.391	1.455	0.540	1.832	0.680
Idriss (1997)	Empirical	Rock	0.320	1.053	0.337	1.455	0.466	1.832	0.586
Sadigh et al. (1993)	Empirical	Rock	0.346	1.053	0.364	1.455	0.503	1.832	0.634
Spudich (1996)	Empirical	Rock	0.325	1.053	0.342	1.455	0.473	1.832	0.595
Silva	Theoretical	Site-Specific							0.930
Zeng & Anderson	Theoretical	Site-Specific							0.520
Chin & Aki	Theoretical	Site-Specific							0.460
Somerville & Saikia	Theoretical	Site-Specific	-+						0.630
MEAN			0.338		0.356		0.492		0.616
SIGMA (EPISTEMIC)			0.034		0.034		0.034		0.081

Model	Type	Site	California			Yucca N	Iountain		
			100 Bars	50 Bars		75 Bars		100 Bars	
			PGA (g)	Ratio	PGA (g)	Ratio	PGA (g)	Ratio	PGA (g)
Abrahamson & Silva (1997)	Empirical	Rock	0.325	1.053	0.342	1.455	0.473	1.832	0.595
Boore et al. (1997)	Empirical	V <sub>s</sub> =620 m/s	0.193	1.053	0.203	1.455	0.281	1.832	0.354
Campbell (1997)	Empirical	Soft Rock	0.297	1.053	0.313	1.455	0.432	1.832	0.544
Idriss (1997)	Empirical	Rock	0.290	1.053	0.305	1.455	0.422	1.832	0.531
Sadigh et al. (1993)	Empirical	Rock	0.313	1.053	0.330	1.455	0.455	1.832	0.573
Spudich (1996)	Empirical	Rock	0.186	1.053	0.196	1.455	0.271	1.832	0.341
Silva	Theoretical	Site-Specific							0.470
Zeng & Anderson	Theoretical	Site-Specific							0.220
Chin & Aki	Theoretical	Site-Specific							0.350
Somerville & Saikia	Theoretical	Site-Specific							0.630
MEAN			0.261		0.275		0.379		0.440
SIGMA (EPISTEMIC)			0.109		0.109		0.109		0.146

#### PEAK GROUND ACCELERATION Moment Magnitude 6.5 on Foot Wall at 10 km From Surface Trace of 65° Dipping Normal Fault

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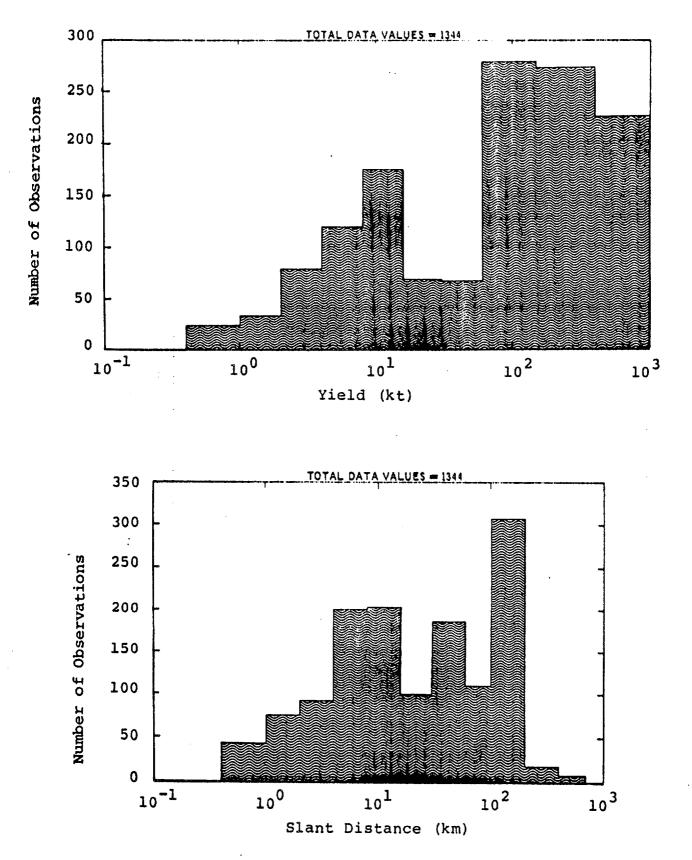
## Additional Information and Background Material

Maxwell Technologies, Inc. Federal Division Reston Geophysics Office 11800 Sunrise Valley Drive Suite 1212 Reston, Virginia 22091

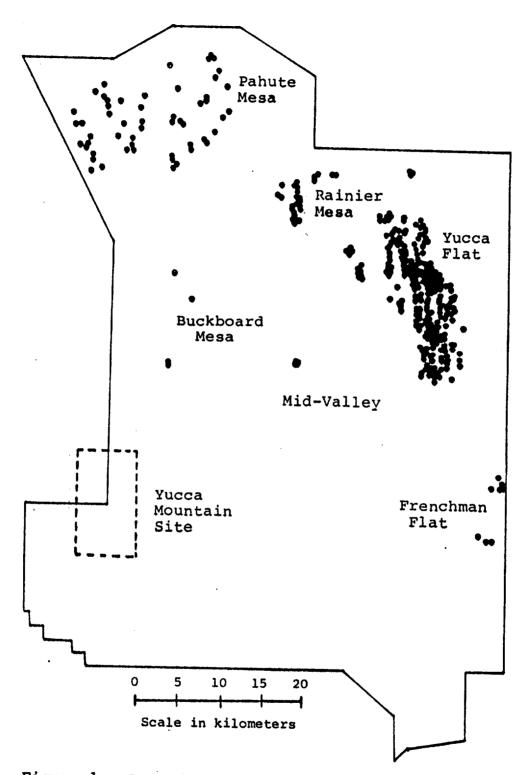
Further Results from Initial Phase of Work As presented in previous Phase 1 workshops.

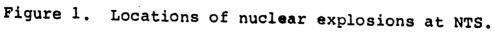
#### **Empirical Ground Motion Prediction** Goals for Yucca Mountain Repository

- **Objective:** Use large knowledge base of strong ground motion predictions for NTS underground nuclear explosions to help establish reliable prediction capability for potential earthquake scenarios which might affect the Yucca Mountain Repository site.
- Experience is based on a large database Advantages: • (thousands of recordings) covering a range of magnitudes, distances and site conditions comparable to earthquake scenarios under consideration for the site
  - Uses region-specific knowledge of attenuation
  - Large database was statistically analyzed to provide specific information on uncertainty associated with ground motion predictions
  - Can be used to identify potential site response problems which may affect predictions
- **Disadvantages:** Uncertainties associated with defining equivalence between earthquake and explosion source term
  - Mechanism differences, such as radiation pattern effects from finite sources, and focal depth differences are not accounted for



Distribution of acceleration data with respect to yield (top) and range (bottom).





Power Law Model for Ground Motion

### $\mathbf{A} = \mathbf{A}_{\mathbf{0}} \quad \mathbf{W}^{\mathbf{B}} \cdot \mathbf{R}^{\mathbf{C}}$

 $\log A = \log A_0 + B \log W + C \log R$ 

where

A = Peak or Spectral Ground Motion Parameter

W = Explosion Yield (kiloton)

R = Range (km)

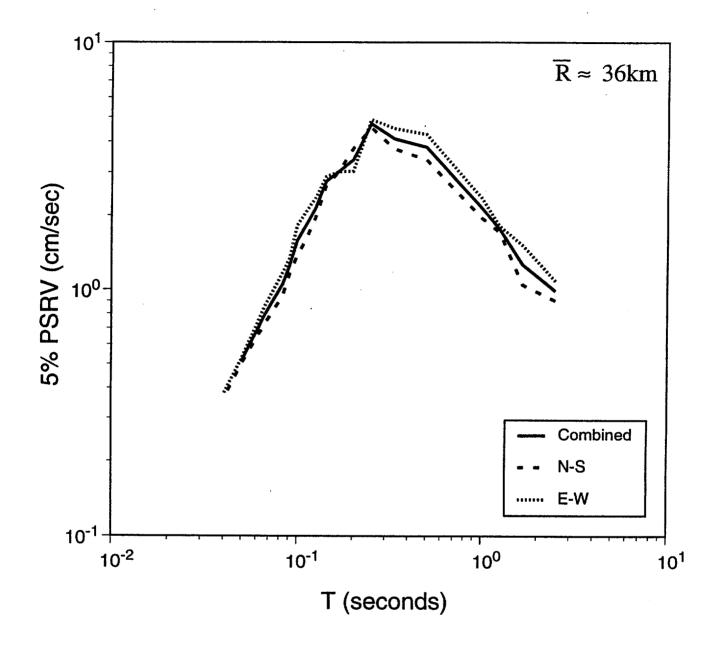
 $A_0$ , B, C = Constants Determined from Regression Analysis

### Outline of Empirical Ground Motion Prediction Methodology Based on Explosion Experience

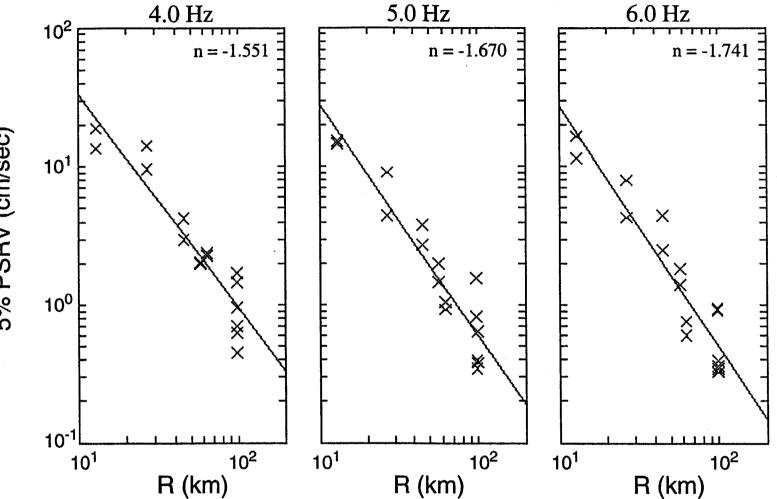
- Estimate source spectra corresponding to postulated earthquake scenarios:
  - A. Compare earthquake and explosion spectra for similar events at similar distances and stations to assess source equivalence.
  - B. Use magnitude relationships and magnitude/yield relations to determine earthquake/explosion equivalence.
  - C. Define response spectra levels at a near-source reference distance using nominal earthquake spectral scaling laws.
- Predict the PSRV ground motions:
  - A. Use the prediction relations developed from NTS experience to predict the spectra for the equivalent nuclear explosion source at the specified range of the scenario event.
  - B. Use the NTS experience to provide the attenuation adjustment to an earthquake near-source spectrum specified by other means for the scenario event.
- Assess uncertainties associated with the PSRV predictions based on NTS experience.
- Modify the spectra for site response using spectral comparisons between Yucca Mountain and average site response and other site response information.
- Assess the adequacy of predicted PSRV spectra in the light of historical earthquakes recorded near Yucca Mountain (e.g. Little Skull Mountain earthquake).

### <u>Analyses of Little Skull Mountain</u> <u>Earthquake Data</u>

- Performed Regression Analysis on PSRV Spectra for Little Skull Mountain main shock.
- Estimated Frequency Dependent Attenuation Relations for Little Skull Mountain Data and Compared with NTS Explosion Experience.
- Used NTS Nuclear Explosion Experience to Predict PSRV Spectra for Equivalent Explosion Source and Compared with Little Skull Mountain Spectra and Alternative Empirical Earthquake Prediction Models.
- Reviewed Uncertainty Factors Associated with PSRV Estimates and Compared to Uncertainty in Little Skull Mountain PSRV Regression.

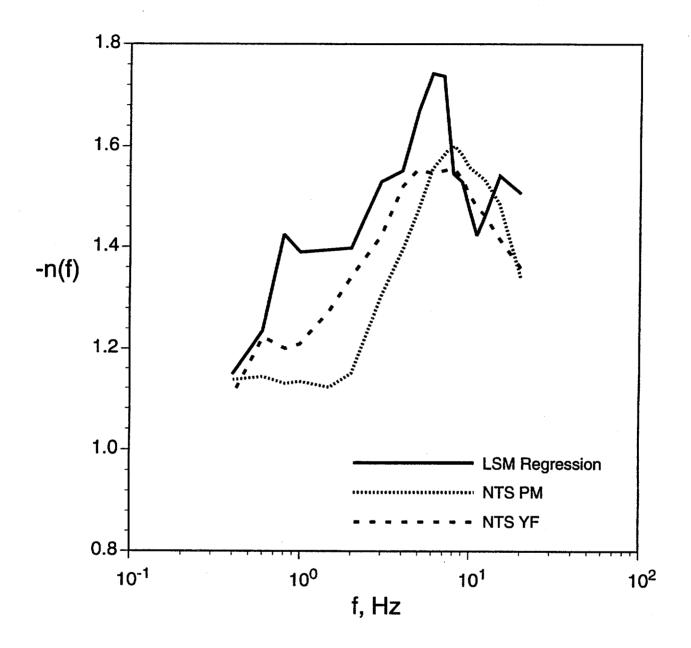


5% Damped PSRV spectra for the Little Skull Mountain earthquake projected at 36km based on regression of all horizontal component data compared with spectra based on separate regressions of each component.

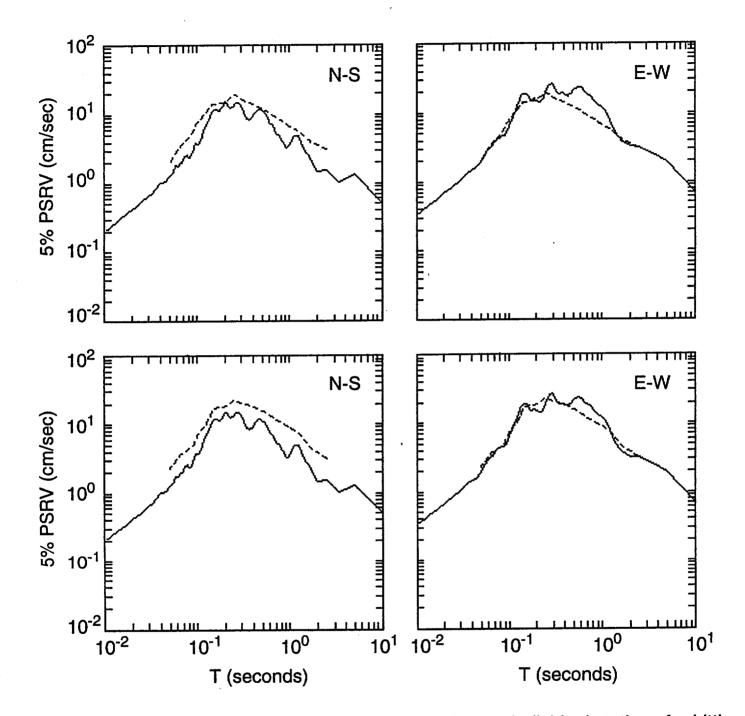


Examples of regression analyses applied to combined horizontal component PSRV spectra at individual frequencies for Little Skull Mountain earthquake. Similar analyses were performed for frequencies over a band from 0.4 Hz (2.5 sec) to 20 Hz (0.05 sec).

5% PSRV (cm/sec)

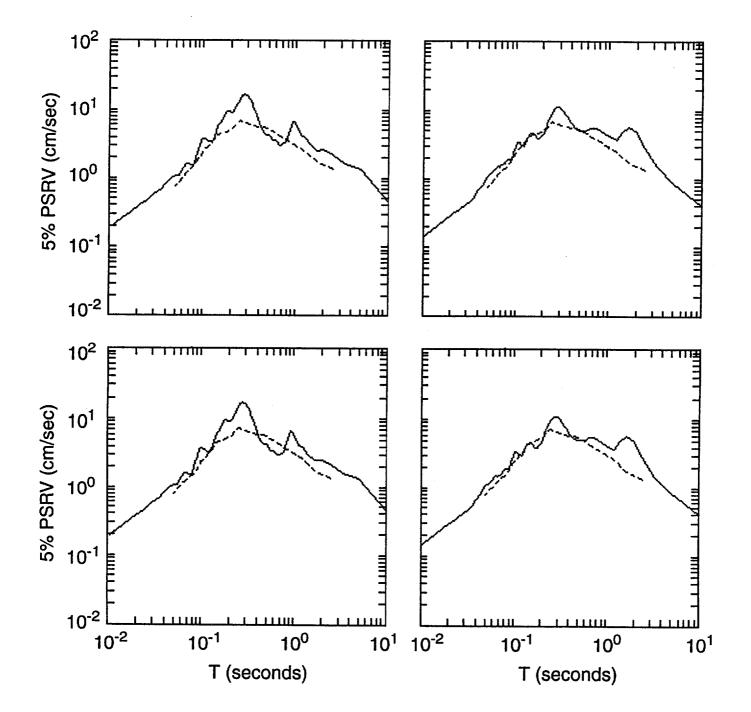


Comparison of 5% PSRV spectra attenuation exponents derived from combined regression of Little Skull Mountain horizontal components with similar regressions for nuclear explosion experience from Pahute Mesa (PM) and Yucca Flat (YF). Behavior is generally seen to be very similar. Note somewhat smoother appearance of curves for larger data samples. <u>R = 12.9 km</u>

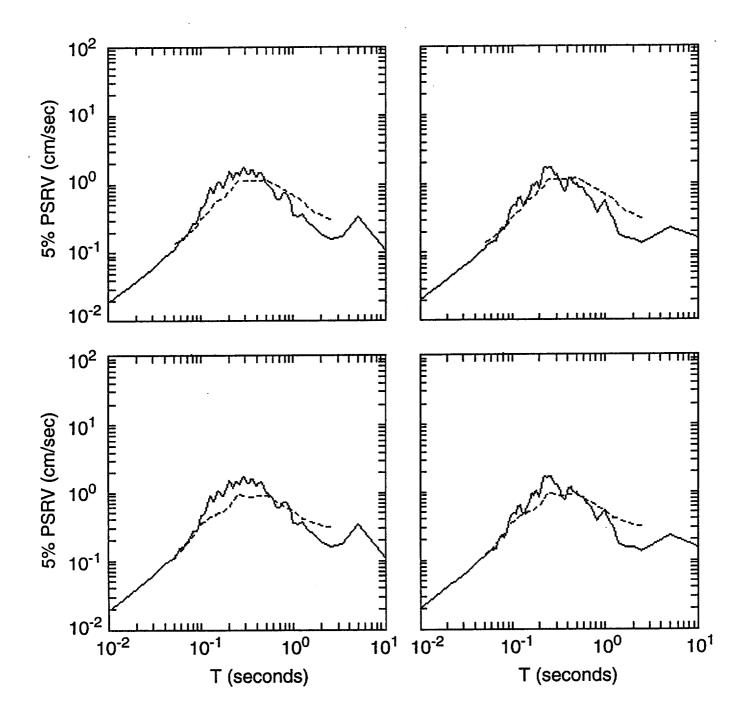


Comparison of PSRV predictions and observations at individual stations for Little Skull Mountain earthquake based on Pahute Mesa explosion attenuation experience (top) and LSM attenuation (bottom). Note fits are equally good for both attenuation relations suggesting that explosion attenuation experience can be used to predict earthquake attenuation over these ranges.

## <u>R =26.9 km</u>



<u>R =98.1 km</u>

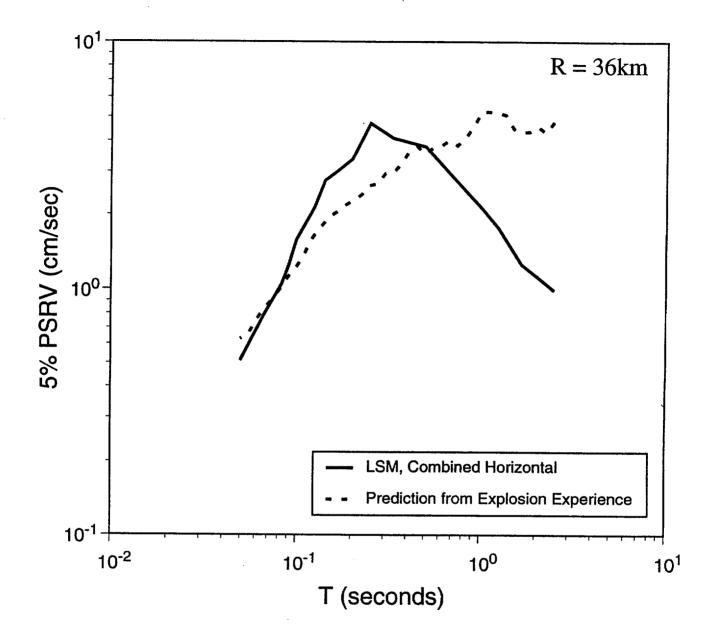


Empirical Ground Motion Predictions for Earthquakes Near NTS Based on Experience with Underground Nuclear Explosions

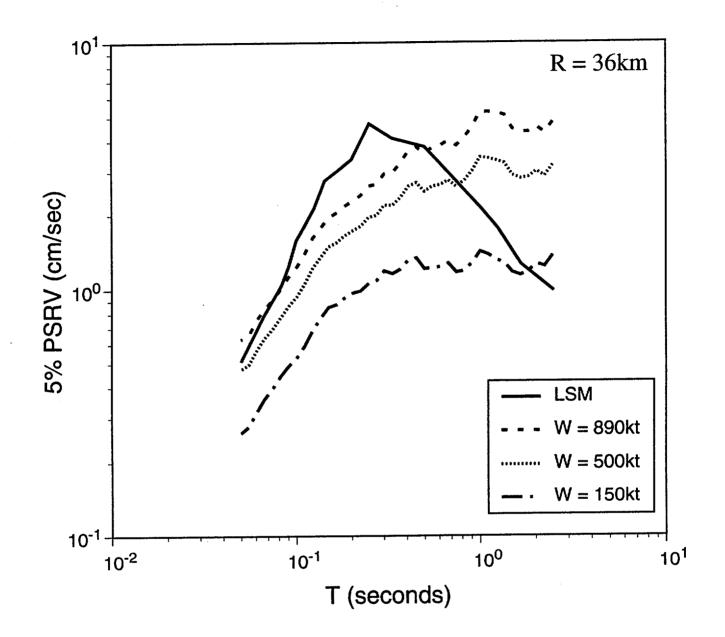
- Identify Nuclear Explosion Sources Equivalent to Postulated Earthquake Scenarios
- Predict the PSRV Ground Motions
- Assess Uncertainties Associated with PSRV Predictions
- Modify the Spectra for Site Response

Preliminary Procedure for Defining  
Earthquake/Explosion Equivalence  
Based on mb/MS Relations for  
Earthquakes and Explosions  
Houston and Kanamori (1986) for worldwide earthquakes:  
$$m_b = 0.53 \text{ Mw} + 2.7$$
  
 $M_w = 5.68 \longrightarrow m_b = 5.71$   
Richter (1957) for worldwide earthquakes:  
 $MS = 1.59 \text{ mb} - 3.97$   
 $m_b = 5.71 \longrightarrow MS = 5.11$   
Marshall (NTS Explosions):  
 $MS = 1.41 + 1.26 \log \text{ (Yield)}$   
 $MS = 5.11 \longrightarrow \text{ Yield} = 890 \text{ kt}$   
Murphy (NTS Explosions below water table):  
 $m_b = 3.94 + 0.81 \log \text{ (Yield)}$   
 $\text{Yield} = 890 \text{ kt} \longrightarrow m_b = 6.32$   
Therefore, at this magnitude level:  
For Earthquakes:  $m_b - MS = 0.60$   
For Explosions:  $m_b - MS = 1.21$   
Then, for the same MS (i.e. same Mw):  
 $m_b \text{ (Explosion)} \approx m_b \text{ (Earthquake)} + 0.61$   
 $m_b \text{ (Explosion)} \approx 0.53 \text{ Mw} \text{ (Earthquake)} + 3.31$ 

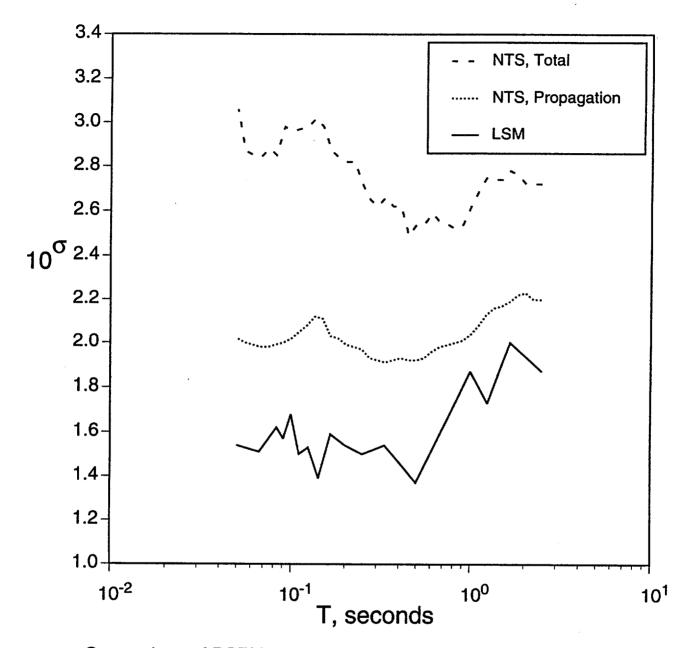
So, for a  $M_W = 5.68$  earthquake the explosion equivalent would have an mb = 6.32 corresponding to Yield = 890 kt.



Comparison of 5% PSRV spectrum for Little Skull Mountain earthquake at 36km with prediction based on nuclear explosion experience assuming approximate equivalence of  $M_w = 5.68$  earthquake and  $m_b = 6.33$  (Yield = 890kt) nuclear explosion. Fit is okay on average but does not match in detail, particularly at longer periods.



5% PSRV spectra predicted for 3 different explosion yields at R = 36km compared to PSRV spectra projected from LSM regression analysis. Lower yields show more tendency to decrease at longer period similar to behavior seen in earthquake spectral shape.



Comparison of PSRV uncertainty factors developed from regression analyses (1) for NTS explosions at Pahute Mesa for all yields, distances and stations (Total), (2) for Pahute Mesa explosions scaled to common yield for all distances and stations (Propagation), and (3) for Little Skull Mountain earthquake for all distances and stations. Note overall propagation uncertainty is roughly a factor of two.

## <u>Observations</u>

- Results of Regression Analysis on PSRV Spectra for Little Skull Mountain Main Shock Produce Frequency Dependent Scaling Exponents Comparable to Those Based on NTS Explosion Experience.
- PSRV Spectra Predicted for Equivalent Nuclear Explosion Agree with the Average Level of Spectra Observed for the Little Skull Mountain Main Shock, but Spectral Shapes Are Notably Different.
- Alternative Empirical Earthquake Prediction Models Produce PSRV Spectral Shapes More in Agreement with the Nuclear Explosion Predictions than with Little Skull Mountain Observations.
- PSRV Spectral Shapes May Vary Significantly between Stations Based on NTS Explosion Experience.
- Uncertainty Factors Associated with PSRV Spectral Estimates Can Be Relatively Large. Station Corrections May Help, but It Could Still Be Difficult to Obtain Uncertainty Factors Much Below About Two.

# Empirical Ground Motion Prediction for Specific Fault Scenarios

Objective: Apply three different empirical ground motion prediction models which utilize attenuation experience from NTS explosions to selected scenario earthquakes for the Yucca Mountain site.

### THREE EMPIRICAL PREDICTION MODELS

### (1) EQUIVALENT EXPLOSION WITH NTS ATTENUATION RELATIONSHIP

Using explosion with yield equivalent to Mw, apply explosion prediction relations for that yield based on NTS explosion experience to get 5 % damped PSRV spectra.

### (2) GEOMATRIX/ATC SPECTRAL SHAPE WITH NTS ATTENUATION RELATIONSHIP

Use Geomatrix/ATC model to determine 5 % damped PSRV spectra at range of 10 km and apply attenuation exponents based on NTS explosion experience to extend to other distance ranges.

(3) LITTLE SKULL MOUNTAIN EARTHQUAKE SPECTRAL SHAPE WITH GEOMATRIX/ATC MAGNITUDE SCALING AND NTS ATTENUATION RELATIONSHIP

Use LSM 5 % damped PSRV spectral shape at 36 km (mean distance of LSM observations) extend to other distances using attenuation exponents based on NTS explosion experience and scale up to desired magnitude using Geomatrix/ATC model.

# MODEL PARAMETERS

**Base Case Normal Fault Scenarios** 

<u>Mw</u>	<u>Distance</u> (Slant/Hypocentral)	Scenario
6.4	6.0 km	SC, BR, PC shallow (6 km)
6.4	8.6	Intermed. shallow
6.4	9.1	PC deep (9 km)
6.2, <b>6.4</b> , 6.6	10.0	SC, BR, BM, Intermed. deep
6.2 <b>, 6.4</b> , 6.6	25.9	Distant deep
6.4	26.9	Distant shallow

### **Base Case Strike-Slip Fault Scenarios**

<u>Mw</u>	<u>Distance</u> (Slant/Hypocentral)	<u>Scenario</u>
6.71	27.0 km	RV deep (9 km)
7.04	52.0	FC deep
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Where faults are Solitario Canyon (SC), Bow Ridge (BR), Paintbrush Canyon (PC), Bare Mountain (BM), Nominal Intermediate Distance (Intermed.), Nominal Distant (Distant), Rock Valley (RV), Furnace Creek (FC).

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# **Summary and Conclusions**

- We have developed three different empirical models which take advantage of the strong motion experience base for southern Nevada based on NTS explosion experience.
- We have applied these models to investigate empirical prediction capability for the LSM earthquake and several scenario earthquakes for the Yucca Mountain site.
- Observed attenuation for the LSM earthquake is not significantly different from that based on NTS explosion experience.
- Attenuation based on NTS experience is only slightly greater than that based on the Geomatrix/ATC standard; spectral predictions are generally within a factor of two.
- Equivalent explosion spectral predictions agree surprisingly well with other prediction methods; largest differences are at periods above about 1 second.
- LSM observed spectral and predictions based on LSM spectral shape are anomalously low at long periods compared to the other empirical prediction methods.

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